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Technical Report

SIMULATION OF THE FLIGHT OF A SHORT RANGE AIR DEFENSE SYSTEM ROCKET BEFORE RADAR ACQUISITION

by.

John E. Cochran, Jr. and James R. Beaty

under contract with

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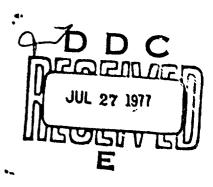
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SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered) READ INSTRUCTIONS BEFORE COMPLETING FORM REPORT DOCUMENTATION PAGE REPORT NUMBER 2. GOVT ACCESSION NO. 3 RECIPIENT'S CATALOG NUMBER TITLE (and Subtitle) TYPE OF REPORT & PERIOD COVERED SIMULATION OF THE FLIGHT OF A SHORT RANGE AIR Final Technical Report DEFENSE SYSTEM ROCKET BEFORE RADAR ACQUISITION. 1 October 1975-15 March . PERFORMING ONG. REPORT NUMBER AUTHOR(+) CONTRACT OR GRANT NUMBER(a) John E./Cochran, Jr. and James R./Beaty DAAG29-76-G-0069 PERFORMING ORGANIZATION NAME AND ADDRESS 10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS Engineering Experiment Station Auburn University Auburn, Alabama 36830 CONTROLLING OFFICE NAME AND ADDRESS U.S. Army Research Office REPORT DATE Apr**il 19**77 Fost Office Box 12211 NUMBER OF PAGES Research Triangle Park, NC 27709 116 4 MONITORING AGENCY NAME & ADDRESS(If different from Controlling Office) 15. SECURITY CLASS. (of this report) UNCLASSIFIED DECLASSIFICATION/DOWNGRADING SCHEDULE 16. DISTRIBUTION STATEMENT (of this Report) Approved for public release; distribution unlimited. 17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report) 18. SUPPLEMENTARY NOTES The findings of this report are not to be considered as an official Department of the Army position, unless so designated by other authorized documents. 19. KEY WORDS (Continue on reverse side if necessary and identify by block number) Short Range Guided Rockets Mallaunch Factors Digital Simulation Single-Axis Control Missile Flight Dynamics Stability and Control of Rolling Missiles Missile Guidance and Control STRACT (Continue on reverse side if necessary and identify by block number) This report deals with the problem of digitally simulating the motion of a Short Range Air Defense System (SHORADS) rocket during launch and until the rocket has been acquired by a launcher-fixed tracking radar. Physical and mathematical models of the launcher, the rocket per se and its environment, the rocket's control system and the pre-radar-acquisition guidance system are presented. The pre-acquisition guidance sensor is a dual field of view infrared angle sensor. The rocket is of the folding-wing, tube-launched, boost-

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sustain type and rolls at an essentially constant rate. Control torques are generated by deflecting the thrust of the solid-propellant, sustainer rocket motor and are available about a single rocket-fixed axis. The models for the launcher and rocket include the anomalistic effects of tipoff, launcher slew rate, rocket dynamic unbalance and thrust misalignment, aerodynamic forces and moments, jet damping, variable mass, and moments of inertia of the rocket and winds. Two computer codes - one for the launch phase and one for the post-launch, controlled phase - are also described and typical simulation results are presented and discussed. The rocket simulated performs well when various combinations of anomalies are present, but large slew rates of the launcher result in failure of the rocket to enter the field of view of the infrared sensor, if it is launched from a "lagging" tube.

SIMULATION OF THE FLIGHT OF A SHORT RANGE AIR DEFENSE SYSTEM ROCKET BEFORE RADAR ACQUISITION

FINAL REPORT

bу

John E. Cochran, Jr. and James R. Beaty

U.S. ARMY RESEARCH OFFICE

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PREFACE

This report describes physical and mathematical models which form the basis for two digital computer codes which can be used to simulate the motion of a Short Range Air Defense System (SHORADS) rocket before it is acquired by a launcher fixed tracking radar. Listings of the two computer codes as well as typical simulation results are also included herein.

Much of the material in this report also constitutes part of Mr. James R. Beaty's Master of Science thesis.

The assistance of Mr. John Howerton of the Army Missile Research and Development Command, Redstone Arsenal, Alabama, who provided technical data for this study is gratefully acknowledged.

Dr. Joe W. Reece, Co-Project Leader, is presently on leave from Auburn University and did not participate in the writing of this report. However, his contributions to the overall effort during its initial stages were indispensable in regard to the successful completion of this study.

The authors also gratefully acknowledge the patience and expertise of Mrs. Marjorie McGee, who typed the manuscript.

John E. Cochran, Jr.

Co-Project Leader

TABLE OF CONTENTS

		PREFACE
		LIST OF FIGURES i
		LIST OF TABLES
SECTION	1.	INTRODUCTION
	1.1	General Comments
	1.2	Scope of the Present Study
SECTION	2.	LAUNCH DYNAMICS
	2.1	Introductory Comments
	2.2	Launcher/Rocket System Physical Model
	2.3	Launcher/Rocket System Mathematical Model
	2.4	Initial Conditions for the Flight Phase 1
SECTION	3.	FLIGHT DYNAMICS
	3.1	Introductory Comments
	3.2	Physical Model for the Rocket
	3.3	Equations of Motion
SECTION	4.	GUIDANCE AND CONTROL
	4.1	General Comments
	4.2	Guidance
	4.3	Control
SECTION	5.	SIMULATION RESULTS 43
	5.1	General Comments
	5.2	Data Used in the Simulations
	5.3	Simulation Results

TABLE OF CONTENTS (CONT)

SECTION	6.	UMMARY, CONCLUSIONS AND SUGGESTIONS
	6.1	Summary
	6.2	Conclusions
	6.3	Suggestions
		EFERENCES
APPENDI	ΥА.	LISTING OF MISSILE SIMULATION (MISSIM) PROGRAM 81
APPENDI)	ζВ.	LISTING OF SIMPLIFIED MISSILE/LAUNCHER (MISSLNCH) SIMULATION PROGRAM
APPENDIX	C.	AERODYNAMIC CHARACTERISTICS

LIST OF FIGURES

Figure No		<u>Pa</u>	ge No
2-1	Launcher Model	•	6
2-2	Geometry During Tipoff		9
2-3	Orientation of the Rocket-Fixed System	•	14
2-4	Geometry at the End of Tipoff		15
3-1	Solid and Fluid Portions of the Rocket	•	18
3-2	Rocket with Wings Unfolded		18
3-3	Thrust Misalignment Angles	•	21
3-4	Control Force Orientation		23
3-5	Aerodynamic Forces and Moments		23
3-6	Notation Used in Equations of Motion	•	28
3-7	Geometry of Solid Propellant Charge	•	28
4-1	IR Guidance Geometry	•	33
4-2	Target Location	•	35
4-3	Control Regions	•	38
4-4	Non-rolling Coordinate System	•	38
5-1	Pitch Control Time, Δt_y , for Simulation 1		49
5-2	Commanded Non-rolling Angular Rate, Q_{NR} , for Simulation 1	•	50
5-3	Non-rolling Angular Rate, $Q_{\mbox{NR}}$, for Simulation 1		51
5-4	Rocket-fixed Angular Rate, Q, for Simulation 1	•	52
5-5	Yaw Control Time, Δt_y , for Simulation 1	•	53
56	Commanded Non-rolling Angular Rate, $R_{NR_{_{\scriptsize C}}}$, for Simulation	1	54
5-7	Non-rolling Angular Rate, R_{NR} , for Simulation 1	•	55
5-8	Rocket-Fixed Angular Rate, R, for Simulation 1		56

LIST OF FIGURES (CONT)

Figure No.	Page No.
5-9	Angle of Attack Time History
5-10	Sideslip Angle Time History
5-11	Pitch Angle Time History 60
5-12	Yaw Angle Time History 61
5-13	Yaw Angle vs. Pitch Angle 63
5-14	Time History of x_G -Coordinate of C 64
5-15	Trajectory for Simulation 1 65
5-16	Trajectory for Simulation 2 66
5–17	Trajectory for Simulation 3
5-18	Trajectory for Simulation 4 69
5-19	Trajectory for Simulation 5
5-20	Trajectory for Simulation 6
5-21	Trajectory for Simulation 7
5-22	Trajectory for Simulation 8
5-23	Trajectory for Simulation 9
5-24	Trajectory for Simulation 10

LIST OF TABLES

Table No.	•
5-1	Launch Phase Data
5-2	Description of Flight Conditions
5-3	Flight Phase Data
C-1	Aerodynamic Characteristics

SECTION 1. INTRODUCTION

1.1 General Comments

The rising costs of design, development and testing of modern weapon systems coupled with the availability of high-speed digital computers have led to increased utilization of digital computer codes to simulate proposed and existing weapon systems. A wealth of information about the operation of a weapon system can be obtained from such simulation codes if they are properly devised. The type of information may range from results which are only order-of-magnitude estimates of say, accelerations and angular rates, to very accurate predictions or reproductions of the system behavior as a function of time. This report describes the development and use of two simulation codes of moderate complexity which are intended for use in determining the effects of various anomalies, such as dynamic imbalance and winds, and of certain inherent characteristics of a particular type of weapon system.

1.2 Scope of the Present Study

This report deals with the problem of simulating the motion of a Short Range Air Defense System (SHORADS) type rocket during the "capture" or pre-radar-acquisition portion of flight. This portion of the rocket's flight includes its launch from a tube attached to the rotating turret of a ground-based mobile launcher and the rocket's motion prior to its being acquired by a launcher-based tracking radar. The part of the flight after launch and prior to radar acquisition can be divided into two subparts. The first subpart is a stabilized, but unguided, flight phase which begins when the

aft end of the rocket leaves the launch tube and ends when the aft end of the rocket enters the field of view (FOV) of an infrared (IR) angle sensor, the sight axis of which is bore-sighted with that of the radar. (The IR sensor senses the position, within its conical FOV, of flares on the rocket's aft end.) The second subpart is a flight phase in which signals from the IR sensor and pre-specified range versus time relationships are used to determine guidance commands for the rocket. This phase begins when the IR sensor acquires the rocket's flares and ends when the tracking radar acquires contact with the rocket.

A simulation code has previously been developed for the purpose of simulating the motion of a SHORADS type rocket from launch tube exit until the end of its flight. That code is very complicated, due to the fact that an attempt was made to simulate the actual operation of all subsystems. It does not, however, contain a provision for simulating the launch phase, nor does it contain a rocket mathematical model which includes certain anomalies considered in this study and included in the "post-launch" simulation code described herein.

Two digital computer codes were developed during this study. The first is a simplified launch dynamics code and the second is the post-launch simulation code cited above.

Section 2 of this report contains a description of the physical and mathematical models which form the basis for the launch dynamics code. The launcher is modeled as a rigid, fixed base to which a rigid turret with two rigid launch tubes is attached. The turret is assumed to rotate about a vertical axis with constant angular speed. For launch dynamics purposes, the rocket is modeled as a constant mass, axisymmetric rigid body. The

effects of tipoff of the rocket are modeled. The desired output of the launch dynamics code is the initial state vector of the rocket at the instant its aft end leaves the launch tube.

The physical and mathematical models of the rocket are presented in Section 3. The rocket is modeled as a variable mass body in the sense that the indirect effects of variations in its mass and moments of inertia with time and the direct effects of thrust, torque due to thrust, and jet damping due to internal flow are modeled. The rocket modeled herein is of the folding-wing, cruciform, boost-sustain type. It is assumed to be spunup to a relatively low roll rate (say, 5 cps) during launch and to maintain an essentially constant roll rate after launch. The thrust of the rocket as a function of time is assumed to be available in tabular form. Its mass is modeled as a piecewise linear function of time. Also, the aerodynamics characteristics of the rocket are assumed to be available in tabular form. For example, $C_{\rm N}$, the normal force coefficient, is assumed to be available as a tabulated function of the flight Mach number and the incidence angle of the rocket.

Control is accomplished by deflecting the thrust vector of the sustainer rocket motor with small "control vanes" which are located at the exit plane of the sustainer nozzle. Control torques about a single transverse axis fixed in the rocket are generated by the deflected thrust. Since the rocket is rolling rapidly, control torques can be applied alternately to control pitch and yaw plane motions of the rocket. The magnitude of the control torque produced by deflecting the control vanes is assumed constant (a delay time is, however, modeled) and the "amount" of control is determined by the length of time the vanes are deflected in a given direction; i.e., the dwell time.

A simple control law is described in Section 4. Under this law, the dwell time is determined as a linear combination of deviations of the rocket's center of mass from the launcher-to-target line-of-sight, the time rates of change of these deviations and the pitch rate of the rocket. The choice of control gains which appear in the control law is also discussed in Section 4.

Results obtained using the launch dynamics (LD) and pre-radar-acquisition (PRA) codes are presented in Section 5. Plots of the flight paths of the rocket for when its motion is affected by various anomalistic factors are shown and discussed.

Section 6 contains a summary of the main findings of this study and also contains some recommendations for further work in simulating the launch of SHORADS rockets.

Throughout this report, the words rocket and missile will be used interchangeably.

SECTION 2. LAUNCH DYNAMICS

2.1 Introductory Comments

Often, the launch phase is neglected when simulations of rocket systems are conducted. The reason for this neglect often is a belief on the part of the one conducting the simulations that the effects of the rocket's motion during the launch phase may be accounted for by varying the initial conditions for the post-launch motion. This may be the case, but one should not be led to believe that it is always so. The main fault of the process of simply varying initial conditions to simulate "bad launches," tipoff, etc., is that the initial conditions may not be consistent and hence may lead to spurious results.

The launch phase is not as adequately treated herein as it could have been if the majority of the time available had not been spent on the post-launch phase. At the beginning of this study, it was anticipated that an existing launch dynamics code² would be used to simulate the launch phase. That code did not appear suitable, however, since it does not contain a model for a launcher with a rapidly rotating turret. Rather than modify it, a relatively simple physical model for the launcher/rocket system during launch was formulated, the associated mathematical model derived and a new code incorporating this new model written.

2.2 Launcher/Rocket System Physical Model

The physical model for the launcher/rocket system during the launch phase is shown schematically in Fig. 2-1. It consists of a rigid, fixed base, a rigid turret and two rigid launch tubes. The turret rotates relative to the base about a vertical axis. The launch tubes may be rotated to different

elevation settings. It is assumed that during launch the turret rotates at a constant rate and that the launch tubes are fixed with respect to the turret. The rocket model is a rigid (constant mass) axisymmetric body.

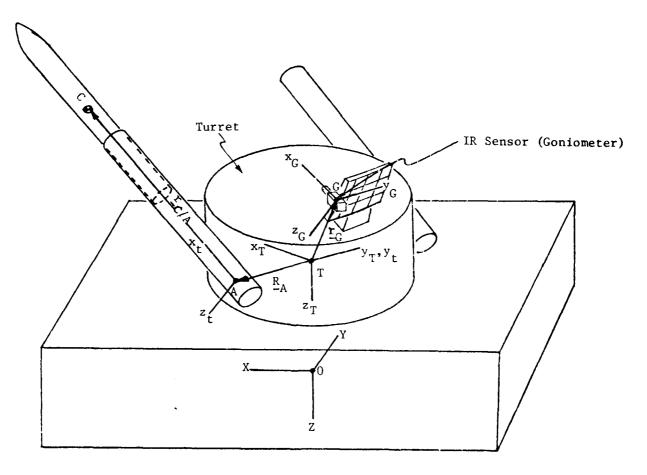


Figure 2-1. Launcher Model

2.3 Launcher/Rocket System Mathematical Model

The launch phase is divided into two parts for the purposes of deriving equations of motion for the rocket (No equations of motion are needed for the launcher, since its motion is specified a priori.). The first part of the launch phase is one in which the rocket translates along a tube, while it spins within the tube. The second part is one in which the rocket is

supported only at a point near its aft end and hence "tips off"; i.e., rotates relative to the tube about a transverse axis.

Motion During the First Part of the Launch Phase

During the constrained translational part of the launch phase, the position of the rocket's center of mass C is given by

$$R_{C} = R_{A} + r_{C/A}$$
 (2-1)

where \underline{R}_A is a vector from point T, the origin of the turret-fixed $\mathrm{Tx}_T y_T z_T$ system, to point A, the origin of the tube-fixed $\mathrm{Ax}_t y_t z_t$ coordinate system and $\underline{r}_{C/A}$ is a vector from A to C, the center of mass of the rocket. If it is assumed that the turret rotates with a constant angular velocity $\underline{\omega}_T = \omega_T \hat{k}_T$, where \hat{k}_T is a unit vector fixed to the z_T -axis, the acceleration of C is

$$\frac{\ddot{\mathbf{R}}_{\mathbf{C}}}{\mathbf{E}} = \underline{\omega}_{\mathbf{T}} \times [\underline{\omega}_{\mathbf{T}} \times (\underline{\mathbf{R}}_{\mathbf{A}} + \underline{\mathbf{r}}_{\mathbf{C}/\mathbf{A}})]$$

$$+ 2 \underline{\omega}_{\mathbf{T}} \times \underline{\mathbf{r}}_{\mathbf{C}/\mathbf{A}} + \underline{\mathbf{r}}_{\mathbf{C}/\mathbf{A}}, \qquad (2-2)$$

where the small circle denotes differentiation of the components of a vector expressed in terms of the tube-fixed unit vectors $\hat{\mathbf{i}}_t$, $\hat{\mathbf{j}}_t$ and $\hat{\mathbf{k}}_t$. Since the \mathbf{z}_t - and \mathbf{y}_t -motions of the rocket are constrained to be zero during this part of the launch phase, only the \mathbf{x}_t -component of $\frac{\mathbf{R}}{\mathbf{C}}$ is needed. By determining this component and also the component of the gravitational force, we find that the equation for the rocket's translation within the tube is

$$\ddot{\mathbf{x}}_{t} = -g \sin \delta_{G} + \mathbf{x}_{t} \omega_{T}^{2} \cos^{2} \delta_{G} + \mathbf{F}_{T}/m \qquad (2-3)$$

where g is the acceleration of gravity, δ_G is the elevation angle of the tube, F_T is the magnitude of the thrust force (friction is neglected) and m is the mass of the rocket.

The rocket also spins within the tube. We let p denote the spin, or roll, rate of the rocket relative to the tube, T_x denote the x-component (also the x-component, where x is the longitudinal axis of the rocket) of the torque on the rocket and I_x denotes the rocket's moment of inertia about the x_t -axis. The equation for rotational motion of the rocket relative to the tube is then simply

$$\dot{\mathbf{p}} = \mathbf{T}_{\mathbf{x}}/\mathbf{I}_{\mathbf{x}} . \tag{2-4}$$

The roll angle of the rocket relative to the tube may be found from the kinematic equation

$$\Delta \phi = \mathbf{p} . \tag{2-5}$$

Tipoff Equations of Motion

For the purposes of this study it is assumed that, when the rocket has traveled a specified distance down the tube, the transverse rotation of the rocket is no longer constrained by the tube and any internal guidance mechanism, such as a carriage. During the interval of time beginning when transverse rotation of the rocket is not constrained and ending when the aft end of the rocket exits the tube, "tipoff" occurs. In formulating the equations of motion for this part of the launch phase, it is assumed that the rocket may rotate transversely about a point a on the circumference of the rocket, which point a is located at the end of the tube (see Fig. 2-2).

We let $\Delta\psi$ and $\Delta\theta$ denote Euler angles which along with $\Delta\phi$ define the relative orientation of the rocket-fixed Cxyz system with respect to the tube-fixed Ax_ty_tz_t system, p, q and r denote the rocket-fixed components of the relative angular velocity, $\omega_{r/t}$, of the rocket with respect to the tube-

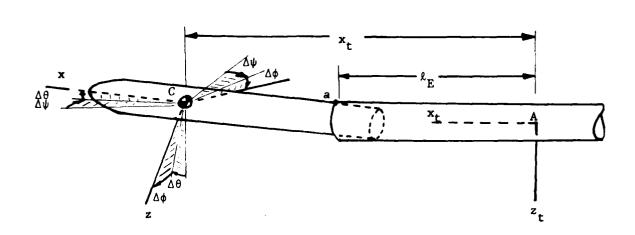


Figure 2-2. Geometry During Tipoff.

fixed system and \underline{I}_{r} denote the rocket's inertia matrix. Furthermore, we define d as the diameter of the rocket at the point a and assume that d is constant. We also let ℓ_{E} denote the distance from point A to the fore end of the tube. Finally, we define the following transformation matrices (assuming $\Delta\theta$ and $\Delta\psi$, but not $\Delta\phi$, are small angles):

$$\frac{A}{=r/t} = \begin{bmatrix} 1 & \Delta\psi & -\Delta\theta \\ -\Delta\psi \cos \Delta\phi + \Delta\theta \sin \Delta\phi & \cos \Delta\phi & \sin \Delta\phi \\ \Delta\psi \sin \Delta\phi + \Delta\theta \cos \Delta\phi & -\sin\Delta\phi & \cos \Delta\phi \end{bmatrix}$$
(2-6)

$$\underline{\underline{C}} = \begin{bmatrix} 1 & \Delta\theta & \sin \Delta\phi & \Delta\phi & \cos \Delta\phi \\ 0 & \cos \Delta\phi & -\sin \Delta\phi \\ 0 & \sin \Delta\phi & \cos \Delta\phi \end{bmatrix}$$
 (2-7)

Here $A_{r/t}$ is the matrix which may be used to transform the x_t -, y_t - and z_t -components of a vector quantity into x-, y-, and z-components and \underline{C} is the matrix such that

$$\begin{bmatrix} \Delta \dot{\phi} \\ \dot{\Delta \theta} \\ \dot{\Delta \psi} \end{bmatrix} = \underline{\underline{C}} \begin{bmatrix} \mathbf{p} \\ \mathbf{q} \\ \mathbf{r} \end{bmatrix}$$
 (2-8)

The methods of Ref. 2 may then be used to obtain the equation of relative rotational motion of the rocket. This equation may be expressed in the matrix form,

$$\frac{\hat{\omega}}{r} r/t = \underline{L}^{-1} \left\{ \underline{I}_{r} \frac{\tilde{\omega}}{r} r/t \triangleq r/t \frac{\Delta}{r} r + \frac{\tilde{\omega}}{r} r \underline{I}_{r} \frac{\omega}{r} r \right\}$$

$$- \underline{m} \underbrace{\tilde{\mathcal{L}}_{a}}_{a} \underline{A}_{r}/t \triangleq 23 \left[\underline{I}_{a} + \frac{\tilde{\omega}_{r}}{r} + \frac{\tilde{\omega}_{r}}{t} \underline{I}_{a} + 2 \underbrace{\tilde{\omega}_{r}}_{t} + \frac{\tilde{\omega}_{r}}{r} \underline{I}_{r} + \frac{\tilde{\omega}_{r}}{r} \underline{I}_{$$

where the letter r beneath a matrix indicates the x-, y- and z-components of the corresponding vector quantity are used to form the matrix and the following additional definitions have been introduced:

$$\frac{\omega}{r}r/t = [\dot{p} \dot{q} \dot{r}]^{T}$$

$$\underline{\underline{I}}_{\mathbf{r}} = \begin{bmatrix} \mathbf{I}_{\mathbf{x}} & 0 & 0 \\ 0 & \mathbf{I}_{\mathbf{T}} & 0 \\ 0 & 0 & \mathbf{I}_{\mathbf{T}} \end{bmatrix}$$

$$\underline{L} = \underline{I}_{r} - m \frac{\tilde{\ell}}{\tilde{r}} \underline{A}_{r/t} = 23 \frac{A}{\tilde{r}} t/r \frac{\tilde{\ell}}{\tilde{r}} \underline{A}_{r/t}$$

$$\frac{\ell}{t}a = [(x_t - \ell_E) \quad 0 \quad 0]^T$$

[†]A superscript T denotes the matrix transpose.

$$\underline{\underline{A}}_{t/T} = \begin{bmatrix} \cos \delta_G & 0 & -\sin \delta_G \\ 0 & 1 & 0 \\ \sin \delta_G & 0 & \cos \delta_G \end{bmatrix}$$

$$\frac{A}{T/t} = \frac{A}{T}$$

$$\frac{\mathbf{F}}{\mathbf{r}^{\mathrm{T}}} = \begin{bmatrix} \mathbf{F}_{\mathrm{T}} & \mathbf{0} & \mathbf{0} \end{bmatrix}^{\mathrm{T}}$$

$$\frac{\mathbf{T}}{\mathbf{r}}\mathbf{s} = \begin{bmatrix} \mathbf{T}_{\mathbf{x}} & \mathbf{0} & \mathbf{0} \end{bmatrix}^{\mathbf{T}}$$

$$\underline{\underline{\omega}}_{T} = \begin{bmatrix} 0 & 0 & \omega_{T} \end{bmatrix}^{T}$$

$$\frac{\omega}{\overline{t}}T = \frac{A}{\underline{t}}/T \frac{\omega}{\overline{T}}T$$

$$\frac{\omega}{r}r = \frac{\omega}{r}r/t + \frac{\Delta}{r}r/t \frac{\omega}{t}T$$

$$\underline{R}_{A} = [x_{T_{A}} \quad y_{T_{A}} \quad 0]^{T}$$

$$\frac{d}{t} = [d/2 \quad 0 \quad 0]^{T}$$

$$\frac{\mathring{\ell}}{r}a = [\mathring{x}_t \quad 0 \quad 0]^T$$

$$\mathbf{E}_{23} = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\underline{\mathbf{E}}_{1} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

$$\begin{aligned} & \underbrace{F}_{\mathbf{r}}^{\mathbf{ex}} = \begin{bmatrix} & -\text{mg sin } \delta_{\mathbf{G}} & 0 & \text{mg cos } \delta_{\mathbf{G}} \end{bmatrix}^{\mathbf{T}} + \underline{A}_{\mathbf{t/r}} & \underbrace{F}_{\mathbf{T}} \\ & \underbrace{F}_{\mathbf{T}} = \begin{bmatrix} F_{\mathbf{T}} & 0 & 0 \end{bmatrix}^{\mathbf{T}} \\ & \underbrace{T}_{\mathbf{r}} = \begin{bmatrix} T_{\mathbf{x}} & 0 & 0 \end{bmatrix}^{\mathbf{T}} \end{aligned}$$

Also, in Eq. (2-9) and throughout this report, a tilde $(\tilde{\ })$ above a 3 x 1 matrix denotes a particular 3 x 3 skew-symmetric matrix formed from the elements of the 3 x 1 matrix. For example,

$$\frac{\tilde{\omega}}{\tilde{r}r/t} = \begin{bmatrix} 0 & -r & q \\ r & 0 & -p \\ -q & p & 0 \end{bmatrix}.$$

The equation which governs the translational motion of the rocket's center of mass may also be obtained by using the methods of Ref. 2. It is

$$\begin{bmatrix} \ddot{x}_{t} \\ 0 \\ 0 \end{bmatrix} = \underbrace{\underline{E}}_{1} \ 2\underline{\underline{A}}_{t/T} \ \tilde{\underline{T}}_{T} \ \tilde{\underline{t}}_{C/A} + \underline{\underline{A}}_{t/T} \ \tilde{\underline{T}}_{T} \tilde{\underline{T}} \\ + \frac{1}{m} \ \underline{\underline{F}}_{t}^{ex} \end{bmatrix} , \qquad (2-10)$$

where

$$\frac{\hat{r}}{t}C/A = \frac{A}{t}/r \frac{\omega}{r}r/t \frac{\hat{l}}{r}a + \frac{A}{t}/r \frac{\hat{l}}{r}a.$$

Equations (2-9) and (2-10) include the effects of the constraint forces which cause the point a to move with the turret. They, along with Eq. (2-8), comprise the equations of motion for the tipoff part of the launch phase.

2.4 Initial Conditions for the Flight Phase

The main purpose of the launch phase equations is to provide realistic initial conditions for the flight phase; i.e., that phase beginning when the rocket is free of the launcher's constraints. At the end of the launch phase simulation in which the requisite differential equations are integrated numerically, we have the values of $x_t = k_E + the$ distance from the aft end of the rocket to the center of mass, $\Delta \phi$, $\Delta \theta$, $\Delta \psi$, p, q, r and $\lambda_G = \omega_T(t_{exit} - t_o)$, where t_{exit} is the time the launch phase ends and t_o is the time the rocket starts to move.

The initial conditions we need for the flight phase is the following: the x_G^- , y_G^- and z_G^- -coordinates of the rocket's center of mass C; the Euler angles ψ , θ and ϕ which are used to define the orientation of the rocket-fixed coordinate system Cxyz with respect to an earth-fixed system OXYZ; the inertial components of the velocity of C, U, V and W; P, Q and R, the x-, y-, and z-components, respectively, of the angular velocity of the Cxyz system relative to the OXYZ system. We shall use a small e as a subscript here to denote the value at the instant of exit. Also, the vector \underline{r}_G , from point G to point A is introduced at this point. Using previous results and resorting to Figures 2-3 and 2-4, we obtain first

$$(P \ Q \ R)_{e}^{T} = [(p \ q \ r)^{T} + \underset{=r/T}{A}_{-T}]_{e},$$
 (2-11)

then

$$(\mathbf{U} \quad \mathbf{V} \quad \mathbf{W})_{\mathbf{e}}^{\mathbf{T}} = \underline{\mathbf{A}}_{\mathbf{r}/\mathbf{T}} \frac{\tilde{\omega}}{\mathbf{T}} \mathbf{T} \frac{\mathbf{R}}{\mathbf{T}} + \underline{\mathbf{A}}_{\mathbf{r}/\mathbf{t}} \frac{\mathbf{r}}{\mathbf{t}} \mathbf{C}/\mathbf{A}$$
 (2-12)

and

$$(x_G y_G z_G)^T = A_{t/T} (R_A - r_G) + r_{t/T} (R_A - r_G) + r_$$

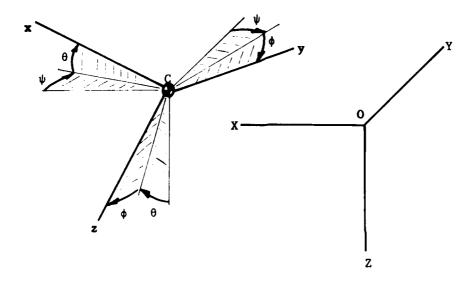


Figure 2-3. Orientation of the Rocket-Fixed System.

To determine the initial values of the Euler angles ψ , θ and ϕ , we construct the direction cosine matrix for the G \mathbf{x}_G \mathbf{y}_G \mathbf{z}_G system (the same matrix as that for the $\mathbf{A}\mathbf{x}_t\mathbf{y}_t\mathbf{z}_t$ system) using first the angles λ_G , δ_G , $\Delta\psi$, $\Delta\theta$, $\Delta\phi$. This matrix we call $\mathbf{L}_{b/I}$, where b/I denotes that the rotation is from the inertial OXYZ system to the body-fixed system Cxyz. This matrix can also be constructed by using the Euler angles ψ , θ and ϕ . By comparing terms in the two different expressions for $\mathbf{L}_{b/I}$, we therefore find that

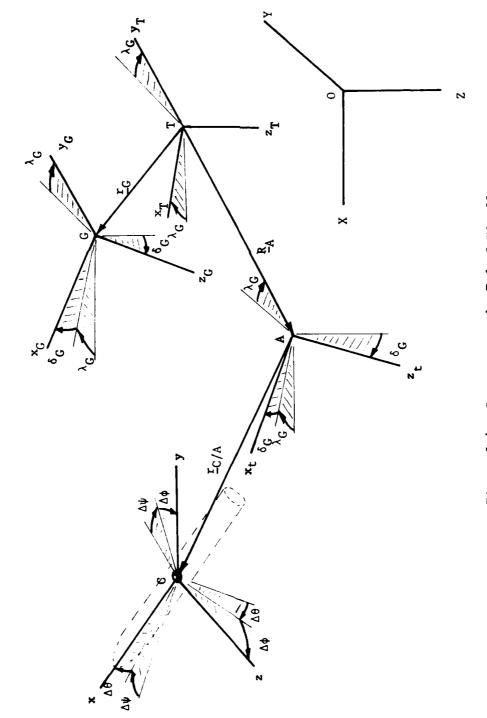


Figure 2-4. Geometry at the End of Tipoff.

$$\tan \psi_{e} = \left[\frac{\cos \delta_{G} \sin \lambda_{G} + \Delta \psi \cos \lambda_{G} - \Delta \theta \sin \delta_{G} \sin \lambda_{G}}{\cos \delta_{G} \cos \lambda_{G} - \Delta \psi \sin \lambda_{G} - \Delta \theta \sin \delta_{G} \cos \lambda_{G}} \right]_{e}$$
(2-14a)

$$\tan \phi_{e} = \left[\frac{\sin \delta_{G} \left[\Delta \psi \cos \Delta \phi - \Delta \theta \sin \Delta \phi \right] + \cos \delta_{G} \sin \Delta \phi}{-\sin \delta_{G} \left[\Delta \psi \sin \Delta \phi + \Delta \theta \cos \Delta \phi \right] + \cos \delta_{G} \cos \Delta \phi} \right]_{e}$$
(2-14b)

$$\sin \theta_{e} = [\sin \delta_{G} + \Delta \theta \sin \delta_{G}]_{e}$$
 (2-14c)

We have, at this point, developed the basis for simulating the launch phase and have also obtained equations from which we can determine initial conditions for the flight phase, given the final conditions for the launch phase. In the next section, we develope the flight phase model.

SECTION 3. FLIGHT DYNAMICS

3.1 Introductory Comments

In this section, we develop the mathematical model for the rocket. This model is essentially the same as that developed in Ref. 2 and used there as the basis for the simulation of the free-flight phase of a "free," or uncontrolled, rocket. The differences in the two models are that (1) additional forces and moments due to the deflection of the sustainer motor's thrust vector are included here and (2) the time variations of the mass of the rocket and of its centroidal moments of inertia are assumed, for the purposes of this study to be prescribed a priori as explicit functions of time.

3.2 Physical Model for the Rocket

The rocket is modeled physically as a variable mass body composed of a rigid portion and a fluid portion (see Fig. 3-1). The rigid portion consists of the unexpendable parts of the rocket, plus the part of the solid propellant not yet expended at time t. The fluid portion consists of that part of the solid propellant which has been burned (or is burning) and is flowing as a fluid within the rocket, having not yet passed through the rocket nozzles. For the purposes of modeling the internal flow, the geometry of the rocket is simplified by assuming that the flow is within the core of a cylindrical, solid propellant charge. Since the internal flow model is actually used only in estimating the jet-damping torque, this simple model is considered sufficient.

The rocket, apart from the solid propellant, consists (see Fig. 3-2) first of all a shell, or fuselage, which contains the warhead, the solid

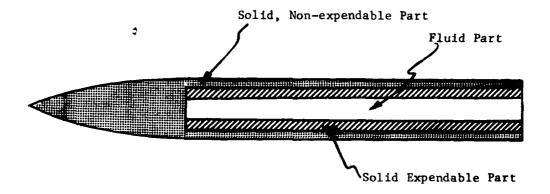


Figure 3-1. Solid and Fluid Portions of the Rocket.

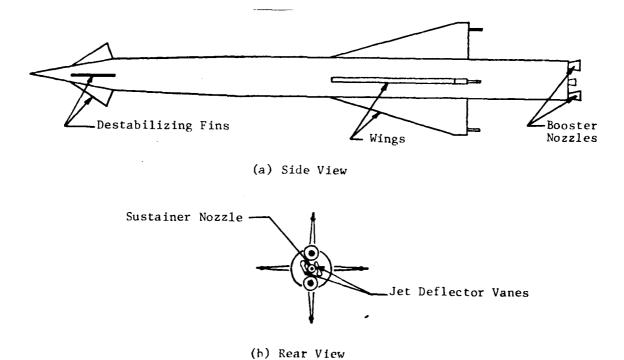


Figure 3-2. Rocket with Wings Unfolded.

propellant, the rocket nozzles, a pitch rate gyro, a roll angle gyro, the actuating mechanism for the thrust deflector vanes, the vanes themselves, the electronic equipment needed to receive and process guidance commands and a device which controls the motion of destabilizing fins. The last six items listed will be discussed more fully in the section on guidance and control (see Section 4). Four wings are attached to the rocket's fuselage in a cruciform configuration. These wings fold out as the rocket exits the launch tube. Also, there are four small fins which are extended through the slots near the nose of the rocket. They are the destabilizing fins mentioned above. They are extended in a pre-programmed manner so that the aerodynamic center of the rocket moves forward as the center of mass moves forward (due to propellant consumption), with the result that a fairly constant static margin is maintained during the rocket's powered flight.

3.3 Equations of Motion

The equations of motion for the rocket may be obtained using the procedure followed in Ref. 1, or, for example, that of Ref. 3.

Translational Motion

The equation which governs the translation of the center of mass of the rocket may be written in the form,

$$m \stackrel{\circ}{V}_{C} = F_{T} + F_{c} + F_{Coriolis} + F_{unsteady} + F_{ex}, \qquad (3-1)$$

where \underline{F}_T is the thrust "force" (see Ref. 4) which is generated by the outflow of the fluid part of the rocket, \underline{F}_c is the control force (also generated by the same mechanism as \underline{F}_T , but segregated here for convenience). $\underline{F}_{Coriolis}$

The word "force" is enclosed in quotation marks here to indicate that it pertains to a term in the equation of motion which is treated as a force, but actually arises due to the fact that mass is being expelled from the rocket and strictly speaking is a reaction force on the solid part of the rocket due

is the "force" required to accelerate the mass of fluid within the rocket transversely, $F_{\rm unsteady}$ is the "force" resulting from the time rate of change of fluid flow properties at a given spatial position and $F_{\rm ex}$ includes all forces on the rocket due to external influences such as the atmosphere and gravity.

In most cases, $F_{-Coriolis}$ and $F_{-unsteady}$ are not significant. Hence, we will neglect these two "forces." Then, by writing

$$V_{C} = V \hat{i} + V \hat{j} + W \hat{k}$$
, (3-2)

where \hat{i} , \hat{j} and \hat{k} are unit vectors fixed to the rolling rocket which has angular velocity,

$$\underline{\Omega} = P \hat{i} + Q \hat{j} + R \hat{k} , \qquad (3-3)$$

and letting $\mathring{\underline{v}}_C$ = $\mathring{\underline{v}}$ $\hat{\underline{i}}$ + $\mathring{\underline{v}}$ $\hat{\underline{j}}$ + $\mathring{\underline{w}}$ $\hat{\underline{k}}$, we may rewrite Eq. (3-1) in the form,

$$\overset{\circ}{\mathbf{V}}_{\mathbf{C}} = - \underline{\Omega} \times \underline{\mathbf{V}} + \frac{1}{m} \left[\underline{\mathbf{F}}_{\mathbf{T}} + \underline{\mathbf{F}}_{\mathbf{c}} + \underline{\mathbf{F}}_{\mathbf{ex}} \right]$$
 (3-4)

If the rocket is imperfect, which is usually the case, then to account for thrust vector misalignment we write

$$\underline{F}_{T} = T \cos \alpha_{y} \cos \alpha_{z} \hat{i} + T \cos \alpha_{y} \sin \alpha_{z} \hat{j} - T \sin \alpha_{y} \hat{k},$$
 (3-5)

where T is the magnitude of the thrust and α_y and α_z are constant angles (as shown in Fig. 3-3) which are measures of the amount and direction of the mechanical thrust misalignment present. It should be pointed out that these angles represent the "equivalent thrust misalignment" resulting from the combined mechanical misalignment of both the booster motor nozzles.

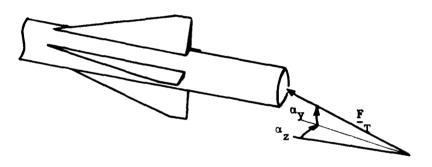


Figure 3-3. Thrust Misalignment Angles.

The control force is discussed more fully in Section 4, but here we note that (see Fig. 3-4).

$$\underline{\mathbf{F}}_{\mathbf{C}} = \pm \mathbf{F}[-\sin \delta \,\hat{\mathbf{j}} + \cos \delta \,\hat{\mathbf{k}}], \tag{3-6}$$

where F is the magnitude of the control force and δ is a constant angle representing the rotation of the control plane with respect to the xz-plane.

The external force which acts on the rocket is the resultant of the aerodynamic force and the force due to gravity, hence,

$$\frac{\mathbf{F}_{-\mathbf{e}\mathbf{x}}}{\mathbf{F}_{-\mathbf{e}\mathbf{x}}} = \frac{\mathbf{F}_{-\mathbf{A}}}{\mathbf{F}_{-\mathbf{g}}} + \frac{\mathbf{F}_{-\mathbf{g}}}{\mathbf{F}_{-\mathbf{g}}} , \qquad (3-7)$$

where

$$\mathbf{F}_{A} = -\mathbf{A} \hat{\mathbf{i}} - \mathbf{Y} \hat{\mathbf{j}} - \mathbf{N} \hat{\mathbf{k}}$$
 (3-8)

and

$$\mathbf{F}_{\mathbf{g}} = \operatorname{mg}[-\sin \theta \ \hat{\mathbf{i}} + \cos \theta \sin \phi \ \hat{\mathbf{j}} + \cos \theta \cos \phi \ \hat{\mathbf{k}}] \ . \tag{3-9}$$

In Eq. (3-8), A is the axial aerodynamic force component, Y is the y-component of the aerodynamic force and N is the normal aerodynamic force component (see Fig. 3-5). In Eq. (3-9), θ and ϕ are two of the Euler angles which are used to define the orientation of the rocket-fixed coordinate system Cxyz (see Fig. 2-3).

For the purposes of this study, the aerodynamic forces are assumed to be expressible as

$$A = 1/2\rho \quad S \quad V_R^2 \quad C_A$$
 (3-9a)

$$Y = 1/2\rho \ SV_R^2 \ C_V$$
 (3-9b)

and

$$N = 1/2\rho \ SV_R^2 \ C_N$$
 (3-9c)

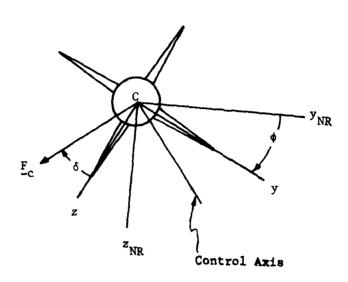


Figure 3-4. Control Force Orientation.

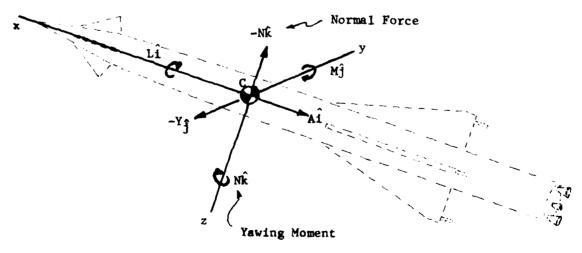


Figure 3-5. Aerodynamic Forces and Moments.

where ρ is the atmospheric density, S is the reference area upon which the aerodynamic coefficients C_A , C_y and C_N are based and V_R is the absolute value of the relative wind that the rocket encounters. Herein

$$V_{R} = \sqrt{(V_{W} - V)^{2} + (V_{W} - V)^{2} + (W_{W} - W)^{2}}$$
(3-10)

where $\mathbf{U}_{\mathbf{w}}$, $\mathbf{V}_{\mathbf{w}}$ and $\mathbf{W}_{\mathbf{w}}$ are the x-, y- and z-components of the velocity of the wind.

The usual assumption that C_A is a function of angle of incidence and Mach number, M, is made and it is further assumed that the incidence angle is small. Then, the following forms for C_A , C_V and C_N are adopted:

$$C_{A} = C_{A_{O}}(M) \tag{3-11a}$$

$$C_{y} = -C_{N_{\alpha}}(M) \beta \qquad (3-11b)$$

$$C_{N} = C_{N}(M) \alpha , \qquad (3-11c)$$

where $C_{A_0}^{(M)}$ and $C_{N_0}^{(M)}$ are tabulated functions and $\alpha = \tan^{-1}[(W-W_W)/(U-U_W)]$ and $\beta = \sin^{-1}[(V-V_W)/V_R]$ are the aerodynamic angles of attack and sideslip, respectively.

In the simulation program, the differential equations for V and W are not integrated. Instead, the variables $\alpha_{\mathbf{x}} = \tan^{-1}(W/U)$ and $\beta_{\mathbf{x}} = \sin^{-1}(V/V_C)$ are used in place of V and W for computational purposes. The variables $\alpha_{\mathbf{x}}$ and $\beta_{\mathbf{x}}$ are the aerodynamic angles of attack and sideslip, respectively if there is no wind. The derivatives V and W are computed using Eq. (3-4) and $\alpha_{\mathbf{x}}$ and $\beta_{\mathbf{x}}$ are obtained from

$$\dot{\alpha}_{\mathbf{x}} = (U\dot{W} - W\dot{U})/(U^2 + W^2)$$
 (3-12a)

The incidence angle referred to here is that engle between the relative

and

$$\dot{\beta}_{\mathbf{x}} = [\dot{v}(v^2 + w^2) - v(v\dot{v} + w\dot{w})]/[v_C^2 \sqrt{v^2 + w^2}]$$
 (3-12b)

The kinematic equation for translation is obtained by noting that the velocity of the center of mass of the rocket may be written either as

$$V_{C} = \dot{X} \hat{I} + \dot{Y} \hat{J} + \dot{Z} \hat{K}$$
, (3-13)

where $\hat{\mathbf{I}}$, $\hat{\mathbf{J}}$ and $\hat{\mathbf{K}}$ are unit vectors associated with the earth-fixed OXYZ system, or as

$$V_C = U \hat{i} + V \hat{j} + W \hat{k}$$
 (3-14)

Since the components of \underline{V}_C in the two systems are related by the transformation matrix (see Fig. 2-3) used previously in Section 2,

$$L_{b/I} = \begin{bmatrix} c\theta c\psi & c\theta s\psi & -s\theta \\ -c\phi s\psi & c\phi c\psi & s\phi c\theta \\ + s\phi s\theta c\psi & + s\phi s\theta s\psi \\ s\phi s\psi & -s\phi c\psi & c\phi c\theta \\ + c\phi s\theta c\psi & + c\phi s\theta s\psi \end{bmatrix}$$

$$(3-15)$$

The required kinematic equation is

$$\begin{bmatrix} \dot{X} \\ \dot{Y} \\ \dot{Z} \end{bmatrix} = L_{1/b} \begin{bmatrix} U \\ V \\ W \end{bmatrix}, \qquad (3-16)$$

where $L_{I/b} = L_{b/I}^{T}$.

Rotational Motion

The equation governing the rotational motion of the rocket about its center of mass C is

$$\underline{\underline{I}} \stackrel{\dot{\Omega}}{\underline{\cap}} + \underline{\underline{\cap}} \times \underline{\underline{I}} \cdot \underline{\underline{\cap}} = \underline{\underline{T}} + \underline{\underline{T}} +$$

where $\underline{\underline{I}}$ is the centroidal inertia dyadic of the rocket, $\underline{\underline{T}}_{T}$ is the "torque" about C due to the thrust, $\underline{\underline{T}}_{c}$ is the control "torque" about C, $\underline{\underline{T}}_{unsteady}$ is the "torque" about C due to the unsteadiness of the flow, $\underline{\underline{T}}_{Coriolis}$ is the "torque" about which is due to the time rate of change of the direction of the motion of the fluid which is flowing inside the rocket caused by rotation of the rocket and $\underline{\underline{T}}_{ex}$ is the torque about C due to aerodynamic reactions.

The inertia dyadic $\underline{\underline{I}}$ is assumed to be general in form to account for mass imbalance which may be present due to manufacturing imperfections. The matrix counterpart of $\underline{\underline{I}}$ expressed in terms of rocket-fixed elements is

$$\frac{I}{r} = \begin{bmatrix}
I_{xx} & -I_{xy} & -I_{xz} \\
-I_{xy} & I_{yy} & -I_{yz} \\
-I_{xz} & -I_{yz} & I_{zz}
\end{bmatrix}.$$
(3-18)

In the ideal case, $I_{xy} = I_{xz} = I_{yz} = 0$ and $I_{yy} = I_{zz}$.

The torque due to thrust is expressed explicitly as

$$\underline{\mathbf{T}}_{\mathrm{T}} = (\underline{\mathbf{L}}_{\mathrm{T}} - \underline{\mathbf{u}}) \times \underline{\mathbf{F}}_{\mathrm{T}} , \qquad (3-19)$$

The word "torque" is enclosed in quotation marks here to indicate that it pertains to a term in the equation of motion which is treated as an external torque, but actually arises from the fact that mass is being expelled from the rocket and strictly speaking is a reaction torque on the solid part of the rocket due to the internal flow or expelled mass. The quotation marks will be dropped in later references to the same term.

where ℓ_T is a vector from an arbitrary point in the non-expendable part of the rocket to a point on the line of action of the resultant thrust vector. Also, in Eq. (3-18) u is a vector from a to C (see Fig. 3-6).

The control torque, like the control force, will be discussed more fully in Section 4. However, we note here that it has the form,

$$\frac{\mathbf{T}}{\mathbf{r}_{\mathbf{C}}} = (\mathbf{r}_{\mathbf{T}} - \mathbf{u}) \times \mathbf{F}_{\mathbf{C}} , \qquad (3-20)$$

where $\underline{\boldsymbol{r}}_T$ is a vector from point a to the line of action of the control force.

For the purposes of this study the torque due to the unsteadiness of the flow is assumed to be negligible compared to other torques.

The Coriolis torque is the so-called "jet-damping" torque, \underline{T}_{JD} , and is retained. By assuming a cylindrical solid propellant charge and constant mass flow rate per unit length of the change, an approximate expression for $\underline{T}_{Coriolis}$ may be obtained.² The expression used in this simulation study is

$$\frac{T}{-JD} = \frac{T}{Coriolis} = -2 C_{JD}[Q \hat{j} + R \hat{k}]$$
 (3-21)

Here, the jet damping coefficient, \mathbf{C}_{JD} , is given by

$$C_{JD} = -\dot{m}[(u_1 - x_2^{\dagger}/3) \ell_p + (x_1^{\dagger})^2/3],$$
 (3-22)

where \dot{m} is the time rate of change of the rocket's mass, $u_1 = \dot{u} \cdot \hat{i}$, l_p is the length of the propellant charge and x_1' and x_2' are the coordinates of the aft and fore ends, respectively, of the propellant charge as measured from point a as shown in Fig. 3-7.

Figure 3-6. Notation used in Equations of Motion.

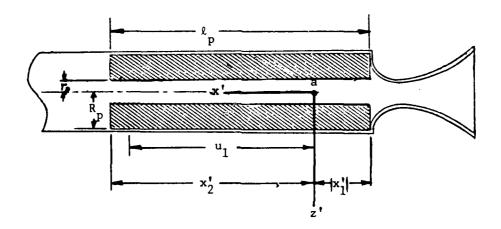


Figure 3-7. Geometry of Solid Propellant Charge.

The external torque about the rocket's center of mass is due to the resultant aerodynamic force. This aerodynamic torque may be expressed in the conventional form,

$$T_{ex} = T_{A} = L \hat{i} + M \hat{j} + N \hat{k}$$
 (3-23)

where L, M and N † are the rolling, pitching and yawing components, respectively, of \underline{T}_A . The components L, M and N may be expressed in the forms,

$$L = 1/2 \rho S V_R^2 d C_{\ell}$$
 (3-24a)

$$M = 1/2 \rho S V_R^2 d C_m$$
 (324b)

and

$$N = 1/2 \rho S V_R^2 d C_n,$$
 (3-24c)

where C_{ℓ} , C_m and C_n are the usual aerodynamic coefficients and d is the reference length upon which these coefficients are based.

In general,

$$C_{\varrho} = C_{\varrho}(M,\alpha,\beta,P)$$
 (3-25a)

$$C_{m} = C_{m}(M,\alpha,\dot{\alpha},Q)$$
 (3-25b)

and

$$C_n = C_n(M, \dot{\beta}, \dot{\beta}, R),$$
 (3-25c)

where M is used here to denote the flight Mach number. For small α_A and β_A , which we assume is the case, C_{ℓ} can be adequately represented by the expression,

$$C_{\ell} \simeq [d/(2V_R)]C_{\ell} (M) P,$$
 (3-26a)

Those that the symbols M and N are used elsewhere for the flight Mach number and the normal component of the aerodynamic force, respectively. This notation is also conventional and it should be clear from the context in which the symbols appear which meaning is to be attached to each of them.

where C_{ℓ} is a non-dimensional stability derivative defined as

$$C_{\ell_p} \equiv (2V_R/d)(\partial C_{\ell}/\partial P)_{p=0}$$
.

Also, for small α , β , P and Q,

$$C_{m} \approx C_{m_{\alpha}} \alpha + [d/(2V_{R})] C_{m_{q}} Q$$
, (3-26b)

where

$$C_{\mathbf{m}_{\alpha}} = (\partial C_{\mathbf{m}}/\partial \alpha) \Big|_{\alpha=0}$$

and

$$C_{\mathbf{m}_{\mathbf{q}}} = (\partial C_{\mathbf{m}}/\partial Q) (2V_{\mathbf{R}}/\mathbf{d}) \Big|_{Q=0}$$

Since the rocket is geometrically symmetric, $C_{n_{\beta}} = -C_{m_{\alpha}}$ and $C_{n_{r}} = C_{m_{q}}$, so that we also write

$$C_n \approx -C_{m_\alpha} \beta + [d/(2V_R)]C_{m_q} R$$
 (3-25c)

In this report, the quantities C_{ℓ_p} , C_{m_q} and C_{m_q} are assumed to be given functions of the flight Mach number in the form of tabulated values. The stability derivative C_{m_q} is a function of the static margin; i.e., $(\mathbf{x}_{cp} - \mathbf{x}_{cg})/d$ where \mathbf{x}_{cp} and \mathbf{x}_{cg} are the distances from the rocket's nose to its aerodynamic center and its center of mass, respectively. This quantity is a function of M because the distance \mathbf{x}_{cp} varies directly with Mach number and \mathbf{x}_{cg} varies indirectly with Mach number, since as the rocket's fuel is consumed and its center of mass moves forward, the Mach number increases until burnout of the booster motor. The destabilizing fins shown in Fig. 3-2 are extended as the fuel is consumed in such a way that $(\mathbf{x}_{cp} - \mathbf{x}_{cg})$ remains fairly constant during powered flight; hence, C_{m_q} also remains fairly constant. The

destabilizing fins do not make the rocket unstable, but they only make it less statically stable than it would otherwise be at Mach numbers near and above unity.

The basic mathematical model of the rocket has been presented. We turn, in the next section, to the task of formulating guidance and control algorithm for the system composed of the rocket and the sensing and guidance command generating equipment on the launcher.

SECTION 4. GUIDANCE AND CONTROL

4.1 General Comments

The guidance and control of the rocket prior to radar acquisition are considered in this section. First, the problem of guiding the rocket toward a moving target is addressed. Then, the control algorithm used in this investigation is described.

4.2 Guidance

It is assumed that guidance commands are formulated in the launch vehicle by means of a special purpose guidance computer. The input to the guidance computer is angular data acquired by the launcher-fixed IR sensor. This information is available, however, only if the aft end of the rocket (which contains flares) is within the field of yiew (FOV) of the IR sensor. The sensor is assumed to have two FOV's - one for acquisition of the rocket and a more narrow one for use after acquisition by the sensor, but prior to radar acquisition (see Fig. 4-1). The guidance computer is assumed to contain a pre-programmed range versus time relation, so that the spherical coordinates, (R $_{G},~\epsilon_{z},~\epsilon_{v})$ (see Fig. 4-1) where R $_{G}$ is the range of the rocket and $\boldsymbol{\epsilon}_z$ and $\boldsymbol{\epsilon}_v$ are the "aximuth" and "elevation" angles, respectively, of the rocket with respect to ${^G}x_G^{y}_G^{z}_G$ coordinate frame. Furthermore, for the purposes of this study, it is assumed that values of \dot{R}_G , $\dot{\epsilon}_z$ and $\dot{\epsilon}_v$ are available. These may be estimated by using the range versus time relationship, the angular measurements and the gimbal rates of the radar (which is assumed to perfectly track the target). For use in the current control algorithm, the linear deviations of the rocket from the line of sight (LOS) from the launcher radar to the target (This LOS is the extended x_{C} -axis)

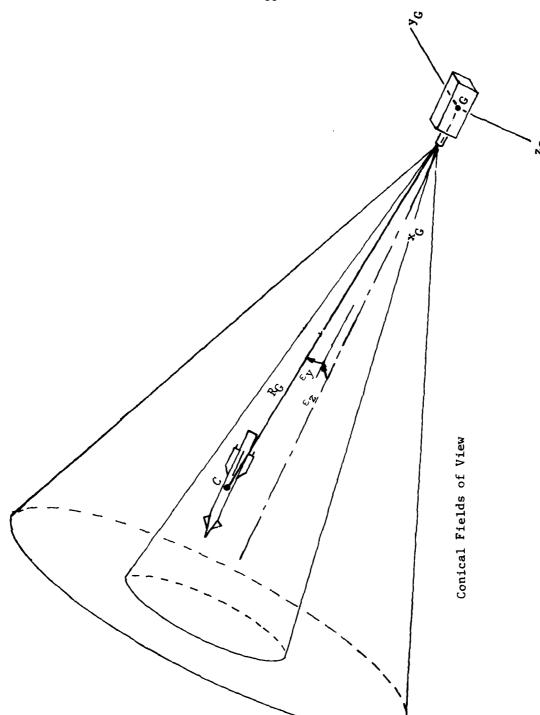


Figure 4-1. IR Guidance Geometry.

are used. These deviations are \mathbf{y}_G and \mathbf{z}_G which may be computed by using the equations,

$$y_G = R_G \cos \varepsilon_y \sin \varepsilon_z$$
 (4-1a)

and

$$z_G = -R_G \sin \epsilon_y$$
 (4-1b)

The time rates of change of \mathbf{y}_{G} and \mathbf{z}_{G} are also used in the control algorithm. These may be obtained from

$$\dot{y}_{G} = \dot{R}_{G} \cos \varepsilon_{y} \sin \varepsilon_{z} - R_{G} \dot{\varepsilon}_{y} \sin \varepsilon_{y} \sin z$$

$$+ R_{G} \dot{\varepsilon}_{z} \cos \varepsilon_{y} \cos \varepsilon_{z} \qquad (4-2a)$$

and

$$\dot{z}_G = - \left[\dot{R}_G \sin \varepsilon_y + R_G \varepsilon_y \cos \varepsilon_y \right] \tag{4-2b}$$

In an actual system, these rates could be estimated by using

$$\dot{y}_G \simeq -R_G \dot{\lambda}_G \cos \delta_G + \dot{R}_G \varepsilon_z$$
 (4-3a)

and

$$\dot{z}_{G} \simeq -R_{G} \dot{\delta}_{G} - \dot{R}_{G} \varepsilon_{V} \tag{4-3b}$$

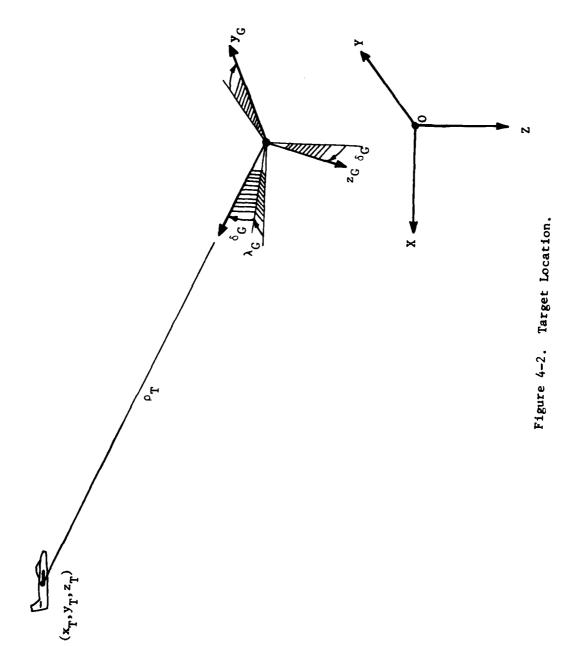
for small ϵ_y , ϵ_z , $\dot{\epsilon}_y$, $\dot{\epsilon}_z$ and pre-radar acquisition values of R_G.

In this report, we consider only constant-speed targets (see Fig. 4-2). For such targets, the angles \mathbf{x}_G and δ_G are given by

$$\lambda_{G} = \tan^{-1}(y_{T}/x_{T}) \tag{4-4a}$$

and

$$\delta_{G} = \sin^{-1}(-z_{T}/\rho_{T}) \tag{4-4b}$$



respectively, where

$$x_{T} = x_{Y} + \dot{x}_{T}(t-t_{o}),$$
 (4-5a)

$$y_T = y_T + \dot{y}_T(t-t_0),$$
 (4-5b)

$$x_{T} = x_{Y_{o}} + \dot{x}_{T}(t-t_{o}), \qquad (4-5a)$$

$$y_{T} = y_{T_{o}} + \dot{y}_{T}(t-t_{o}), \qquad (4-5b)$$

$$z_{T} = z_{T_{o}} + \dot{z}_{T}(t-t_{o}), \qquad (4-5c)$$

$$\rho_{\rm T} = \sqrt{x_{\rm T}^2 + y_{\rm T}^2 + z_{\rm T}^2} \tag{4-5d}$$

and $\boldsymbol{x}_{T}^{},~\boldsymbol{y}_{T}^{}$ and $\boldsymbol{z}_{T}^{}$ are the coordinates of the target in a non-rotating coordinate system with origin at G. It follows from Eqs. (4-4) that

$$\dot{\lambda}_{C} = (\dot{y}_{T}/x_{T} - y_{T} \dot{x}_{T}/x_{T}^{2})\cos^{2}\lambda_{C}$$
 (4-6a)

and

$$\dot{\delta}_{G} = (-\dot{z}_{T}/\rho_{T} + z_{T} \dot{\rho}_{T}^{2}/\rho_{T}^{2})/\cos \delta_{G}$$
 (4-6b)

where $\dot{\rho}_{T} = (x_{T} \dot{x}_{T} + y_{T} \dot{y}_{T} + z_{T} \dot{z}_{T})/\rho_{T}$.

4.3 Control

Control of the rocket is physically accomplished, as mentioned previously, by causing the deflector vanes to dwell in either a positive or negative position, thereby producing a torque about the control axis (see Fig. 3-4) of the rocket. This torque produces an angular acceleration about either the positive or negative control axis. The integrated effects of the torque are, first of all, an angular rate and, secondly, an attitude change. The latter results in a change of the rocket's angle of incidence and an accompanying change in the aerodynamic force and torque on the rocket. Finally, the altered aerodynamic force produces a change in the rocket's flight path. The duration of the dwell and the roll orientation of the rocket while it is taking place determine the resultant change in its flight path.

The purpose of the control system is two-fold. The first part of its purpose is to "stabilize" the rocket's angular velocity in such a way that angular rates due to disturbances, and not guidance commands, are nulled out rapidly. Secondly, it must produce the attitude changes dictated by the guidance commands.

Since the control force is either "on" or "off", the control system is of the bang-bang type. Thus, in formulating a control algorithm the questions of when to turn the control force on (and in what direction) and how long to leave it on (the dwell time) must be answered.

Control Algorithm

We let $|\Delta t_y|$ and $|\Delta t_z|$ denote the dwell times of the deflector vanes for control of the rocket's motion in the $x_G z_G^-$ and $x_G y_G^-$ -planes, respectively. The signs Δt_y and Δt_z determine whether $F_c = \pm F_c$, as will be explained in what follows. We also let δ_y and δ_z denote the angles through which the rocket rolls during a "longitudinal" ($x_G z_G^-$ -plane), or "lateral" ($x_G y_G^-$ -plane), control period. To be more specific, we assume that positive control torques are desired. Then, to control longitudinal motion, the control force is given by (see Fig. 4-3)

$$F_c = F_{c_{max}}$$
, if $2n\pi - \delta_y/2 < \phi + \delta < 2n\pi + \delta_y/2$, (4-7a)

and by

$$F_c = -F_{c_{max}}$$
, if $(2n+1)\pi - \delta_y/2 \le \phi + \delta \le (2n+1)\pi + \delta_y/2$. (4-7b)

Here n = 0,1,2,... Similarly, for lateral control,

$$F_c = F_{c_{max}}$$
, if $[(4n+1)/2]\pi - \delta_z/2 \le \phi + \delta \le [(4n+1)/2]\pi + \delta_z/2$, (4-8a)

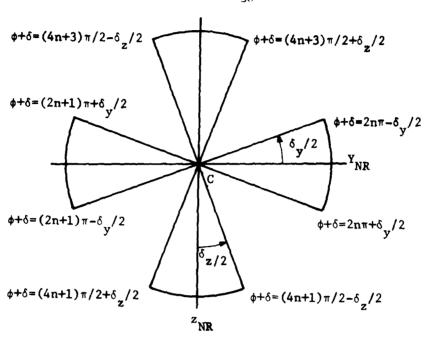


Figure 4-3. Control Regions.

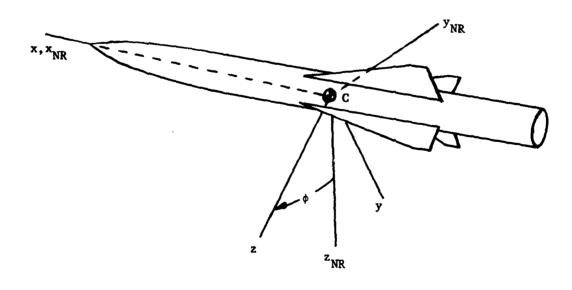


Figure 4-4. Non-rolling Coordinate System.

and

$$F_c = -F_{c_{max}}$$
, if $[(4n+3)/2]\pi - \delta_z/2 \le \phi + \delta \le [(4n+3)/2]\pi + \delta_z/2$.

Ideally, the control forces given by Eqs. (4-7) and (4-8) act as space-fixed forces which produce space-fixed torques and the latter result in changes in the rocket's attitude. Since the rocket is rolling, there is some coupling between its pitch and yaw motions. But, since it is also "slender" (i.e., $I_{xx} \ll I_{yy} \cong I_{zz}$), this coupling is not severe.

The roll angle ϕ must be known if $\boldsymbol{F}_{\boldsymbol{C}}$ is to be generated properly. This angle is assumed to be measured by a roll gyro on board the rocket.

The dwell times Δt_v and Δt_z are determined from the control laws

$$\Delta t_{y} = -K_{1} (Q_{NR} - Q_{NR_{c}})$$
 (4-9a)

and

$$\Delta t_z = - K_1 (R_{NR} - R_{NR_c}), \qquad (4-9b)$$

where K_1 is a constant, Q_{NR} is the angular rate of the rocket about the y_{NR} -axis [which is one of the three axes of the non-rolling $Cx_{NR}y_{NR}z_{NR}$ coordinate system (see Fig. 4-4)], R_{NR} is the angular rate of the rocket about the z_{NR} -axis and Q_{NR} and R_{NR} are commanded angular rates about the y_{NR} - and z_{NR} -axes, respectively. The angular rates Q_{NR} and R_{NR} are computed from

$$Q_{NR} = Q \cos \phi - R \sin \phi \qquad (4-10a)$$

and

$$R_{NR} = Q \sin \phi + R \cos \phi, \qquad (4-10b)$$

respectively, Also, the commanded angular rates are determined using the equations,

$$Q_{NR_{C}} = \frac{k_{2}}{k_{1}} z_{G} + \frac{k_{3}}{k_{1}} \dot{z}_{G}$$
 (4-11a)

and

$$R_{NR_{c}} = -\frac{k_{2}}{k_{1}} y_{G} - \frac{k_{3}}{k_{1}} \dot{y}_{G}$$
 (4-11b)

respectively, where K_3 and K_3 are time varying gains which have the forms,

$$K_2 = K_{20} t_0/t$$
 (4-12a)

and

$$K_{30} = K_{30} t_o/t$$
 $(t \ge t_o)$ (4-12b)

Here, K_{20} and K_{30} are constant and t_0 is the time the control system is enabled (This is a short time after the rocket exits the tube and corresponds to the time the sustainer motor is ignited.)

We note that, for an actual single-axis system, both Q and R <u>may</u> not be measured by rate gyros. In fact, there will probably be only one rate gyro which measures only the angular rate of the rocket about the control axis. However, δ_y and δ_z are herein restricted to small angles, so that the value of Q_{NR} (R_{NR}) used to calculate Δt_y (Δt_z) is approximately the angular rate about the control axis just prior to a control phase.

In an actual system, values of Q_{NR_C} and R_{NR_C} are calculated by the guidance computer and sent to the rocket via a radio link. These values are used by the rocket's on-board systems to generate Δt_y and Δt_z commands. In the present simulation, the procedure used is: (1) Specify a priori $\delta y = \delta_z \quad \text{and an associated } \Delta t_{max} = \delta_y / \Omega, \text{ where } \Omega \text{ is the average roll } y_{max} = \delta_z / \Omega$ and check to see if it is less than Δt_{max} . (3) If $\Delta t_y \leq \Delta t_{max}$ ($\Delta t_z \leq \Delta t_{max}$), then compute $\delta_y = |\Delta t_y| \Omega$ ($\delta_z = |\Delta t_z| \Omega$). (4) If $\Delta t_y > \Delta t_{max}$ ($\Delta t_z > \Delta t_{max}$), then set $\Delta t_y = \text{sign } (\Delta t_y) \Delta t_{max}$

 $(\Delta t_z = sign (\Delta t_z) \Delta t_{max})$ before computing $\delta_y(\delta_z)$. (5) Check to see if the

rocket's roll attitude satisfies Eqs. (4-7) (Eqs. (4-8)). (6) If it does, control is exercised. If not, no action is taken. (7) If the time since the beginning of this control phase is less than τ , the control force magnitude is adjusted so that a ramp up from zero to F_{cmax} is obtained in τ seconds during the beginning of the phase. Also, if the time before the end of this control phase is less than, or equal to, τ , a ramp down in F_{c} is generated during the last τ seconds of the phase. (8) If $|\Delta t_{\mathbf{y}}| < 2\tau$ ($|\Delta t_{\mathbf{z}}| < 2\tau$), no control is exercised.

Control Gain Selection

An approximate linear stability analysis was conducted, assuming that the rocket's roll rate is rapid enough that the average values of the control torques generated during one period of the rolling motion could be considered continuous torques with respect to the non-rolling system $Cx_{NR}y_{NR}z_{NR}$. This analysis provided some indication of the values of K_1 , K_{20} and K_{30} which should be used, but the responses predicted by the linear analysis were not the same as those obtained via nonlinear simulations. This might be expected, since the control problem is actually very nonlinear. Hence, preliminary values of the gains were chosen using physical and hueristic reasoning and "refined" values obtained by changing the gains selectively and generating trajectories with the simulation code.

The reasoning used to pick the preliminary gains was as follows. The commanded transverse angular rates of the rocket are assumed to be limited by Q_{c} . Hence, in one control period the control torque total impulse must be no more than that necessary to produce a rate Q_{c} . For a given maximum control region width, $\delta_{y} = \delta_{z}$, the duration of control application $\delta_{y} = \delta_{z}$

is $\Delta t_{max} = \delta / \Omega$. Hence, if $\delta_{y_{max}}$ is small, so that the effective magnitude of the control force is approximately $F_{c_{max}}$, if I_{T_o} is the value of the lesser of I_{yy} or I_{zz} at the beginning of controlled flight and if ℓ_c is the effective moment arm of F_{c} about C, then the change in magnitude of the angular rate is approximately (longitudinal control)

$$Q_{c_{\max}} \stackrel{\text{2}}{=} \ell_{c} F_{c_{\max}} \Delta t_{\max} / I_{T_{o}}$$
(4-13)

Now, from Eq. (4-9a) (with $Q_{NR} = 0$ and $Q_{NR} = Q_{c_{max}}$)

$$\Delta t_{\text{max}} = K_1 Q_{c_{\text{max}}}$$
 (4-14)

Hence, from Eqs. (4-13) and (4-14), we have

$$K_1 \simeq I_{T_0}/(\ell_c F_{c_{max}})$$
 (4-15)

By replacing z_G and \dot{z}_G with their expected maximum values at the beginning of the controlled flight and Q_{NR} by Q_{c} , in Eq. (4-11a), we obtain

$$Q_{c_{\max}} = K_{20} |z_{G_{\max}}| + K_{30} |z_{G_{\max}}|$$
 (4-16)

By considering the results of the linear stability analysis⁵ and some trial simulation results, it was found that equal numerical values for K_{20} and K_{30} resulted in reasonable response characteristics. Hence, (except for units)

$$K_{20} = K_{30} = Q_{c_{max}} / |z_{G_{max}}|$$
 (4-17)

were chosen as preliminary values of the "guidance" control gains.

As stated above, the preliminary values of K_1 , K_{20} and K_{30} were adjusted to obtain values which result in reasonable response characteristics of the typical rocket simulated in this study.

5. SIMULATION RESULTS

5.1 General Comments

To check out the operation of the simulation codes and to study the effects of the various anomalies, such as winds, several simulations were carried out. In the course of these simulations, several different numerical integration algorithms were used to solve the flight phase equations of motion, while the launch phase equations were integrated using only a standard fourth-order Runge-Kutta algorithm. The procedures used to solve the flight phase equations were (1) a variable-step, fourth-order, Runge-Kutta algorithm, 6 (2) a variable-step Hamming predictor-corrector algorithm, 6 (3) a fixed-step, fourth-order, Runge-Kutta algorithm and (4) a fixed-step Euler algorithm.

The variable-step algorithms were not satisfactory because, during time intervals in which the control force changes very rapidly, the step-size adjusting segments of the algorithms failed to find a suitable step-size.

This occurred, not because of inaccuracies in the calculations, but as a result of the methods used to check on the accuracy of the computations.

The fixed-step algorithms were tested by using various step sizes and a "best" step size was obtained for each. These "best" step sizes are defined as those which produced consistent solutions and which are such that step sizes larger or smaller produced inconsistent results.

Simulations using the fixed-step, Runge-Kutta algorithm with its "best" step size require more computer time than their Euler algorithm counterparts. Hence, the fixed-step, Euler algorithm was used to generate the

results presented herein. However, the simulation code contains both algorithms and the one used is optional with the user.

5.2 Data Used in the Simulations

Most of the data for the launch phase simulations is given in Table 5-1. The remaining data is the angular rate of the launcher turnet and the tipoff distance. These were different for each of the cases for which results are given and may be found in Table 5-2.

The data for the flight phase simulations is given in Table 5-3 and Appendix C. The physical characteristics of the rocket are given in Table 5-3. The manner in which aerodynamic parameters were calculated is explained in Appendix C. Values used for the control gains were $K_1 = 0.125 \, \text{sec}^2$, $K_{20} = 0.03 \, \text{rad-sec/m}$ and $K_{30} = 0.03 \, \text{rad-sec/m}$.

5.3 Simulation Results

Since the question of whether the rocket is acquired by the IR sensor and guided in such a manner that radar acquisition is possible is the one of interest, only the flight phase results of the simulations are presented here. The results of the corresponding launch phase simulation provided the initial conditions for each flight phase simulation. The results for ten simulations are given here. These may be classified as follows:

Simulation 1 - No Anomalies

Simulation 2 - Tipoff

Simulation 3 - Mass Imbalance

Simulation 4 - Thrust Misalignment

Simulation 5 - Cross Wind

Simulations 6 and 7 - "Positive" Turret Rates

Simulations 8 and 9 - "Negative" Turret Rates

Simulation 10 - "Combination" of Anomalies

TABLE 5-1. LAUNCH PHASE DATA

Rocket

LENGTH 2.4 (m)

DIAMETER 0.16 (m)

MASS 62.4 (kg)

$$I_{x} = 0.325 \text{ (kg-m}^2)$$

$$I_y = I_z = 21.3 \text{ (kg-m}^2\text{)}$$

трист

16850.0 Nt)

SPIN TORQUE 100.0 (Nt-m)

Other Data

$$\frac{R}{T}A = (-0.95 \ 1.03 \ 0.0)^{T} (m)$$

$$\frac{R}{T}G = (-0.95 \ 0.0 \ -1.015)^{T} \ (m)$$

$${}_{t}^{r}C/A(INITIAL) = (1.001 0.0 0.0)^{T} (m)$$

$$\ell_{\rm E} = 2.4 \, (\rm m)$$

TABLE 5-2. DESCRIPTION OF FLIGHT CONDITIONS.

NI A	TIPOFF	TURRET ANGULAR PATE	MASS IMBALANCE	pa	THRUST MISAL IGNMENT	ENT	MIND NI NI	WIND VELOCITY IN INERTIAL	VELOCITY INERTIAL
NUMBER	(METERS)	(DEG/SEC)	μ ₂	, μ3	y y	z g	arcic arcic	M A	W W
1	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
7	0.15	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
ო	0.0	0.0	0.7	0.7	0.0	0.0	0.0	0.0	0.0
7	0.0	0.0	0.0	0.0	0.35	0.35	0.0	0.0	0.0
2	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.9-	0.0
9	0.0	+5.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
7	0.0	+10.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
œ	0.0	-5.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
6	0.0	-10.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
10	0.15	+10.0	0.7	0.7	0.35	0.35	0.0	0.9-	0.0

TABLE 5-3. FLIGHT PHASE DATA.

REFERENCE AREA FOR AERODYNAMICS - 0.021 (m²)

REFERENCE LENGTH FOR AERODYNAMICS - 0.16 (m)

TIME OF BOOSTER BURNOUT - 1.65 (sec)

MASS - (INITIAL) - 63.2 (kg)

MASS - (AT BOOSTER BURNOUT) - 58.3 (kg)

MOMENTS OF INERTIA (INITIAL) - $I_x = 0.325$ (kg-m²)

$$I_v = I_z = 21.5 \text{ (kg-m}^2\text{)}$$

MOMENTS OF INERTIA (AT BOOSTER BURNOUT) - $I_{y} = 0.299$ (kg-m²)

$$I_y = I_z = 15.46 \text{ (kg-m}^2)$$

u (INITIAL) - $(1.001 \ 0.0 \ 0.0)^{T}$ (m)

 \underline{u} (AT BOOSTER BURNOUT) - (1.110 0.0 0.0) $^{\mathrm{T}}$ (m)

$$\underline{\ell}_{T} - (0.124 \quad 0.0 \quad 0.0)^{T} \quad (m)$$

 $|x_1'| - 0.158$ (m)

 $x_2' - 0.793$ (m)

SLAT - 0.0 (m)

 $I_{sp} - 230.0 \text{ (sec)}$

 $F_{c_{max}} - 444.822 \text{ (Nt)}$

 δ - 0.0 (rad)

THRUST VALUES - 16850.0, 16850.0, 18471.5, 18471.5, 1621.5, 1621.5, 0.0 (Nt)

THRUST TIMES - 0.0, 0.200, 0.201, 1.650, 1.651, 13.350, 13.351 (sec)

No Anomalies

In Simulation 1 the turret is non-rotating, there is no tipoff, no wind and the rocket is "perfect," i.e., no mass imbalance nor thrust misalignment. The results for this simulation are shown in Figs. 5-1 through 5-17. The first four figures, Figs. 5-1 through 5-8, show Δt_y , Q_{NR_c} , Q_{NR} , Q_{NR_c} , $Q_$

For this simulation, guidance commands were possible after about 0.40 seconds. Due to the rocket's orientation at that time, lareral control was first exerted, then longitudinal control. Note that Δt_y and Δt_z had maximum magnitude at the start of guided flight, but not for the total simulation. Note that $Q_{NR_{_{\rm C}}}$ (Fig. 5-2) is composed of "pulses" for which the maximum values vary smoothly with time. Note also that the amplitude of the oscillatory curve obtained by connecting the midpoints of the extremities of adjoining steps has the appearance of a damped oscillation.

The time history of the angular rate about the y_{NR} axis, Q_{NR} , is shown in Fig. 5-3. Note the rapid response in Q_{NR} . Also, of interest are the

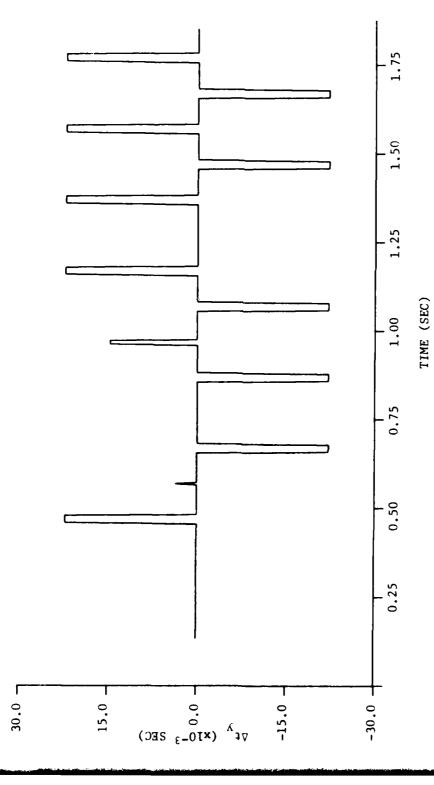


Figure 5-1. Pitch Control Time, Δt_y , for Simulation 1.

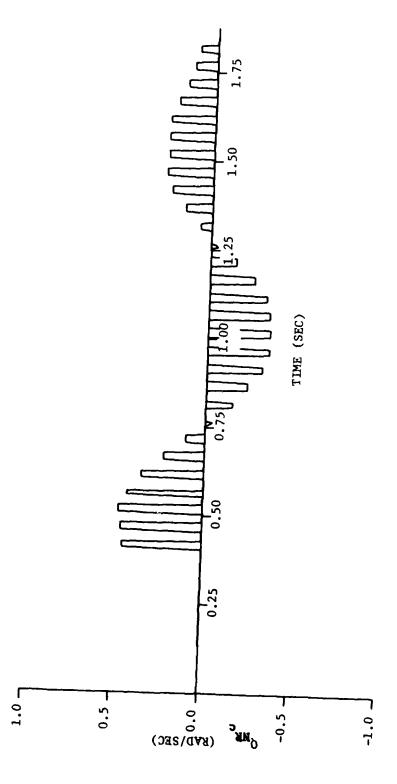


Figure 5-2. Commanded Non-rolling Angular Rate, $Q_{
m NR}$, for Simulation 1.

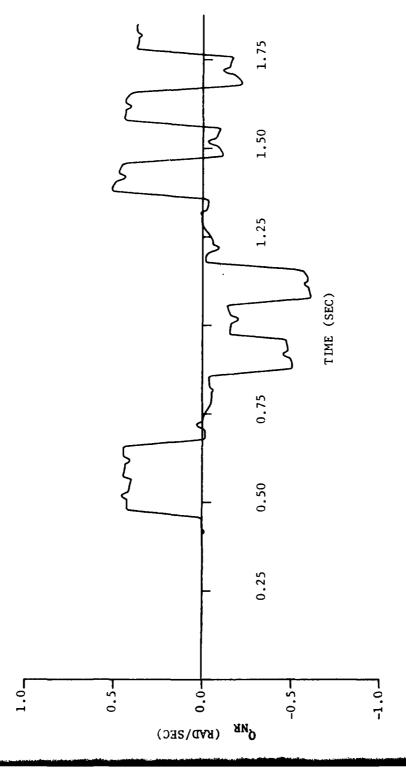


Figure 5-3. Non-rolling Angular Rate, $^{\rm O}_{
m NR}$, for Simulation 1.

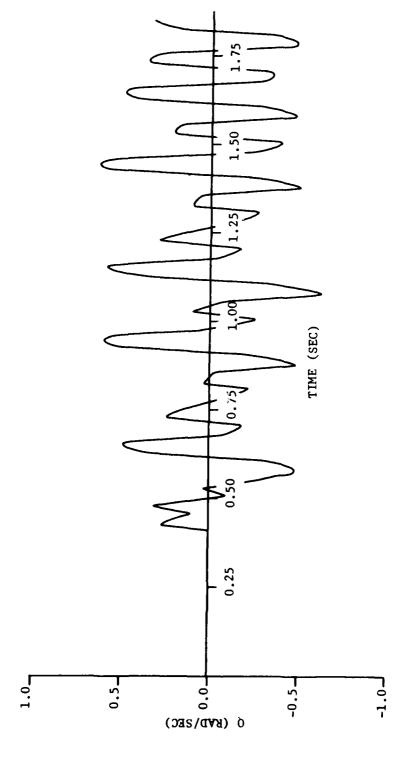


Figure 5-4. Rocket-Fixed Angular Rate, Q, for Simulation 1.

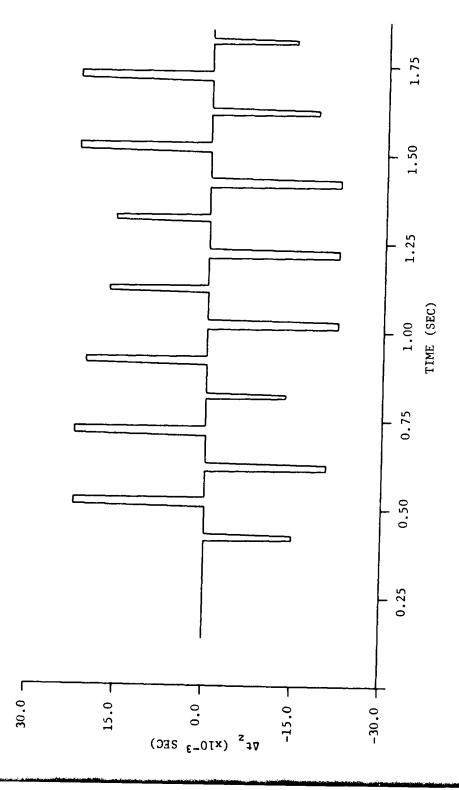


Figure 5-5. Yaw Control Time, Δt_y , for Simulation 1.

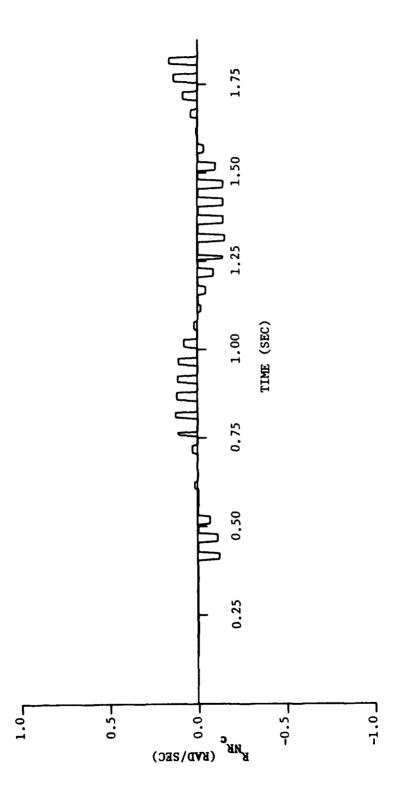


Figure 5-6. Commanded Non-rolling Angular Rate, $R_{\rm NR}$, for Simulation 1. $_{\rm C}$

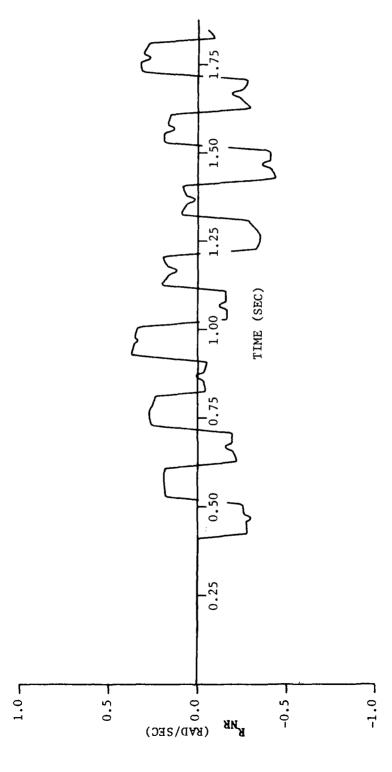


Figure 5-7. Non-rolling Angular Rate, R_{NR}, for Simulation 1.

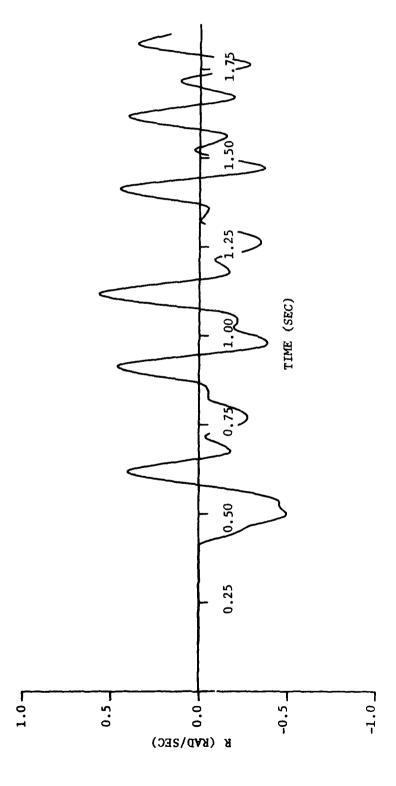


Figure 5-8. Rocket-Fixed Angular Rate, R, for Simulation 1.

small "bumps" and the Q_{NR} curve. These are due to the application of control forces during lateral control phases, since a finite control region centered on $\phi + \delta = [(2n+1)/2]\pi$, for example, with Δt_2 positive, results in first a small negative torque about that axis and then a positive torque. The net effect of each pair of positive and negative torques is essentially zero. We note that if there were no aerodynamic damping of transverse angular rates, the tops of the "pulses" in Q_{NR} would (except for the bumps) be flat between control force applications.

The angular rate about the y-axis is shown in Figure 5-4. Because δ =0 for these simulations, the control axis is the y-axis. Therefore, rapid changes in Q with time occur when control of either a longitudinal or lateral motion of the rocket takes place,

The results for Δt_z , R_{NR}_c and R_{NR} are similar to those for Δt_y , Q_{NR}_c and Q_{NR} , respectively. However, the rates R_{NR}_c and R_{NR} are generally smaller than their "longitudinal" counterparts. The angular rate about the z-axis, R, is a much smoother function of time than Q, since it results from the integrated effect of control torques applied about the y-axis.

Figures 5-9 and 5-10 are plots of the angles $\alpha_{\mathbf{x}}$ and $\beta_{\mathbf{x}}$ as functions of time. Since the wind was zero for this simulation, $\alpha_{\mathbf{x}} = \alpha$ and $\beta_{\mathbf{x}} = \beta$ and hence, these are the time histories of the angle of attack and side slip angle, respectively, of the rocket. Note that α and β are 90° out of phase, as should be the case.

The pitch and yaw angles of the rocket as functions of time are shown in Figs. 5-11 and 5-12. In this simulation the "target" was stationary and could be considered to be located on a line of sight with an elevation of

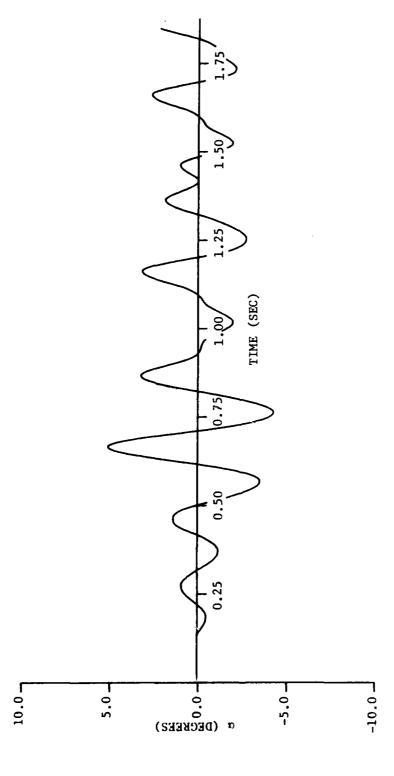


Figure 5-9. Angle of Attack Time History.

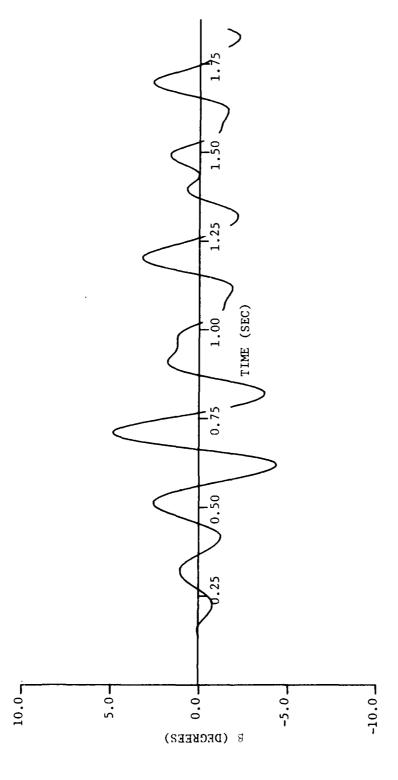


Figure 5-10. Sideslip Angle Time History.

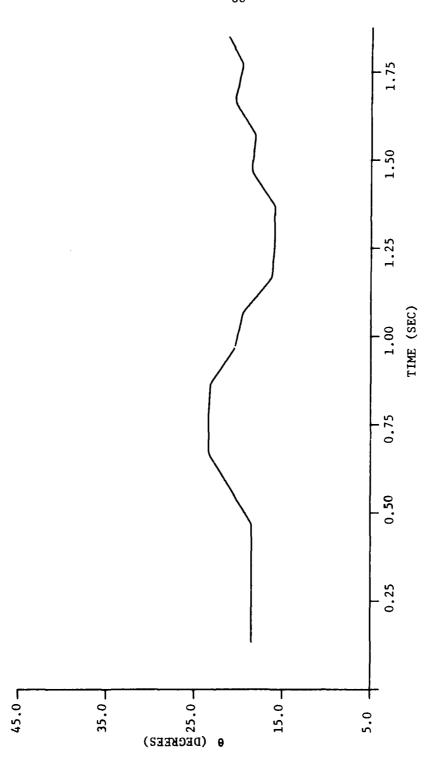


Figure 5-11. Pitch Angle Time History.

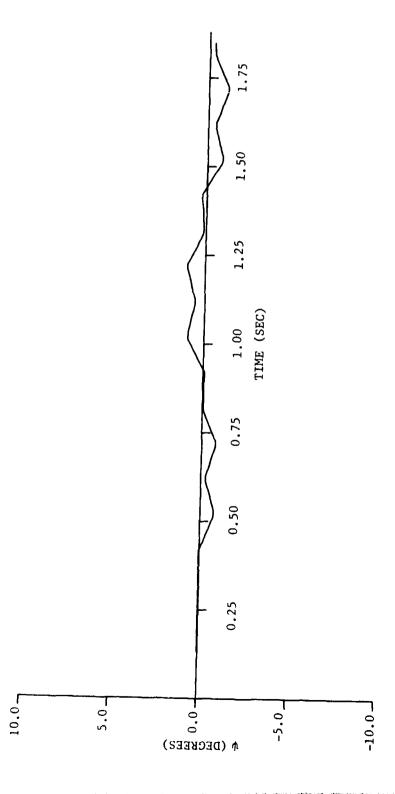


Figure 5-12. Yaw Angle Time History.

18.5°. The rocket's pitch angle was therefore 18.5°, initially. Due to the "gravity drop" as the rocket left the launch tube with zero aerodynamic incidence angle, the guidance and control systems operated to produce an increase in θ for a period of time during which the rocket reacquired, and overshot the line of sight. Long period oscillations in θ , with smaller short period oscillations superimposed then occurred. The yaw angle ψ was always small with mean value approximately zero. Figure 5-13 is included because it shows clearly the maximum and minimum values of θ and ψ which occurred.

The \mathbf{x}_{G} -coordinate of the center of mass of the rocket as a function of time is presented in Fig. 5-14. It is essentially a cubic function of time during the portion of flight simulated.

Three "views" of the trajectory of the center of mass of the rocket as seen in the $Gx_Gy_Gz_G$ system are given in Fig. 5-15. Also shown in Fig. 5-15 is the boundary of the 1° FOV of the IR sensor. This is the smaller of two FOV's used, the larger being 4.5°. We note that although the transverse angles are not very smooth functions of time, the trajectory of the rocket's center of mass is very smooth. The "head-on" view given in Fig. 5-15 shows that the center of mass of the rocket stays within 2 meters of the launcher to target LOS during the course of the simulation.

Tipoff

For the simulation in which tipoff from the launcher was included and for Simulations 3-10, only the three views of the trajectory are given. The three views of the trajectory for the tipoff simulation are shown in Fig.5-16.

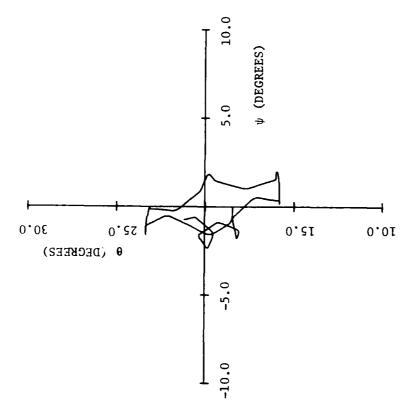


Figure 5-13. Yaw Angle vs. Pitch Angle.

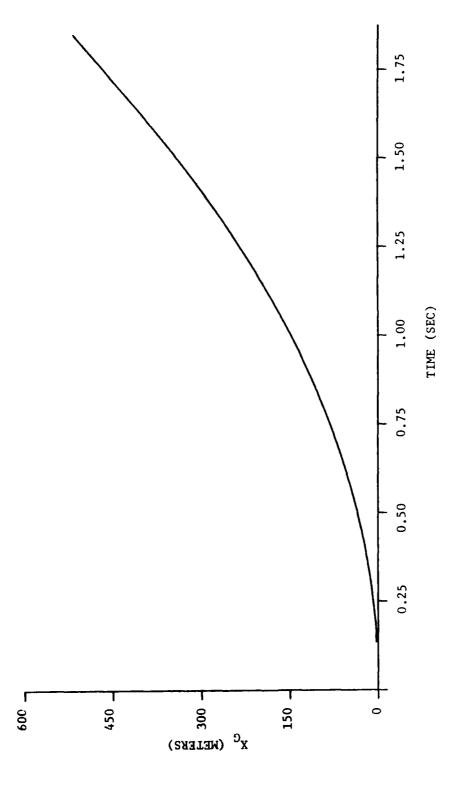


Figure 5-14. Time History of ${\rm x_G}$ -Coordinate of C.

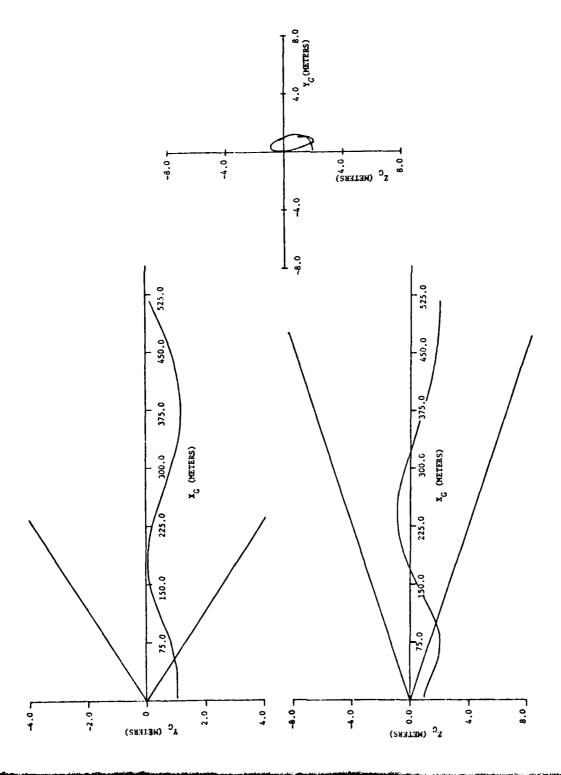


Figure 5-15. Trajectory for Simulation 1.

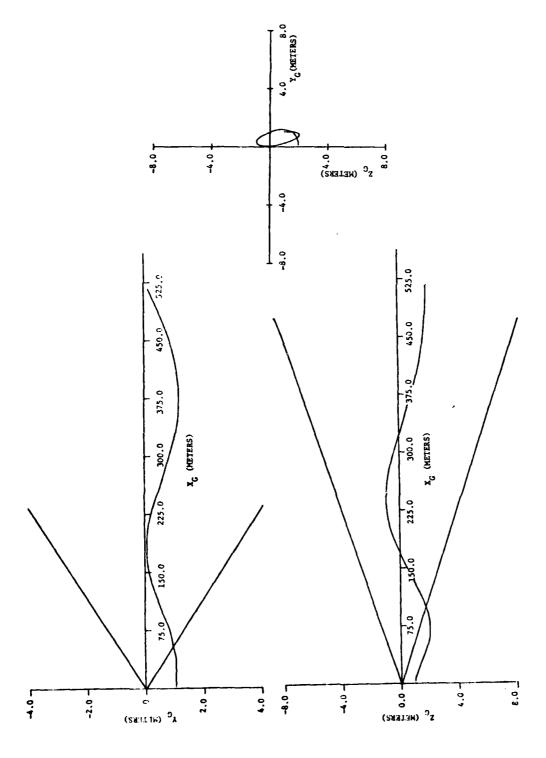


Figure 5-16. Trajectory for Simulation 2.

The main effects of tipoff are, of course, that the rocket has in initial transverse angular rate and its center of mass is also moving transversely when it clears the launch tube. Upon comparing the trajectory for the nominal simulation (Simulation 1) with that given in Fig. 5-16, we note little difference in the two sets of figures. Hence, by itself, tipoff (at least for a distance less than or equal to 0.15 m) is not significant.

Mass Imbalance

Since no rocket is perfect, each may be expected to be dynamically unbalanced. Simulation 3 was made to determine whether such mass imbalance would have a significant effect on the rocket's trajectory. In the simulation code the angles μ_2 and μ_3 (which are small angles of rotation about the y- and z-axes, respectively) were used to generate time varying products of inertia,

$$I_{xy} = -\mu_3 (I_{yy} - I_{xx}) \tag{5-1a}$$

and

$$I_{xz} = \mu_2 (I_{zz} - I_{xx}).$$
 (5-1b)

For $\mu_2 = \mu_3 = .0007$, the three views of the trajectory of the rocket's center of mass shown in Fig. 5-17 were produced via simulation. This particular source of error above does not appear to present any problem as far as guidance and control of the rocket are concerned.

Thrust Misalignment

Figure 5-18 shows three views of the trajectory generated by including only thrust misalignment as an error source. For the values, $\alpha_y = \alpha_z = .00035$,

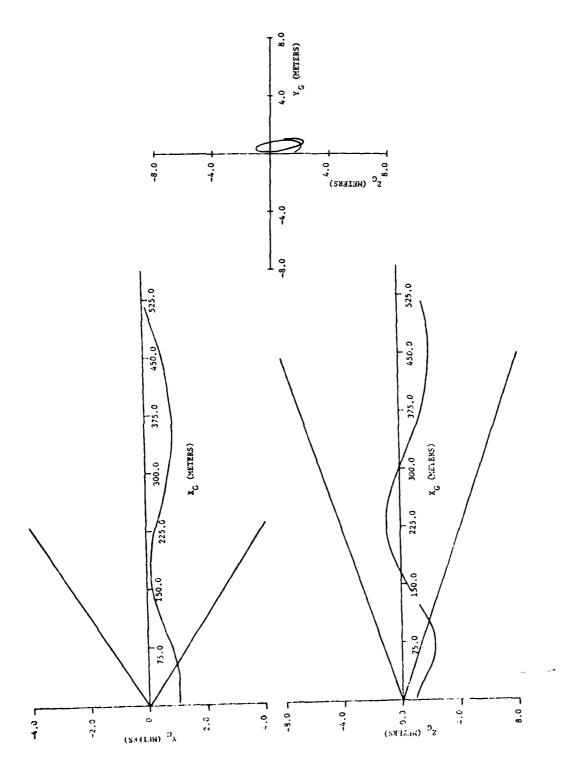


Figure 5-17. Trajectory for Simulation 3.

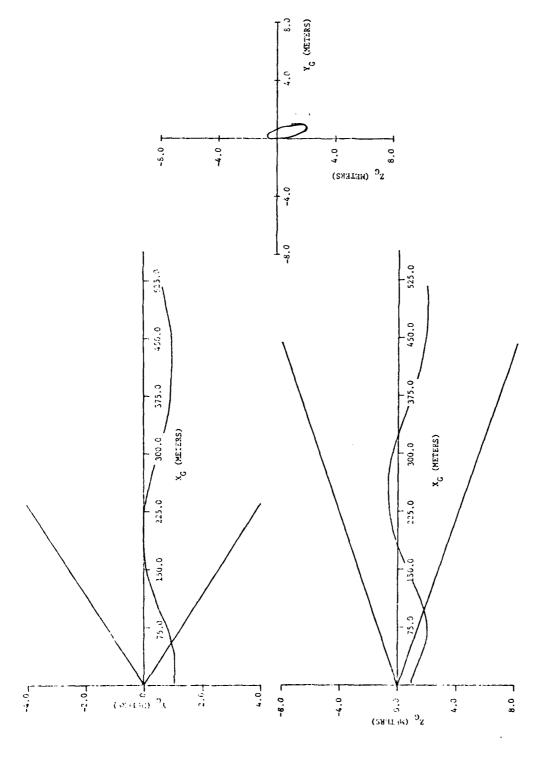


Figure 5-18. Trajectory for Simulation 4.

we note that thrust misalignment is also not a severe problem. That is, although there are recognizable differences in the trajectories for Simulations 1 and 4, these are not large enough to cause concern.

Several simulations were conducted to determine the relative effects of cross winds on the motion of the rocket. Simulation 5 is representative of the results obtained. In 5, a steady cross wind of 6 meters/second in the -Y-direction was included in the input for an otherwise nominal run. By comparing the trajectory shown in Fig. 5-19, with the nominal trajectory (Fig. 5-15) small differences may be noted. In particular, the rocket (since it is statically stable) turns into the wind. This is seen clearly by comparing Figs. 5-15 and 5-19.

Turret Angular Rates

Cross Wind

To track a moving target, the turret of the launch must rotate about the vertical axis \mathbf{z}_T . The rapidity of this rotation depends on the speed of the target, its distance from the launcher and its direction of flight. The $G\mathbf{x}_G\mathbf{y}_G\mathbf{z}_G$ system also rotates about its \mathbf{y}_G -axis during the tracking process. In this study, we have neglected this rate of rotation in the launch phase simulations, but not in the flight phase simulations.

For Simulations 6 and 7, the target's motions were such that the initial (for flight phase) angular rates of the launcher turret about the z_T -axis were +5°/sec and +10°/sec, respectively. The target's initial position for the two cases was (1800, 0, -600) km and the velocities were [302 157 0]^T m/sec and [130 314 0]^T m/sec, respectively. The rocket was fired, in both cases, from the right-hand tube of the launcher. Thus, in these simulations

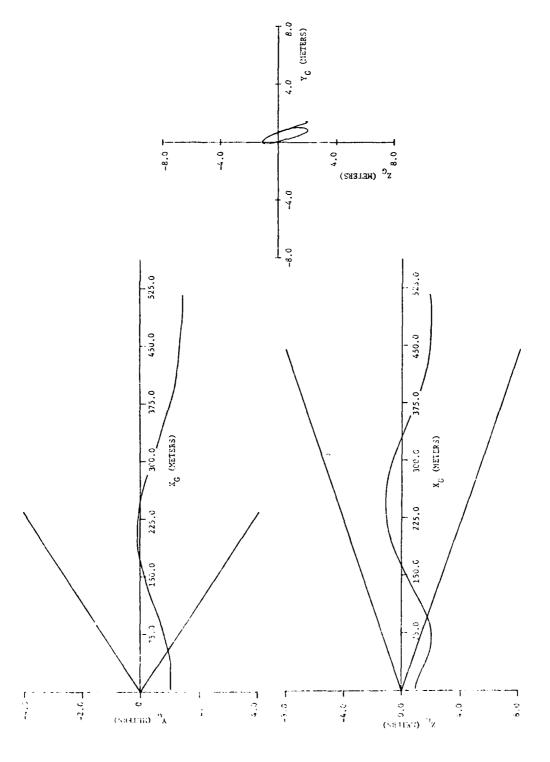


Figure 5-19. Trajectory for Simulation 5.

the FOV of the IR sensor was rotated so that it tended to "engulf" the rocket. This resulted in the entry of the rocket into the 4.5° FOV more quickly than in the nominal case (Simulation 1). Hence, guidance was begun sooner after launch in Simulations 6 and 7 than in the nomimal case. The trajectories for Simulations 6 and 7 are shown in Fig. 5-20 and Fig. 5-21, respectively. These results indicate that the system simulated would perform adequately even for the 10°/sec turret angular rate if the rocket were fired from the right-hand, or "leading" tube.

Results for negative turret angular rates about the $\mathbf{z}_{\mathbf{r}}$ -axis are shown in Fig. 5-22 and Fig. 5-23, for cases in which the initial rates were -5°/sec and -10°/sec, respectively. These were obtained by using the data used in Simulations 6 and 7, except the target velocities. These velocities were replaced by [301 -157 0] and [130 -314 0] m/sec, respectively, for Simulations 8 and 9. The rocket was acquired by the IR sensor when the initial rate was approximately -5°/sec, since its aft end did come within the wider, 4.5° FOV of the sensor (see Fig. 5-22). Also, the guidance and control system quickly brought the rocket within the narrower, 1° FOV of the sensor and it remained therein. However, in the -10°/sec case, the IR sensor's FOV was rotated away from the rocket's initial direction of flight so rapidly that, although the rocket entered the 4.5° FOV momentarily, it did not remain therein. Hence, guidance and control of the rocket was lost. Combination of Anomalies

Simulation 10 was made with a combination of anomalies as indicated in Table 5-1. As can be seen in Fig. 5-24, the rocket entered the 4.5° FOV and remained within the 1° FOV after reaching a range of approximately 310 m.

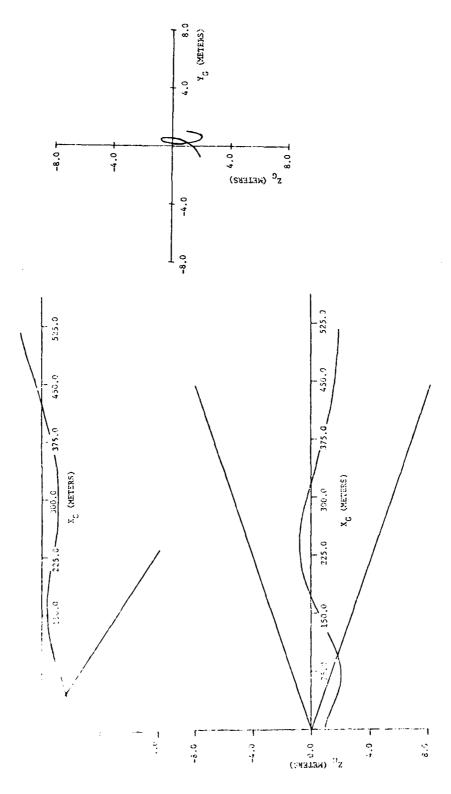


Figure 5-20. Trajectory for Simulation 6.

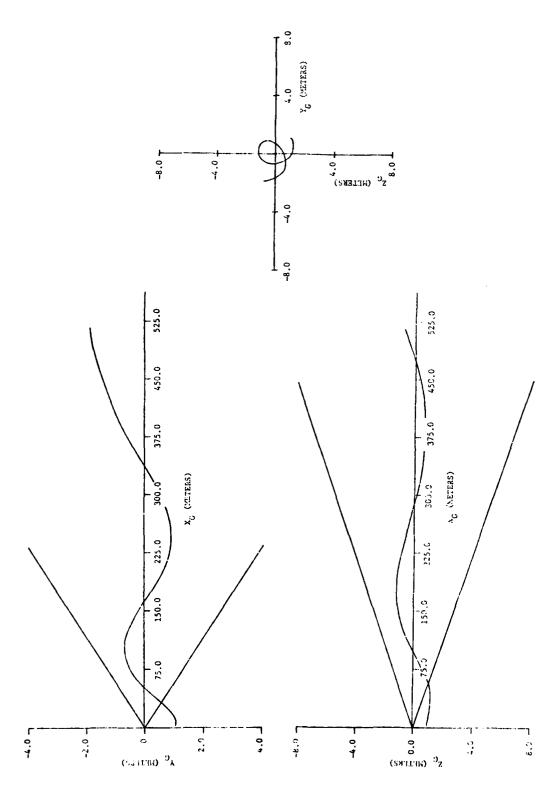


Figure 5-21. Trajectory for Simulation 7.

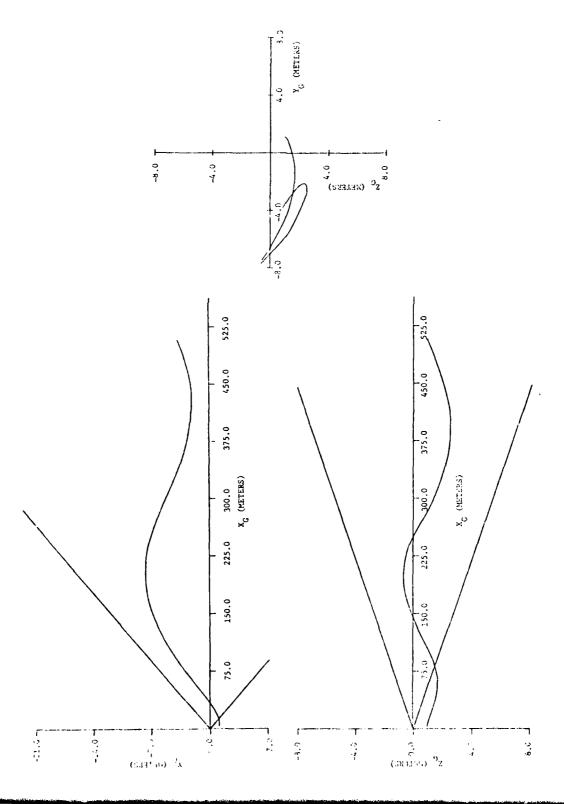


Figure 5-22. Trajectory for Simulation 8.

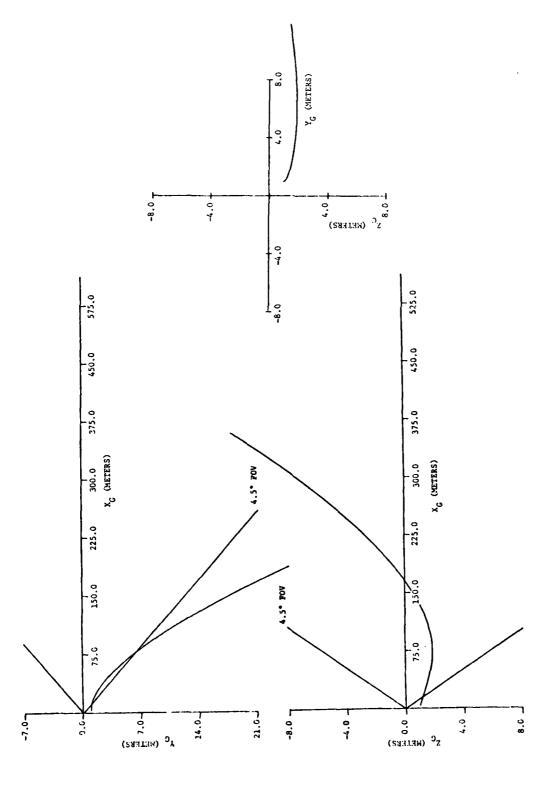


Figure 5-23. Trajectory for Simulation 9.

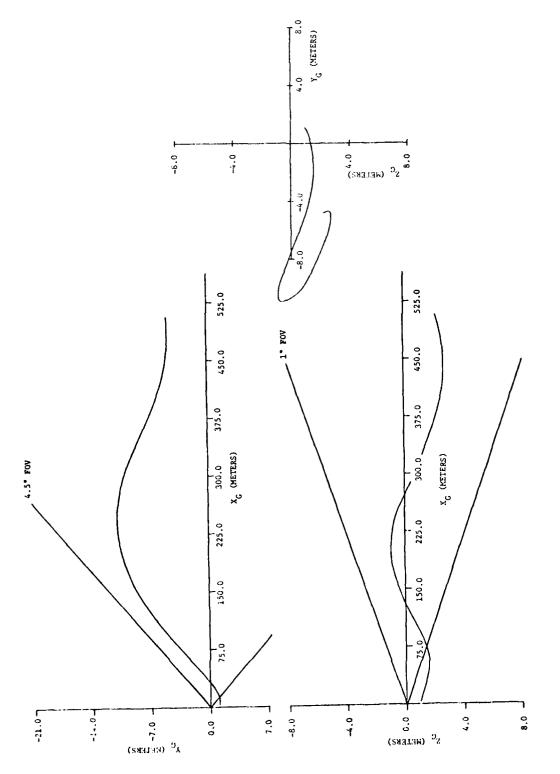


Figure 5-24. Trajectory for Simulation 10.

6. SUMMARY, CONCLUSIONS AND SUGGESTIONS

6.1 Summary

In this report we have described the physical and mathematical models which form the basis for digital simulation codes which may be used in studying the motion of a short-range air defense system rocket during launch and prior to its acquisition by a launcher-based radar. Listings of the FORTRAN IV digital computer codes are also included. The codes were used to simulate a typical system and results of these simulations have been presented and discussed.

6.2 Conclusions

The simulation codes are flexible enough that different systems may be simulated by changing data and/or subroutines. They are not as complex as some codes of a similar nature, since simulation of the operation of all the various subsystems is not attempted. However, many anomalies are modeled and the computer time required for each run is reasonable (around 2.5 minutes on an IBM 370/158 in conjunction with the FORTRAN H compiler.

In regard to the particular system simulated, it was found that the presence of anomalies such as cross-winds, mass imbalance, thrust misalignment, etc., of expected magnitudes did not prevent adequate operation of the system. The only factor which seems to be of major importance is the rate of rotation of the turret, and this is of vital importance only when the rate is large in magnitude (say, 10°/sec) and the rocket is fired from a "lagging" tube. This would appear to preclude the use of both rockets against two fast moving targets which appear successively. That is, if a target moving such that a large turret rate is necessary appears, if a rocket

is fired from the leading tube and the rocket guided to impact and, if before the time required for reloading has elapsed, another such target appears, based on the simulations made in this study, the second target cannot be successfully attacked.

6.3 Suggestions

On the basis of experience gained during the course of this study, it is suggested that additional attention be given to determining the effects of the following factors:

- Induced motions of the rocket due to launcher motions other than the angular rate of the turret about a vertical axis.
- 2. Unfolding of the wings of the rocket.

It is also suggested that the simulation codes presented herein be modified and/or extended to include mathematical models of the above factors.

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- 5. Beaty, James R., "Development of a Digital Simulation Code for a Short Range Air Defense Missile," Master of Science Thesis, Auburn University, Auburn, Alabama, August 1977.
- 6. IBM, System 1360 Scientific Subroutine Package (360A-CM-03X) Version III, Programmer's Manual, Fifth Edition, International Business Machines Corporation, White Plains, New York, 1970.

APPENDIX A

LISTING OF MISSILE SIMULATION (MISSIM) PROGRAM

On the following pages is a listing of the missile simulation (MISSIM) program used for the flight phase analysis in the report. The computer code developed is compatible with the FORTRAN G, FORTRAN H, or WATFIV compilers used in conjunction with the IBM 370/158 digital computer available at Auburn University. All computations in the program are done in the double precision mode.

All input into the program is formatted with a generalized (G) field descriptor and is accomplished with punched cards. Each card contains ten data fields which are eight columns wide. The generalized descriptor was chosen because it allows one to input logical, integer or real (external fixed point or floating point) variables using the same format. The entire input necessary to use MISSIM is read in the main program, and is explained below.

NVAL The number of thrust-time values tabulated for the missile (right-hand justified).

TVECTR Vector (dimensioned NVAL) of thrust magnitude times (sec).

FVECTR Vector (dimensioned NVAL) of thrust magnitude values (Nt).

XL Length of the missile (m).

Reference area for aerodynamics (m^2) .

D Reference length for aerodynamics (m).

RP Outer diameter of the booster motor propellant grain (m).

SRPL Initial inner diameter of the booster motor propellant grain (m).

RHOP Booster motor propellant density (kg/3).

PGL Booster motor propellant grain length (m).

ISP Booster motor special impulse (sec).

GRAV Gravity magnitude (m/sec²).

RHO Atmospheric ambient density (kg/m^3) .

TEMP Atmospheric ambient temperature (°K).

GAMMA Ratio of specific heats for air.

RAIR Gas Constant for air $(m^2/s^2-{}^{\circ}K)$.

XP1,XP2 Coordinates of ends of booster motor propellant grain (m).

SLAT Distance from point A to aft end of missile (m).

RT Vector from point A to a point on the line of action of the sustainer motor thrust (m).

TIMEV Five-element vector of times for CG location and moments of inertia values (sec).

VXCG Five-element vector of CG locations (m).

VIX Five-element vector of spin moment of inertia values (kg-m²).

VIY Five-element vector of pitch moment of inertia values (kg-m²).

VIZ Five-element vector of yaw moment of inertia values (kg-m²).

IXY, IXZ, Values of products of inertia. (Used if mass imbalance IYZ quantities are not specified) $(kg-m^2)$.

FCMAX Magnitude of control force (Nt).

DELTA Angle that the control plane makes with the z-axis (see Fig. 3-4)(rad).

RTUR Distance from axis of rotation of launcher turret to origin of goniometer system (m).

HANT Height of radar antenna from origin of inertial system (m).

TBEAM Half-angle of infrared seeker's field of view (rad).

TMAX Maximum allowed thrust deflector dwell time (sec).

TDELAY Delay time from command of control force until control force magnitude equals FCMAX (sec).

MAXRAT Macimum allowed commanded angular rates (rad/sec).

TBOOST Time of booster motor burnout (sec).

TBC Time of sustainer motor ignition (equals earliest time that control is possible)(sec).

EULER Logical variable defining type of integration routine desired. If Euler is true, integration is Euler; otherwise, fourth-order Runge-Kutta integration is used.

PRTSUP Logical variable indicating whether excess output is to be suppressed.

PLONLY Logical variable indicating whether output is to be printed only on the dataset.

H Integration step size (sec).

NEQ Number of dependent variables to be integrated (right-hand justified).

NUMB Number of integration steps before output is printed (right-hand justified).

NUMPPT Number of integration steps before output is stored for Dataset storage (right-hand justified).

UG, VG, WG Components of wind velocity in negative direction of inertial axes (m/sec).

TF Time at end of simulation (sec).

Time at beginning of simulation (sec).

ALY, ALZ Euler angles which orient the thrust vector (rad).

MU2, MU3 Euler angles which define principal axis rotations. Used to compute dynamic mass imbalance quantities (rad).

X Vector of initial values of the dependent variables (dimensioned NEQ). XTV Initial position vector of target in inertial reference system (m).

VTV Velocity vector of target in inertial reference system (m/sec).

GAIN1 Control gain Kl (sec²).

GAIN2 Control gain K2 (sec/m).

GAIN3 Control gain K3 (sec^2/m).

TITLE Eighty-character alphanumeric vector for the identifying title of the simulation.

Several additional vectors of input data used in subroutine AERO to determine the aerodynamic force and moment on the missile are described in Appendix C.

Output from the program can be obtained in three forms. Which form is obtained depends on input values of PRTSUP and PLONLY (explained above). In the normal form (PRTSUP = FALSE), much output is printed for checking purposes. In the suppressed form (PRTSUP = TRUE and PLONLY = FALSE), only the time and the state variables are printed. In the third form (PRTSUP = TRUE and PLONLY = TRUE) output is stored on DATASET only, and no printed output is obtained.

Comment cards have been provided liberally throughout the program to indicate the most important calculations and to provide the user with additional information.

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3EAD (5, 100) AVAL

X(6)=GLANDA X(11)=GDELDT*DCOS(X(4))+GLANDT*DCOS(GDELTA)*DSIN(X(4))

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READ (5,100) (ITVEC L(I), I=1,9)
READ (5,100) (F2VEC (I), I=1,9)
READ (5,100) ((F1MAT (I,J), J=1,6), I=1,10)
READ (5,100) (KVEC (I), I=1,3), (CHQVC1(I), I=1,3), (CHQVC2 (
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          READ(5, 100) (FIMEY(I), VXCG(I), VIX(I), VIY(I), VIZ(I), I=1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           1 , 5), IXY,IXZ,IYZ
READ(5,100) PCMAX, DELTA, RTUR, HANT, TBEAM, TMAX, TDELAY, NA
READ (5,100) (TVECTR(I), I=1,NVAL), (FVECTR(I), I=1,NVAL)
READ (5,100) XL,S,D,RP,SRPL,RHOP,PGL,ISP,GMAV
READ (5,100) RHO,TEMP,GAMMA,RAIR,XP1,XP2,SLAT
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      READ(5,100) (XTV(I),I=1,3), (VTV(I),I=1,3)
READ(5,100)GAIN1,GAIN3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         READ (5, 100) EULER, PRISUP, PLONLY
                                                                                                                          READ(5,100) (MACHVC(I), I=1,27)
READ(5,100) (CNAVC1(I), I=1,27)
                                                                                                                                                                                               (CNAVC2 (I), I=1,27)
                                                                                                                                                                                                                                (CNOVEC (I), I=1,27)
                                                                                                                                                                                                                                                            ( CDVEC (I), I=1,27)
                                                                                                                                                                                                                                                                                             READ (5, 100) (LRVEC (I), I=1, 22)
READ (5, 100) (BRVEC 1(I), I=1, 22)
                                                                                                                                                                                                                                                                                                                                                            KEAD (5, 100) (BRYEC2 (I), I=1, 10)
                                                                                                                                                                                                                                                                                                                                                                                              READ (5, 100) (MVECTR (I), I=1,6)
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READ(5,100) (X(I), I=1, NEQ)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   CALL TRACKR (TO, X, XDOT, 0)
                                                                                              READ (5, 100) (RT(1), I=1,3)
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  COMMON/COM 130/MACH VC, CNA VC1, CNA VC2, CNO V EC, CD V EC, LR V EC,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     COAMON/COM70/GDELTA, GLAMDA, GDELDT, GLAMDT, XTV (3), VTV (3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              BAVECT, BAVECZ, AVECTH, PIMAT, ITVECT, F2VEC, XVEC, CMUVCT,
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                                                                            abal+bebyac, avectr, levect, nachvc, nach, Jdcoep, naxrat
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  COMMON/COM110/FINEV(5), VIX (5), VIY (5), VIZ (5), VXCG (5)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    :PSI, MISSILE YAW ANGLE
:U, X COMP. UP MISSILE VELOCITY IN BODY AXES
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           DIMENSIOM X (13), XDOT (13), FA (3), MA (3), PVECTR (50), TVECTR (50), RT (3)
                                                                                                                                                                                                                                                                                                                                                                                                        HIT, IS, LT, JDCOZP, TMAX, TDELAY, MAXRAT, TJUOST, TBC
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X(10):P, MISSILE HOLL RATE IN BODY AXES
X(11):Q, MISSILE PITCH RAFE IN BODY AXES
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                                                                                                                                                                                                                                                                                                       SLAT, JAHMA, HAIR, RTUR, HANT, TBEAN
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       :PHI, MISSILE ROLL ANGLE
                                                                                                                                              REALT LENGIA, ISP, IXY, IXZ, IYZ
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                                                                                                                                                                          LOGICAL PLCNLY, FRTSUP, EULER
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                                                                                                                                                                                                                                                                                                                                           CORMON/COM40/FVECTR, TVECTR
            IMPLICIT SEAL*8 (A-H,0-Z)
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                                                                                                                                                                                                              CDBSGN/CDS 10/EA, NA
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X (4) X (5) x (6) x (7) (8) x

X (3)

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DIMENSION KI(13), K2(13), K4(13), K4(13), K(13), DELTA X(113), XPRIME (13), XDOT (13), X LAST (13)
COMMON/COM 150/EULER
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             NOW THAT THE K'S HAVE BEEN CALCULATED, COMPUTE THE VALUE OF DELIAX FROM THE WEIGHLED AVERAGE FORMULA.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            OUTPUT THE VALUE OF T,K, AND KDUI AF THIS STEP.
                                                                                                                                                                                                                                                                                                                                                0.) GO TO 17 CO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             IF EULER IS TRUE, THIS IS EULER INTEGRATION SO SKIP THE RUNGE KUTTA SECTION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         BEGIN THE SECTION TO COMPUTE THE K'S
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     SAVE THE VALUE OF X(I) AT THIS STEP.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   X PRIME(I) =X(I) +K1(I) *...5
CALL FUNCT(T PRIME,X PRIME,XDOT)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          X PRIME(I) =X(I) + ... 5 * K2(I)
CALL PUNCT(T PRIME, X PRIME, XDOT)
SUBROUTINE ERKINT (TO, TF, HIN, K, N)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            CALL FUNCT (T PRIME, X PRIME, XDOT)
                                                                                                                                                                                                                                                                                                                                             .GI.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  CALL OUTPUT (I,X,XDOI,IO,FF,H)
                                                                                                                                                                                                                                                                      (ro .Eu. TF) Gu To 1300
                                                                                                                                                                                                                                                                                                        SIGN = (DABS (TF-TO) / (TF-TO)
                                                                                                                                                                                                                                                                                                                                          IF (SIGN LLT. 0. AND. HIN
IF (HIN .EQ. 0.) GO TO 1500
CONTINUE
                                     IMPLICIT REAL*8 (A-H, K, U-Z)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           X PRIME(I) =X(I)+K3(I)
T PRIME=T+H
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 CALL FUNCT (T,X,XDOT)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  IF (EULER) GO TO 700
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         K2(I) = H*XDOF(I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             K3(I) = H*XDOT(I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      K4 (I) = 4*XDOT (I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              K1(I) = H * X DOT (1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          T PRIME=T+.5*H
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            X \text{ LAST}(I) = X(I)
                                                                          LOGICAL EULER
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           DO 200 I=1,N
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            DO 300 I=1,N
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       DO 400 I=1,N
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        DO 500 I=1,N
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      NIH=H
                                                                                                                                                                                                                                 I=T0
                                                                                                                                                                                                                                                                      41
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1, PLVC5(I), PLVC6(I), PLVC7(I), PLVC6(I), PLVC9(I), PLVC10(I)
2, PLVC11(I), PLVC12(I), PLVC13(I), PLVC14(I), PLVC15(I), PLVC
                          X(12) =-3D&LDf*DSIN(X(4))+GLAMDT*DCOS(GDELTA)*DCOS(X(4))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               COMMON/COME40/TIMYEC (1.00), PLVC1 (1000), PLVC2 (1000), PLVC2 (1000), PLVC3 (1000), PLVC3 (1000), PLVC4 (1000), PLVC4 (1000), PLVC4 (1000), PLVC3 (1000), PLVC10 (1000), PLVC3 (1000), PLVC10 (1000), PLVC3 (1000),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      SAITE THE TITLE OF THE RUN, ALCNG WITH THE SOLUTION OF THE SIGULATION, ON DAIASET IN UNFORMATTED FORM
                                                                                                                                                           CALL FAE EULEH/RUNGE KUTFA INTEGRATION MOUTINE
                                                                                                                                                                                                                                                                                                                  STORE THE SOLUTION ON DATASET
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        WAITE (11) (TITLE (I) ,I=1,20)
                                                                                                                                                                                                                                        CALL ERKIN (TO, TF, H, K, NEJ)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               316 (I), PLVC17 (I), PLVC18 (I)
COMTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         COMMON/COM 100/IITLE (20)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ISING UNIT NUMBER 11.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              SUBROUTINE SAVPLT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     NN. 1=1 COL OG
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    WRITE (11) NN
                                                                                                                                                                                                                                                                                                                                                                                                CALL SAVPLT
                                                                                       COMPINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                           Srop
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         100
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•					8	7						
PORMAL(1H1, ***********************************	RETURN END	SUBROUTINE OUTPUT (TIME, X, XDOT, 10, TF, H) IAPLICIT MEAL+H (A-H, O-Z) REAL+H TIMVEC, PLVC1, PLVC2, PLVC3, PLVC4, PLVC5, PLVC6, 1PLVC7, PLVC18, PLVC9, PLVC10, PLVC11, FLVC12, PLVC13, PLVC14,	2PLVC15,PLVC16,PLVC17,PLVC18,SNGL LOGICAL PAISDE,PLONLY REAL+8 MCY,NCZ,MAXHAT REAL+8 JUCUEF,II,IS DIMENSION X (13),XDOT (13)	14G35T, VR CUNNON/CONSO/ECNAX, DELTA, GRAV, CMA, CZA, CMQ, UDOT, DIA, TAHOS, IT, IS, LZ, JDCOEP, THAX, IDELAY, MAKRAT, TBOOST, TBC CONNON/COM190/XG (3), VG (3), DEGDEL, DEGLAM, CNR, BNR CONNON/COM190/XE (3), VBLTZ, ANGY, ANGZ, PHTPD, SGN, PY, PC7	1MCY, MCZ, XK1, XK2, XK3 COMMON/COA220/B, RDOT, RPSY, EPSZ, EPSZDT, EPSZDT, D, DHAX COBBON/COM240/FINVEC (1000), PLVC1 (1000), FLVC2 (1000)	1PLVC3 (1000), PLVC4 (1000), PLVC5 (1000), PLVC6 (1000), PLV 2C7 (1000), PLVC8 (1000), PLVC3 (1000), PLVC10 (1000), PLVC 311 (1000), PLVC12 (1000), PLVC13 (1000), PLVC14 (1000), PLVC	415 (1000), PLVC16 (1000), PLVC17 (1000), PLVC18 (1000), NN COMMON/COM90/NUMB, NUMPPT COMNON/COM210/2NRC, MNRC, DLTZ COMMON/COM140/21CM1Y, DRTSHB	RAD=57.29577951DO IF(DABS(TIME-TO) .Gr. 1.D-5)GO TO 100 NN=0	NUMBPL=(TF-TO)/H/NUMPPT NSTEP=NUMB PRINT 1300,XK1,XK2,XK3 GO TO 200	IP (NPSTEP .GE. NUMBPL) GO TO 200 NPSTEP=NPSTEP+1 GO TO 300 NM=NN+1	STURE THE SOLUTION VALUES AT THIS STEP IN ARRAYS POR DATASET STORAGE LATER.	
1900										100		
C 600 DELFA X (1) = (K1(I) + 2*K2 (1) + 2*K3 (1) + K4 (1)) /6. 30 TO 900 700 CONTINUE	DO 02LTA X(I)=H*XDOT(I)	C ADD DELTA X TO X TO GET ITS NEW VALUE FOR THE NEXT STEP. JOO CONTINUE DO 1000 I=1,N	1000 X(I)=X(I)+DELTA X(I) C CAECK TO SEE IF T IS STILL IN THE SPECIFIED INTEGRATION C INTERVAL. IF IT IS, CONTINUE INTEGRATING. IF IT IS C MOT, STOP HERE.	IF(SIGN .GT. 0AND. T .LT. TF) GU TO 1200 IP(SIGN .LT. 0AND. T .GT. TF) GO TO 1200 IMH=T-H DO 1100 I=1,N	1100	C OUTPUT THE VALUES POR T, X, AND XDOT POR THE PINAL C INTERVAL.	CALL OUTPUT(T,X,XDOT,T0,TF,H) GO TO 1500 1200 CONTINUE	C SINCE T IS STILL IN THE SPECIFIED INTEGRATION INTERVAL C GO TO 130 AND CONTINUE INTEGRATING.		IF THE INPUT DATA FOR THE RUNGE-KUTTA ARE NOT FEASIBLE. 1300 WRITE (6,1400) TO 1400 FORMAT (141, ***********************************		

BEST AVAILABLE COPY

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21H ,2x,'DELTA G=',G12.5,3x,'LAMBDA G=',G12.5,3x,
3 ALPHA=',G12.5,3x,'BLTA=',G12.5,3
900 PORMAT(H ,2x,'CZA=',G12.5,3x,'CMA=',G12.5,3x,'CMQ=',
1G12.5,3x,'UDGT=',G12.5,3x,'IT=',G12.5,7,1H ,2x,'IS=',
2G12.5,3x,'LT=',G12.5,3x,'JDCOEF=',G12.5,3x,'IM1. STEP='
                                                                                                                                                                                                                                      1000 FORMAT (1H ,2X,*R=',G12.5,3X,*RDOI=',G12.5,3X,*D=',G12.1,5,3X,*DBAX=',G12.5,7,1H ,2X,*K1=',G12.5,3X,*K2=',G12.5,3X,*DBAX=',G12.5,3X,*DBAX=',G12.5,3X,*DELTZ=',G12.5,3X,*DELTZ=',G12.5,3X,*DELTZ=',G12.5,3X,*DELTZ=',G12.5,3X,*DELTZ=',G12.5,3X,*DELTZ=',G12.5,3X,*DELTZ=',G12.5,3X,*DELTZ=',G12.5,3X,*DELTZ=',G12.5,3X,*DELTZ=',G12.5,3X,*DELTZ=',G12.5,3X,*DELTZ=',G12.5,3X,*DELTZ=',G12.5,3X,*DELTZ=',G12.5,3X,*DELTZ=',G12.5,3X,*DELTZ=',G12.5,3X,*DELTZ=',G12.5,3X,*DELTZ=',G12.5,3X,*DELTZ=',G12.5,3X,*DELTZ=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*K30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5,3X,*M30=',G12.5
                                                                                                                                                                                                                      ,///, 3X, "TIME=",F7.4,3X," MASS=",G12, 5,3X,
600 IP(FLUNLY) GO TO 700
                                         PRINT 1200, TIME
GO FO 500
                                                                                                                                       700 RETURN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        3,612.5)
                                                                                                                                                                                             O
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                Ų
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              AN (ESTEP .GE. NURB) GO TO 400
                                                                                                                                                PLVC3 (NN) = SNGL (XG (3))
PLVC4 (NN) = SNGL (X (5) *RAD)
PLVC5 (NN) = SNGL (X (6) *RAD)
PLVC6 (NN) = SNGL (X (8) *RAD)
                                                                                                                                                                                                                                                                                                                                             PLVC7 (NE) = SNGL (X (9) *RAD)
PLVC8 (NE) = SNGL (X (11) )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          VEL=DSQRT (X (7) **2+H**2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      PLVC10 (NN) = SNGL (GNR)
PLVC11 (NN) = SNGL (RNB)
PLVC12 (NN) = SNGL (NRC)
PLVC13 (NN) = SNGL (NRC)
PLVC14 (NN) = SNGL (BNRC)
PLVC14 (NN) = SNGL (DLTY)
                                                             PLVC2 (NN) = SNGL (XG (1) )
PLVC2 (NN) = SNGL (XG (2) )
                                                                                                                                                                                                                                                                                                                                                                                                                                                    PLVC9 (NN) = SNGL (X (12)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             H=X (7) +DTAN (X (4))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    V=VEL+DIAN (X (3))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           ALPDEG=X (8) *RAD
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            BETDEG=X (9) *RAD
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ANG5=X (5) *8AD
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ANGU=X (4) *RAD
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ANGE X (6) *RAD
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     PLVC16 (NN) =0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               PLVC17 (NN) =0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        PLVC18 (NN) =0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 NSTEP=1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              RETURN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   350
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PRINTED IF PECNEY IS TRUE, ONLY DATAILED STORAGE OF PRESCULLON IS DESIRED, SC NO OUTPUT IN TO BE PRES RELURN

PAINT 1500,X (1),XG(1),ANG4,X (10),X (7),VG (1),X (2),XG (2),ANG5,X (11),2NA,V,VG (2),X (3),XG (3),ANG6,X (12),RNK,M,

PRINT 1403, (XDOT (I), I=1,13)

IF (PRISUP) GG TO 600
PRINT 800, TIME, X (13), XCG, XCF, STMAR, DEGDEL, DEGLAM, A
ILPDEG, BETDEG
PRINT 900, GZA, CHA, CHQ, UDOF, IT, IS, LT, UDCULF, d
PRINT 1000, R, HDOF, D, DHAX, XK1, XK2, XK3
PRINT 1100, DELTY, DELTZ, ANGY, ANGZ, PHIFD, SGN, PCY, FCZ,

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SUPRESSED, SO SKIP THIS SECTION.

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ON PAPER

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MISSILE VELOCITY IN BODY AXES FACE THE ANGLE OF ATTACK, THE SIDESLIP ANGLE, AND THE MISSILE SPEED
COMPUTE V AND W, THE Y AND Z COMPUNES OF THE
                                                                                                                                                                                                                                                                                                                                                                 TANT=STHETA/CTHETA

XDOT(4) = X (10) + X (11) * SPHI*TANT+X (12) * CPHI*TANT

XDOT(5) = X (11) * CPHI-X (12) * SPHI

XDOT(6) = (X (11) * SPHI+X (12) * CPHI) / CTHETA

CALL INTERP(TIME, XCG, TIMEV, VXCG, 5, NSTOP)

IF (NSTOP .LT. 0) STOP 130
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     CALL THE AERODYNAMIC SUBROUTINE TO OBTAIN THE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          CALL THRUST (TIME, T, TVECTR, FVECTR, NVAL)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             COMPUTE THE THRUST PORCE AND MOMENT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            AEKODYNAMIC FORCES AND ACMENTS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 COMPUTE THE SEPTEMBERS HORIENT
                                                                                                                                                                                                                                                                     VB(3)=W
CALL MATXV(LBVINV,VB,VTHANS)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       CALL TAIDE (RT, RT TILD)
CALL MATKY (RF PILD, FT, MT)
                                                                                              W=X(7) *DTAN(X(3))
VEL=DSQRT(X(7) **2+W**2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     FI(2) = T*CALFAY*SALFAZ

PI(3) = -1*SALFAY

RI(1) = KTSTOR(1) - U1

RI1=DABS(RI(1))

RI(2) = RISTOR(2)
                                                                                                                                             V=VEL+DTAN (X (9))
VRSQ=X (7) * *2+V**2+#**2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  PT (1) = T + CALFAY + CALFAZ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        SALFAZ =DSIN (ALFAZ)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     U1=LENGTH-XCG-SLAT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      CALPAY = DCOS (ALFAY)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           SALFAY=DSIN (ALFAY)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     CALPAZ=DCOS (ALFAZ)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        SOUT =- T/ (ISP * GRAV)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              CALL AERO (TIME, X)
                                                                                                                                                                                                                                                                                                                                              XDUT (I) =VTRANS (I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  RT (3) = R1STOR (3)
                                                                                                                                                                                                 VR=DSURI (VRSU)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  TOOL (11) = NOOF
                                                                                                                                                                                                                                                                                                                  DO 4001=1,3
                                                                                                                                                                                                                        VB(1) = X(7)
                                                                                                                                                                                                                                              V3(2) = V
                                                                                                                                                                                                                                                                                                                                              000
    9000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 0000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              o o o
                                                                                                                                                 1PA (3), FT (3), PG (3), FC (3), MA (3), MI (3), MC (3), DODEGA (3),
2VTRANS (3), MJO (3), IDOTCM (3), ANGACL (4), AA (3), RT (3),
3OMEGXV (3), VB (3), ANG (3), OMEGAI (3, 3), INERTA (3, 3), ININV
4 (3, 3), OMEGA (3), VV (24), VEC1 (3), VEC2 (3), RTSTOR (3), RT TILD
5 (3, 3), LBV (3, 3), LBV INV (3, 3)
COMMON/COM120, LSP, IXX, IXZ, IYZ, PGL, Uc, VG, NG, LENGTH, XP1,
                                                                           11Y, 12, NA, MI, AC , IXX, 1XZ, IYZ, ISP, LENGIH, MG, MJD, JDCOEP,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        CALL CMAT (VV.LBV.LBVINV, SPSI, CPSI, STHETA, CIHETA, SPHI,
                                                                                                                            DIMENSION X(13), XDOT(13), IVECTR(50), FVECTR(50), P(3),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              TRANSPORM WIND VELOCITY FROM INERTIAL TO BODY SYSTEM
                                               AZAL ** 1901, 145S, INERTA, ININV, ILOTOM, LBV, LSVINV, IX.
                                                                                                                                                                                                                                                                                                                                                                                                    COMMON/COMSO/FCMAX, DELTA, GRV, CMA, CZA, CMW, UDOT, DIA, 1RHOS, IY, IX, K?1, JDCOEF, TMAX, TDELAY, MAXRAR, FBOOST, FBC
                                                                                                                                                                                                                                                                                                                                                                                                                                                                        COMMUN/COMINATIMEV(5),VIX(5),VIX(5),VIZ(5),VXCG(5)
COMMON/COM230/XCG,XCP,SIMAM,ALPHA,BETA,UGUSI,VGUSI,
                                                                                                                                                                                                                                                                                                                                                                              COMMON/COM 20/ALFAY, ALFAZ, MU2, MU3
                                                                                                                                                                                                                                                                                                                                                       COMMON/COM40/FVECIR, TVECTR
                                                                                                                                                                                                                                                                                                   IXP2, GRAV, SLAT, RT STOR, NVAL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          PHIDEG=X (4) *57, 2957795100
                           IMPLICIT REAL®S (A-H,O-Z)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         CALL MATXV (LBV, VEC1, VEC2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     X (4) = DMOD (X (4), IMOPI)
                                                                                                                                                                                                                                                                                                                                                                                                                                                     COMMON/COM160/FC, MC
                                                                                                                                                                                                                                                                                                                               COMMON/COM 10/FA, MA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   PI=3, 14159265400
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 JMEGA(I)=X(I+9)
CONTINUE
                                                                                                         2472,4U3,4AXRAI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        DO 300 I=1,3
VV (I+3) =ANG(I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   DO 200 I=1,24
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                UGUST = VEC 2 (1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        1G 331 = VEC 2 (2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             HGUST=VEC2 (3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         50 100 I=1,3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ANG (1) = X(4)
ANG (2) = X(5)
ANG (3) = X(6)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             THUPI=2. *PI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 00.0= (I) VV
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                7EC 1 (1) = UG
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       VEC1 (2) = V-3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             VEC 1 (3) = #G
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  MASS=X (13)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            WGUST, VR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 (LPHI)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   200
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           100
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                300
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         o o o
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JD CORP=-3007*([01-xP2/1.00]*PGL+XP1*XP1/3.00]

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90
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AUDIT (E) ENCHOSTS (EDGT-GBOSEDTAN (K (E)))

COSUTTO VELLY VELL

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1RHOS, II.IS, LI, JECOEF, THAN, IDELAY, HANRAT, THOOST, TBC
COMMON/COA130/MACHVC, CNAVC1, CNAVC2, CNOVEC, CDVEC, LRVEC,
13RVEC1, ERVEC2, MVLCTR, FINAT, ITVECT, F2VEC, XVEC, CMQVC1,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               1F1MAF (10,6), LIVECT (9), F2VEC (9), MACHYC (30), CNA
2VC1 (30), CNAVCZ (30), CNOVEC (30), CDVEC (30), VECTR
31(6), VECTR 2 (6), X (13), LBV (3,3), VEC1 (3), VEC2 (3), LVB (3,3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  COMMON/COM 30/MACH, ALFA, BELA, AL, S, RHO, DIA, TEMP, XCG, XCP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ISLAT, GÄMMA, R, RIUR, HAMI, IBEAN
COMMON/COASO/FCMAX, DELIA, GRAV, CMA, CZA, CMQ, UDUI, DIAM,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       COMMON/COM23J/XXCG, XXCP, STMAR, ALPDEG, BETDEG, UGUST, VG
                                                                                                                                                                                                                                                                                                                                                                                                                                                        IMPLICIT REALMS (4-H,0-Z)
REALMS MS, MACHN, L, L1, LMKGG, II, IS, LI, JDCOEF, LBV, LVB,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              DIMENSION LAVEC (22), BRVECT (22), BBVEC2 (10), MVECTR (6)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                IMAXBAT, LRVEC, MVECTE, ITVECT, MACHYC, MACH, M, ITANGL, LR,
                                                                                                                                                                                                                                                                                                   IP (DASS (XDOT (III)) . LT. 1.0-15) XDOT (III) = 0. DU
ROUT(4) ACC BUTTO (VDOT-UTAN (K (4))/VELOCONST2)
CALL GATKE (THEESTAN GREEA, TOUTOR)
CALL GATEV (CHECAT, LOCTOR, ANGACL)
                                                                                                                        AA (1) =-AB :ALL (1) + HT (1) + BA (1) + BC (1) + BJD (1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        DINEMSION AVEC (3), CRUVC1 (3), CRUVC2 (3)
                                                                                                                                                    CALL SATING (TREFTA, ININV, DETINA)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            W=X (7) *DTAN (K (8))
V=DSQRT (X (7) **2+W**2) *DTAN (X (9))
                                                                                                                                                                                     CALL MATER (INLAW, AA, DOMEGA)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   1151, WGUST, VR
EQUIVALENCE (ALPHA, ALFA)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           VRTSU=U:**2+VT**2+WT**
                                                                                                                                                                                                                                                                                                                                                                                                                              SUBROUFINE ACAU (TINE, K)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       DIMENSION FA(3), HA(3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        a=dsdrt (gamma=r=temp)
                                                                                                                                                                                                                                             KDUT (1++) = EDMEUA (1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CORNON/COR 10/FA, RA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        VRT=DSQRT (VRTSQ)
                                                                                                                                                                                                                                                                          30 800 III=1,13
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    UT=X(7) +UGUST
                                                                                              1,1=1 3(A CC
                                                                                                                                                                                                                    1.1 1.00 CC
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         LMXCG=L-XCG
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      MACHN=VRT/A
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    RHOS=RHO*S
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      VT=V+VGUSA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ISO DM+M=IM
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     MACH-MACHN
                                                                                                                                                                                                                                                                                                                                    800 CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   SOXX=SOX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                DIAMSDIA
                                                                                                                                                                                                                                                                                                                                                                 BETURN
                                                                                                                                                                                                                                                7 00
                                                                                                                               630
                                                                                                                                       INTERPOLATE TO FIND THE VALUES OF MURENTS OF IMENTA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  CALL THE CONFROL SUBROUTINE TO OBTAIN THE CONTROL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             COMPUTE THE HEIGHT COMPONENTS IN BODY AXES
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              INERTA (1,2) =-303* (INERTA (2,2) - INERTA (1,1))
INERTA (1,3) = AU2* (INERTA (3,3) - INERTA (1,1))
                                                                                                                                                                                                                         CALL INTERP (TIME, IX, TIMEY, VIX, 5, MSTOP)
IP (NSIOP .LT. 0) STOP 110
CALL INTERP (TIME, IX, TIMEY, VIX, 5, NSIOP)
                                                                                                                                                                                                                                                                                                                   IP (MSTOP LIT. U) STOP 120
CALL INFERP (TIME, IZ, TIMEV, VIZ, 5, WSTOP)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   COMPUTE DYNAMIC IMBALANCE QUANTITIES.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           CALL TILDE (OMEGA, UMEGAT)
CALL JATAV (OMEGAT, VB, OMEGAV)
USOT=-OMEGAV(1)+F(1)/MASS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    F(1) = PA(1) + PG(1) + PT(1) + PC(1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  700T=-ONEGXV (2) +F (2) /NASS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              #DOT=-JMEGXV (3) +F (3) /MASS
                                                                                                                                                                                                                                                                                                                                                                        IP (NSTOP .LT. 0) STOP 140 INERTA (1,1) = IX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            CALL CONTRL (TIME, X, XDOF)
                                           MJD (2) =-2. *JD COEP *X (11)
                                                                            MJD (3) =-2. *JD CUEF*X (12)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      INERTA (2, 1) = INERTA (1,2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     INESTA (3, 1) = INERTA (1,3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              PG (2) = MG*CIHETA*SPHI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          PG (3) = MG*CTHETA*CPHI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 PORCES AND MOMENTS.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              CONSTI-X(7)/VEL/VEL
                                                                                                                                                                                                                                                                                                                                                                                                                                      INERTA (1,2) =-IXY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       INERTA (2,2) = IY
INERTA (2,3) =- IYZ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                IMERTA (3, 1) =- IXZ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              INERTA (3,2) =- IYZ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    PG (1) =-MG*STHETA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                  INERTA (1,3) =-IXZ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                INERTA (2, 1) =- IXY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                INERTA (3, 3) = 12
                                                                                                                                                                      AF THIS TIME.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     500 I=1,3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Jodn= (1) Jocx
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          MOSSAGE AV
                         31D (1) =0. DO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    200
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P1=F11+((F12-F11)/(ENVEC2(1)-33VEC2(IM1))) + (BR2-BRVEC
                                                                                                                                                                                                                                                         FOUND BY INTEAPOLATING THE PZ VECTOR FOR THE VALUE OF
                                                                                                                                                                                                                                                                                                                                                                                                                                 NOW THAT PIAND F2 HAVE BEEN FOUND, THE MISSILE'S CENTER OF PRESSURE, MEASURED FROM THE NOSE, CAN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          CLP=-10.8009-1.15415*ITANGL+.164189*ITANGL*ITANGL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CLP=-9.40571-1.20858*ITANGL+.057145*ITANGL*ITANGL
                                                                                                                                                                                                                        NOW THAT PI HAS BEEN FUUND, THE VALUE FUR P2 CAN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            MA (2) =Q3*D1A* (CMQ*X (11) *_5*D1A/VRT+CN* (XCG-XCP))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   MA(3) = 25*DIA* (CNR*X (12) *.5*DIA/VHT+CY* (XCP-XCG))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               MA(1) = US*DIA* (CLP*X (10) * 5*DIA/VRT+CLNU*NU) +L0
                                                                                                                                                                                                                                                                                                                                                           CALL INTERP (ANGL II, PZ, ITVECT, FZVEC, 9, NSTOP)
IF (NSTOP .LT. J) STOP 160
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 1-8.37143E-03*ITANGL**3-3.73996E-05*ITANGL**4
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    COMPUTE THE AEEODYNAMIC FORCES AND MOMENTS
                          IP(MACH .GE. SVECTR(6)) M=MVECTR(6)
CALL INTERP(4,P11,MVECTR,VECIR1,6,NSIUP)
                                                                                                 CALL INTERF (M.F.12, MVECTR, VECTR2, 6, NSTOP)
      IF (AACH . LI. MVECTM (1) ) M=MVECTM (1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        IP (VRT . LI. 1.D-5) GO TO 1000
                                                                                                                                                                                                                                                                                                                                  ANGLIT=ITANGL*57.2957795100
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         IP (MACH .GI. 1.) GO TO 800
                                                                                                                           IF (NSTOP . LT. 3) STOP 73
                                                                          IF (NSTOP . LT. 3) STOP 60
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               CY=CYBETA*BETAT+CYO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                STMAR = (XCP-XCG) /DIA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      CN=CNA * ALPHAT+CNO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                CLNU=544.88286D0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            L1= (F1+F2) *. 331
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         CHA=STRAB*CZA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     FA (1) =- 05 * CD
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            PA (3) =- US*CN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          NU=.00541D0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            FA (2) = US*CY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       MA (2) = 0... DU
MA (3) = 0... DU
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     MA (1) = 0. DO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            GO TO 1100
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  MA (1) = 0.00
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                GO TO 300
                                                                                                                                                                                                                                                                                                                                                                                                                                                                              BE FOUND.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                XCP=L-L1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           XXCP=XCP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               T0=0"D0
                                                                                                                                                                           12([3]))
                                                                                                                                                                                                                                                                                      ITANGL.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             RETURN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      1100
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      300
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  1000
                                                                                                                                                                                                                                                   000
                                                                                                                                                                                                    د ر.
                                                                                                                                                                                                                                                                                                                                                                                                          00000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             0000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         WITH THE VALUES POR MACH NUMBER AND ERZ FOUND ABOVE,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                NOW GO TO THE PI MATRIX (THE TABLE OF VALUES FOR PI VERSUS MACH NO. AND BR2) AND INTERPOLATE TO FIND PI.
                                                                                                                                                                                                                                 IF (ITANSE .GI. .0698132)GO TO 100
CALL INFERP (1ACH.CNA, MACSVC, CNAVCI, 27, NSTOP)
IF (MSFOP .LI. 0) STOP 10
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             IP (NSTOP .LT. 0) STOP 30
CALL INTERP (4ACH, CNO, MACHYC, CNOVEC, 27, NSTOP)
IP (NSTOP .LT. 0) STOP 40
                                                                                                                                                                                                                                                                                                                                                               CALE INTEFE (AACH, CNA, MACHYC, CNAYCZ, 27, HSTOP)
IF (NSTOP - LE. 9) SFOP 20
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CALL INTEAP (EMXCG,CMQ,XVEC,CMQVC1,3,NSTOP)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CALL INTERP (LMXCG, CMQ, XVEC, CM, VC2, 3, NSTOF)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          CALL INTERP (MACH, CD, MACHVC, CDVEC, 27, NSTOP)
                                               CONSTRUCTOR ( (X (7) + UGUST) + 42+ (H+HGUST) ++1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 IF (TIME .LT. 0.8) LB=0.DO
IF (TIME .GI. 2.5) LB=163.DO
CALL INTE3P (LR, BR2, LRVEC, BRVFC1, 22, MSTUP)
                                                                                                                                            I TANGL = DSQAT (DZTAT * HETAT + AEPHAT * ALKHAT)
                                                                                                                                                                                         INTERPOLATE FUR CNA, XCP, CNO, AND LD.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  IF (LAKCG . LT. XVEC(1)) LAKCG = (VEC(1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       IP(LMXCG - GT. XVEC(3))LMXCG=KVEC(3)
IP(FIME - GE. - 5DO)GG TO 300
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     IF (ITANGL .LE. . C698132) CNO=U. DO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             (BRVEC2(I) .GT. BR2) GO TO 600
                                                                    3ETAT=0ATAN2 (VI, CONST)
ALFDEG=ALFGAT*57.29577951D0
BETDEG=BETAT*57.29577951D0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                IP (NSTOP .LT. 3) STOP 50
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  VECTR1 (J) = FIMAR (IM1, J)
25=0.5 * RHU * VAI * VRI*S
                  ALPHAI = DAFANZ (4T,UE)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 LR=58.8235* (TIME-.8)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             VECTR2 (J) = P1MAT (I,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        DO 500 I=1,10
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          DO 704 3=1,6
                                                                                                                                                                                                                                                                                                                                                                                                                                                          CYBETA = - CNA
                                                                                                                                                                                                                                                                                                               007 01 00
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               GO TO +00
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             HUNITAGE
                                                                                                                                                                                                                                                                                                                                    CONFINUE
                                                                                                                                                                                                                                                                                                                                                                                                            CONTINCO
                                                                                                                                                                                                                                                                                                                                                                                                                                     CZA =- CNA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            CYU =- CNO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      CNR = CRC
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       1-1=1 KI
```

100

000

230

300 400 **M=MACH**

7 00

200 009

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IF CNTR CH IS TRUE, SKIP THE SECTION TO COMPUTE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ADIES AUX1 .OR. AUX2 .OR. AUX3 .OR. AUX4
IF (AUX5) GO TO 4C0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                          AJX2=PHIPD .GT. CONST .AND. PHIPD .LT.
AJX3=PHIPD .GT. PI .AND. PHIPD .LT. A3
                                                                                                                                                                                                                                                                                                                                                                                                                                   AUX1=PHIPD .GT. 0. .AND. PHIPD .LT. A1
CONST=.5*PI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ANAC=-K2/K1*YG-K3/K1*YGDOT
                                                                                                                                                                                     IF (TIME .LT. TBC) GO TO 400
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             UNRC=K2/K1*ZG+K3/K1*ZGDOF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            IF (J . GT. DMAX) GO TO 103
                                                                               IF (CHIR CN) GO TO 300
                                                                                                                                                                                                                                                                                                                                                                                            13=.5+(3. +PI-ANGMAX)
                                                                                                                                                                                                                                                                                        POSSIBLE THIS STEP.
                                                                                                                                                                                                                                                                                                                                                                                                               A4=IHOPI-.5*ANGMAX
                                                                                                                                                                                                                                                                                                                               NNGMAX = TMAX * OMEGA
                                                                                                                                                                                                                                                                                                                                               A1=.5* (PI-ANGHAX)
                                          DELTY AND DELTZ
                                                                                                                                                                                                                                                                                                                                                                      12=PI-.5*ANGMAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        IF (DABS (RNHC)
GO TO 200
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   CONST×1.5*PI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    00
                                                                                                                                                               J
                                                                                                                                                                                                        000000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   0000000000000
0000
                       IMPLICIT REAL® (A-H,M,U-Z)
LUGICAL CNTR ON,AUX1,AUX2,AUX3,AUX4,AUX5
LUGICAL CNTR ON,AUX1,AUX2,AUX3,AUX4,AUX5
REAL® IT, IS,LI,K1,K2,K3,NUMB,JDCOEP,K20,K30
DIMENSION FC (3), HC (3), X (13), XDUF (13)
COMMON/COMSU/PCMAK,DELTA,GRAV,CMA,CZA,CMU,UDOT,DIA,KHU
15,II,IS,LI,JDCUEF,TMAK,TDELAY,MAKBAI,TBGOSI,THC
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    SET THE AXIAL PORCE AND THE ROLLING MUMENT DUE TO THE CENTROL DEFLECTORS EQUAL TO ZENO, SINCE THE DESIGN OF THE DEFLECTORS DUES NOT ALLOW FOR EITHER OF
                                                                                                                                                                                                              CJANJON/COM 170/ZG,YG,ZGDOI,YGDOT
COGNON/CON 180/XG(3),VG(3),DEGDEL,DEGLAM,ÇMR,RNR
COMMON/COM 190/DELTY,DELTZ,ANGY,ANGZ,PHIPD,SGN,FCYNR,
1FCZNR,MCYNR,NCZNR,K1,K2,K3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               IF (TIME .ST. IBUGST) KZ=K20*TBC/TBCUSI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 IP (TIME _GT_ TBOOST) KJ=K30*TBC/TBOOST
                                                                                                                                                                                                                                                                                               CCHHON/COM200/D, DMAX
COMMON/COM210/2NRC,RNRC,DLTX,DLTZ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        IF (TIME . LE. IBC) CNTR ON=.FALSE.
       SUBMOUTINE CONTRI (TIME, X, XDO!)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 JNB=2 * DCOS (PHI) - B * DSIN (PHI)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      HAREQ*DSIN (PHI) +R*ECUS (PHI)
                                                                                                                                                                        COMMON/COM80/XK1, K20, K30
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               PHIPD=DACO (PHIPD, TWOPI)
                                                                                                                                                                                                                                                                                                                                        SIGH (X) = DSIGN (1. DO. X)
                                                                                                                                                                                              COMMON/COM 160/PC. NC
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        TDEL2=2.D0*TDELAY
                                                                                                                                                                                                                                                                                                                                                                               PI=3.141592654D0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               PHIPD=K (4) +DELTA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          PHESE REACTIONS.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           K2=K20*TBC/TIME
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             K3=K30 * TBC/TIME
                                                                                                                                                                                                                                                                                                                                                                                                     TWOPI=2.D0*PI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ONEGA=X (10)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    AC (1) = 0. DO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   PC (1) = 0. DJ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                 MASS=X (13)
                                                                                                                                                                                                                                                                                                                                                                                                                            PHI = X (4)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             0=x (11)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               R=X (12)
                                                                                                                                                                                                                                                                                                                                                               K 1=XK 1
                                                                                                                                                                                                                                                                                                                                                                                                                                               U=X (7)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        CONTRO
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```
CHECK AND SEE IF WE HAVE ALREADY CONTROLLED DURING THIS CONTROL PERIOD. IP SO, CONTROL IS NOT PUSSIBLE. IF NOT, CHECK TO SEE IF CONTROL IS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      COMPUTE DELTA T, THE TIME INCREMENT POR THE THRUST DEFLECTORS TO REMAIN ENGAGED, FOR BOTH THE LONGITIONAL AND LATERAL EQUATIONS.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       IF THE TALL OF THE MISSILE IS OUTSIDE THE TRACKER
JEAN CONE, NO GUIDANCE COMMANDS ARE SENT, SO ONLY
RATE STABILIZATION COMMANDS ARE POSSIBLE
(I.S. -- COMMANDED PITCH AND YAW RATES ARE ZERO).
IF TIME IS LESS THAN THE TIME OF SUSTAINER MOTOR ISNITICN, CCNTROL IS NOT POSSIBLE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   IF (DABS (JARC) ...GT. MAXHAT) JARC=MAXRAT*SIGN (JARC)
IF (DABS (RNEC) ...GT. MAXRAT) RNEC=MAXHAT*SIGN (KNRC)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       A2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  AUX4=PHIPD .GT. CONST .AND. PHIPD .LT. A4
```

CALL TRACKER ROUTINE TO ALCEIVE TELEMETRY COMMANDS

CALL TRACKR (TIME, X, XDOT, 2)

200 COAPINGE JNRC=0. RNRC=0.

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COMPUTE CONTROL FORCES AND MOMENTS IN ROLLING AXES
                                                                                                                                                                                                                                               IP (DABS (SGN) .LT. 1.D-6) .GN=DABS (DELTZ) /DELTZ
TOUT=TIN+DABS (DELTZ)
IP (TIME .ST. T2) CONST=1./fbebay* (TOUT-TIME)
                                                                                                                                                                                                                                                                                                                                                             IF (TIME .LT. I) CONST=1./IDELAY* (TIME-IIN)
IP (TIME .GT. T2) CONST=1./IDELAY* (TOUT-TIME)
                                                                                                                                                                                                              IP(DABS(DELIZ) .LT. TDELZ)GO TO 500 3GN=SIGN(DELIZ)*SIGN(DELIZ)
                   PCNTRL=PCMAX*CONST
PCYNR=-PCNTRL*HSIN (PHIPD) *5GN
PCZNB=+PCNTRL*bCOS (PHIPD) *5GN
                                                                                                                                                                                                                                                                                                                                                                                                                    PCYNR=-FCNTBL*SGN*DSIN (PHIPD)
FCZNR=+FCNTRL*SGN*DCOS (PHIPD)
                                                                                                                                                                                                                                                                                                                                             IF (TDELAY . LE. 0.) GO TO 900
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  FC(2) = FCYNR*CP+FCZNR*SP
FC(3) = - FCYNR*SP+FCZNR*CP
                                                                                                                                                                                                                                                                                                                                                                                                   FCNTRL=FCMAX *CCNST
                                                                             CATE ON - TRUE.
                                                                                                                                                                                                                                                                                                                                                                                                                                                             CNTR ON = . TRUE.
                                                                                                                                                                        LATERAL CCNTRUL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  MCZNR=-LT*FCYNR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            MC (3) =-LI*FC (2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                MCYNR=LT*FCZNR
                                                                                                                                                                                                                                                                                                        T2=TOUT-TDELAY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          MC (2) =LT*FC (3)
                                                                                                                                                                                                                                                                                      T1=IIN+IDELAY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            CP=DCOS (PHI)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              SP=DSIN (PHI)
                                                                                                                5LTZ=0.
                                                                                                                                                                                                                                                                                                                           CONST= 1. DO
                                                                                              DLTY=DELTY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                               DLTZ=DELTZ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   DT FY=0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             BETURN
                                                                                                                                                                                                              300
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            1000
                       700
                                                                                                                                                                                                                                                                                                                                                                                                       900
                                                                                                                                                         Ü
                                                                                                                                                                         ر, ر,
                                                                                                                CHACK TO SEE IF THE MISSILE IS IN THE CORRECT ROLL AFFITUDE FOR LONGITUDINAL OR LAFERAL CONTROL.
                                                                                                                                                                                                                                                                                                                                                                               IP (ABSPPD .GE. BH .OR. ABSPPD .LE. AA) GO TO 600
IF (ABSPPD .GE. CC .AND. ABSPPD .LE. DD) GO TO 800
                                                                                                                                                                                                                                                                                      IP (JABS (DELIY) . LT. TDELZ . AND. DAUS (DELIZ) . LT.
                                                         IP(DABS(DELTY) .G1. TMAX) DELTY=IMAX*SIGN(DELTY) IP(DABS(DELTZ) .GT. TMAX) DELTZ=IMAX*SIGN(DELTZ)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   IP(DABS(DELTY) .LF. TDEL2)GO TO 500
SGN=SIGN(DELTY)*SIGN(DCOS(PHIPD))
IP(DABS(SGN) .LT. 1.D-6)SGN=DABS(DELTY)/DELTY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  IF (TDELAY LE. 0.) GO TO 700
IF (TIME .LI. T1) CONST=1./FDELAX* (TIME-TIN)
                                                                                                                                                                                                                                                                                                                                             IP(PHIPD - GT. PI)PHIPD=PHIPD-THOPI
AssPPD=DABS(PHIPD)
                                                                                                                                                                        ANGY=DASS (CMEGA*DE, TY)
ANGZ=DABS (CMEGA*DELTZ)
                                                                                                                                                                                                                                                                                                                                                                                                                                           NO CONTROL THIS STEP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 LONGITUDIAAL CONTRUL
                OSLEZ=-K1* (RNR-BNRC)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          FOUR-TIN+DABS (DELTY)
                                                                                                                                                                                                                                                                                                        TEDELEJ GO TO SOU
                                                                                                                                                                                                                                                  CC=. 5* (PI-ANG2)
                                                                                                                                                                                                                                                                   DD=.5. (PI+ANGZ)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              T2= FOUT-TDELAY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             T1=TIN+TDELAY
                                                                                                                                                                                                            AA=ANGY . 500
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  CONST = 1.DO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           GO TO 1000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CNTR ON =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                             30 70 450
                                         PRILERIA
                                                                                                                                                                                                                                  3B=PI-AA
                                                                                                                                                                                                                                                                                                                           COMPINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      DELTZ=0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                PARCEO.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  DELTY=0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                PCYNS=0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  PCZNR=0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        DLTY=0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          AMGY=0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        DL F 2=0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ANGZ=0.
                                                                                                                                                                                                                                                                                                                            300
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      450
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              500
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     009
                                                                                              0000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ပပပ
                                                                                                                                                                                                                                                                                                                                                                                                                       ひりひ
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COMPUTE THE LOCATION OF THE MISSILE'S TAIL IN THE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             RDOT= (XG(1) *VG(1) +XG(2) *VG(2) +XG(3) *VG(3))/R
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       d=DS_dET (XG (1) *KG (1) + KG (2) *XG (2) + KG (3) *XG (3))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 DMAX=XVEC(1) *DTAN (TBEAM)

IP (XVEC(1) .LI. 0.) DMAX=0.

D=DSQRI (XVEC(2) *XVEC(3) *XVEC(3))
                                                                                                                                                                                                                                                     CALL CHAI (V.LGV, LVG, S3, C3, 52, C2, 51, C1)
CALL HATXV (LGV, VV, XG)
CALL HATXV (LGV, VV, VG)
CALL TILDE (XVEC, XMAT)
CALL TILDE (XYEC, XMAT)
DO 400 I=1,3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               CALL CHAT (V, LBV, LVB, S3,C3,S2,C2,S1,C1)
CALL MATXV (LVB, XVLC, XVEC2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     XVEC(3) = XVEC(3) - ZMEF
CALL VAD(XVEC, XVEC3, XVEC3)
CALL MATXV (LGV, XVEC3, XVEC)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               XVEC (2) = XVEC (2) - YREF
XV (3) = X (3) - 23 E?
VV (1) = XDOT (1) - VAEFX
VV (2) = XDOT (2) - VREFY
VV (3) = XDOT (3) - VAEF2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      XVEC (1) = XVEC (1) - XREP
                                                                                                                                                                                                                                                                                                                                                                                                                 VG(L) = VG(L) - KVEC(L)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         GUNIOMETER SYSTEM.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              X VEC (1) =XCG-XL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   50 500 I=1,3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           XVEC(I) = X(I)
                                                                                                                                 V (2) =DELTAG
                                                                                                                                                          V (3) = LAMDAG
                                                                                                                                                                                                           V (S) =DELTAG
                                                                                                                                                                                                                                   V (6) = LAMDAG
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  (3DOT=VG(2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           (1) 5A = LOG 52
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ZGDT=ZGDOT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            TLAST = TIME
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       AVEC (2) =0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             XVEC (3) =0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    YGDT = YGDOT
                                                                                                      V(1) = 0.00
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        (t) X=(t) A
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   V(5) = X(5)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           (9) x = (9) A
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     DAX = DRAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               3=XG (2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            (C) (3)
                                                                                                                                                                                  V (4) =0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      52=522
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              YY G= YG
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     RETURN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             Q=CQ
                                                                                                                                                                                                                                                                                                                                                                                                                    007
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                500
                                                                                                                                                                                                                                                                                                                                                                                                                                            0000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CONST=1.D0/DSGRT (1.D0- (XTV (3) / RHGG) **2)
RAUGDT= (XTV (1) *VTV (1) *XTV (2) *VTV (2) *XTV (3) )/BHGG
DZL.DT=CUNST* [-VTV (3) / RHGG*XTV (3) *KHUCDT/RHGG/KHG5)
CONST=1.D0/ (1.D0+ (XTV (2) / XTV (1)) **2)
GLASDT=CONST* (VTV (2) / XTV (1) ) **2)
                                                                                                               DIMENSIUN X(13) «XDOT (13) «V(24) «XV(3) «VV(4) «XTG (3) »

1VTG (3) "LGV (3,3) "LVG (3,3) "XVEC (3) "XMAT (3,3) "LBV (3,3)

2) "LVB (3,3) "XVEC2 (3) "XVEC3 (3)

EXLAB (3,2) "XVEC2 (3) "XVEC3 (3)

COMMON/COMPOUND ACH ALPHA, BETA, XI, SAHEA, HO, DIA, TEMP, XCG

COMMON/COMPOUND TO, TO, TP, HIN
                                                                                                                                                                                                                                                                                                  COMMON/COM70/DELTAG, LAMDAG, DELGDT, GLAMDT, XTV (3), VTV (3)
COMMON/COM170/2G, YG, ZGDOT, YGDOT
COMMON/COM180/XG (3), VG (3), DEGDEL, DEGLAM, QNR, RNR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                BHOG=DSURT (XTV (1) *XTV (1) +XTV (2) *XTV (2) +XTV (3) *XTV (3))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       FRANSFURM THE POSITION AND VELOCITY OF THE MISSILE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 COMPUTE THE EULER ANGLES OF THE GCNIOMETER SYSTEM
                                                                                                                                                                                                                                                                                                                                                                                                      COMMON/COM220/A, RDOT, ZZG, YYG, ZGDT, YGDT, D, DHAX
IF (TIME . LE. TO) GO TO 200
DO 100 I=1,3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    PROM THE INERTIAL TO THE GONLORETER SYSTEM
                                            SUBROUTINE TRACKR (TIME, X, XDUT, TRODE)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  XTV(I) = XTV(I) + VTV(I) + (TIME-TLAST)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   VREPY=-PTUR*DCOS (LAMBAG) * LAMB E
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          VREPX=BTUR #DSIN (LAMDAG) #GLAMDT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               LAMDAG=DATAN2 (XTV (2), XTV (1))
DEGDEL=DELTAG+57_29577951D0
DEGLAM=LAMDAG+57_29577951D0
                                                                  IMPLICIT REAL *8 (A-H, M, O-Z)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         DELTAG=DABSIN (-XTV (3) /RHOG)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               XREF = - RTUR * DCOS (LAMDAG)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       YREF=-ATUR*DSIN (LAMDAG)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        IF (THODE . LT. 1) RETURN
                                                                                                                                                                                                                                                                                                                                                                              COMMON/COM250/DD, DMX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    XV (1) = X (1) - XREP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               XV (2) = X (2) -Y3EF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                XVEC (2) = DELGDT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        XVEC (3) =GLABOT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ZREP=-HANT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       XVEC (1) =0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             GO TO 300
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        TLAST=70
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              VREFZ=0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         300
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    100
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   200
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SUBPOUTING BRAT (V. D. BI, COJALI, DIKALI, COSALZ, SINALZ,
                                        DIMENSION B(3, 3), 5T (3, 3), V(24)
DIMENSION B1(3, 3), B2(3, 3), B3(3, 3), Td1(3, 3)
                             IMPLICIT REALS (A-8,0-2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             DIMENSION A (3, 3), B (3, 3),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   SUBROUTINE MSUB(A, B, D)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               DOUBLE PRECISION A.B.
                                                                                                                                                                                                                                                                                                                                                                                                                                      CALL MATMPY (03, 82, IN1)
                                                                                                                                                                                                                                                                                                                                                                                                                                              CALL MATMPY (B1,TM1,5)
CALL TRANSP (B,BI,3,3)
RETURN
                                                                 DO 106 II = 1,3

DO 106 JJ = 1,3

B1(II,JJ) = 0.0D0

32(II,JJ) = 0.0D0

COSAL1 = DCOS(V(1))

SINAL1 = DCOS(V(1))

SINAL2 = DCOS(V(2))

SINAL2 = DCOS(V(2))

SINAL2 = DCOS(V(3))

SINAL3 = DSIN(V(2))
                                                                                                                                                                                                                       B1(1,1) = 1.000
B1(2,2) = COSAL1
B1(2,3) = COSAL1
B1(3,2) = SINAL1
B2(2,4) = SINAL1
B2(1,1) = COSAL2
B2(1,1) = COSAL2
B2(1,3) = COSAL2
B2(1,3) = COSAL2
B2(1,3) = SINAL2
B3(1,3) = SINAL3
B3(1,2) = SINAL3
B3(2,1) = SINAL3
                                                                                                                                                                                                                                                                                                                                         = -SINAL2
                                                                                                                                                                                                                                                                                                                                                      SINAL2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       D(I,J) = 0.000
D(I,J) = A(I,J)
RETURN
                                                                                                                                                                                                                                                                                                                                                                                                                        = 1. JD0
              COSALS, SINALS)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              DO 5 I = 1,3
DO 5 J = 1,3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           J = 1,3
                                                                                                                                                                                                                                                                                                                                                                                                                       B3 (3, 3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       S
                                                                                                                            100
                                                                                                                                                                                                                                                                   IF (A . L.T. C(1) . UR. A . G.T. C(N)) GO TO 3CO BO 100 I=1,N
                                                                                 IP (A. 1E.C (1) . AND. A. LE.C (I+1)) 30 TO 200
SUBROUTINE INTERP (A, B, C, D, N, NSLUP)
               IMPLICIT REALMS (A-H,U-Z)
DIMENSION C(N),D(N)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 REAL+8 X,XT
DIMENSION X(3),XT(3,3)
                                                                                                                                                                                                                                                                                                                                                                                                  SOU PRINT 400, A.NSFOP, C(1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   SUBROUTINE FILDE (X,XT)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            -x (2)
                                                                                                                                                                                                                X4=Y2*X3/X2
                                                                                                                 X=C(I)
X}=C(I+1)
Y=D(I)
                                                                                                                                                                                                                                                                                                                                                                                   GO TO 630
                                                                                                                                                                                                                                                         33 33 B3U
                                                                                                                                                         (1+1) C=1 A
                                                                                                                                                                                                                                                                                                                                                                                                              NSTOP=-1
                                                                                                                                                                                                                                                                                                                                                                       NS 70P=-1
                                                                                                                                                                                                                               1 1= Y 1- X 4
                                                                                                                                                                                                                                                                                                                                                                                                                             CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        XT (3, 1)
                                                                                                   SUNTINCO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       XT(3,2)
                                           NSTOP=1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        XT (1,3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     XF(1,2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                XI (2,1)
                                                                                                                                                                        X-1 X=7 Y
                                                                                                                                                                                    ¥2= ¥1- ¥
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             XT (2,3)
                                                                                                                                                                                                   X 3 = X 1 - A
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    XT (1, 3)
                                                                                                                                                                                                                                                                                                                                                                                                                                          RETURN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            30 5
30 5
                                                                                                                                                                                                                                            i γ = εί
                                                                                                                                                                                                                                                                                                    000
                                                                                                                                                                                                                                                                                                                                                                                                                             009
                                                                                                   100
                                                                                                                 200
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DIMENSION C (3,3), CT (3,3), V (24), TM1 (3,3), TA2 (3,3)
SUBROULINE CNAT (V, C, CT, SPSI, CPSI, SPHEIN, CLHEIN,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      DIMENSICN A (NAA, NCA), B (NCA, NRA)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       SUBROUTINE TRANSP (A, B, NRA, NCA)
                                   INPLICIT REAL®S (A-H, U-Z)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   CALL MATMPY (TM2, TM3, TM4)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CALL MATHPY (TM1, TH4, C)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           DOUBLE PRECISION A, B
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               CALL TRANSP (C,CT,3,3)
RETURN
                                                                                                                                                                                                         STETA=DSIN(V(S))
CTHETA = DCOS(V(S))
SPHI = DSIN(V(4))
CPHI = DCOS(V(4))
IN1(1,1) = 1.0D0
IN1(2,2) = CPHI
                                                                                                                   TAZ (II,JJ) = 0.050
TAT (II,JJ) = 0.000
TAT (II,JJ) = 0.000
SPSI = DSIN (V(6))
CPSI = DCOS (V(6))
                                                                                      100 II = 1,3
100 JJ = 1,3
                                                                                                                                                                                                                                                                                                                                                                                                                           = CIHETA
                                                                                                                                                                                                                                                                                                                                                                                                                                            = STHETA
                                                                   TN3 (3, 3), TN4 (3,3)
                                                                                                                                                                                                                                                                                                                                                                        = CTHETA
                                                                                                                                                                                                                                                                                                                                                                                           =-STHETA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    = 1.000
                                                                                                                                                                                                                                                                                                                                                                                                            = 1.000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 SPSI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               = -SPSI
                                                                                                                                                                                                                                                                                                                     = SPHI
=-SPHI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           J = 1, NCA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              = 1,NCA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                = CPSI
                                                                                                                                                                                                                                                                                                                                                         = CPHI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   = CPSI
                  SPHI, CPHI)
                                                                                                                                                                                                                                                                                                                                                                                                                                           TM2 (3,1)
TM3 (1,1)
TM3 (1,2)
TM3 (2,1)
                                                                                                                                                                                                                                                                                                                       (5,3)
                                                                                                                                                                                                                                                                                                                                                                                                                             (3, 3)
                                                                                                                                                                                                                                                                                                                                      IN1 (3, 2)
                                                                                                                                                                                                                                                                                                                                                       191 (3, 3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   IN3 (2,2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  TH3 (3,3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                B(J,I)
RETURN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               В (Л, І
                                                                                                                                                                                                                                                                                                                                                                                                                           T82(
                                                                                                                                                                                                                                                                                                                     TAL
                                                                                                                                                                                                                                                                                                                                                                        TH2 (
                                                                                                                                                                                                                                                                                                                                                                                         TM 2 (
                                                                                                                                                                                                                                                                                                                                                                                                          TM2
                                                                                                                                                           100
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                S
                                                                                    D=A(1,1)*(A(2,2)*A(3,3)-A(3,2)*A(2,3))+A(1,2)*(A(3,1)
1*A(2,3)-A(2,1)*A(3,3))+A(1,3)*(A(2,1)*A(3,2)-A(3,1)
2*A(2,2))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     IP (FIME .GE. T(I) .AND. TIME .LE. F(I+1)) GO TO 200
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        100 CONTINUE
200 FORCE=F(I+1)-{([(I+1)-TIME)/([(I+1)-T(I)))*(F(I+1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   IP (TIME .LT. T(1) .OK. TIME .GI. I(N)) GO TO 300
                                                                                                                                                                                                                                              = (A(3,1) *A(2,3) - A(2,1) *A(3,1) / D

= (A(1,1) *A(3,3) - A(3,1) *A(1,3) / D

= (A(2,1) *A(1,3) - A(1,1) *A(2,3) / D

= (A(2,1) *A(3,2) - A(3,1) *A(2,2) / D

= (A(3,1) *A(1,2) - A(1,1) *A(3,2) / D

= (A(1,1) *A(2,2) - A(2,1) *A(1,2) / D
                                                                                                                                                                      IP (ABSD _LT, 1.5-05) GO TO 100
B(1,1) = (A(2,2)*A(3,3)-A(3,2)*A(2,3))/D
B(1,2) = (A(3,2)*A(1,3)-A(1,2)*A(3,3))/D
B(1,3) = (A(1,2)*A(2,3)-A(2,2)*A(1,3))/D
                                                                                                                                                                                                                                                                                                                                                                                                    PORMAT (1H1,5X, THE MATRIX IS SINGULAR!)
CONTINUE
                                     DOUBLE PRECISION A, J.DEF, D, DABS, AUSD
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                SUBMOUTINE THRUST (TIME, FORCE, T, F, N) DOUBLE PRECISION TIME, FORCE, I, P
 SUBROUTING MATINY (A, B, DET)
                    DIMENSION A (3, 3), A (3, 3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  DIAENSION F(50), T(50)
                                                                  DO 5 J = 1,3
B(I,J) = J.JD0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   DO 100 I=1,N
                                                                                                                                                                                                                                                                                                                                                                                            WRITE (6, 1000)
                                                                                                                                                             ABSD=DABS (D)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             FORCE=0.DO
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            GO TO 400
                                                                                                                                                                                                                                                                                                                                                                           GO TO 999
                                                                                                                                                                                                                                                                                                    a(3,1) = a(3,2) = B(3,3) = DET = D
                                                                                                                                                                                                                                                8 (2,1)
8 (2,2)
8 (2,3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               REFURN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           1-P(I))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             000
                                                                                                                                                                                                                                                                                                                                                                                           100
                                                                                                                                                                                                                                                                                                                                                                                                                              449
```

Ì

+ A (1,3) *V (3) + A (2,3) *V (3) + A (3,3) *V (3)

```
HEAL*H A, J, V

DINDNOIDN A(3,3), V(3), J(3)

J(1) = A(1,1)*V(1) + A(1,2)*V(2) +

J(2) = A(2,1)*V(1) + A(2,2)*V(2) +

U(3) = A(3,1)*V(1) + A(3,2)*V(2) +

RETURN
                                                                                                                                                                                 C, CCN37
C (3,3)
                                                                                                                                                                SUBROUTINE CXMAT (A,C,CONST)
DOULLE PRECISICN A, C,CCNS
DIMENSION A(3,3), C(3,
  (U'A'A) NAIXA SAIJBORGE
                                                                                                                                                                                                                DO 5 I = 1,3

DO 5 J = 1,3

C(I,J) = 0.0D0

5 C(I,J) = CCNST*A(I,J)

METURN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  SUBRUCTINE VAD(X,Y,DVEC)
DOUBLE PRECISION X,Y, DVEC
DIMBRICN X(3),Y (3), DVEC(3)
DO 5 I = 1,3
DVEC(1) = 0,000
5 DVEC(1) = X(I) + Y(I)
RETURN
                                                                                                                                                                                                                                                                                                                                                                                     DVEC (3)
                                                                                                                                                                                                                            C(I,J) = 3.0

DO 10 K = 1,3

REIUEN = C(I,J) + A(I,K) +3(K,J)

END
                                                                                                                                                        SUBROUTINE MATAPY (A, B, C)
REAL*4 A, B, C
DIMENSION A (3, 3), B (3, 3), C (3, 3)
DO 10 I = 1, 3
DO 10 J = 1, 3
                                                                                                                                                                                                                                                                                                                                             SUBRUTINE VSJE(X,Y,DVEC)

DOUGLE PRECISION X,Y, DVEC

DIMENSICN X(3), Y (3), DVEC (0)

S I = 1,3

DVEC (1) = 0.0D0

RETURN
SUBROUTING C(WEC(X,Z,CUNSF)
DAUGLE PRECISION X, Z,CCNSF
DIMENSION X(3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            SUBROUTING MAD(A,B,D)
DOUBLE PRECISION A,B, D
DIMENSION A(3,3),D(3,3),
DO 5 I = 1,3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                D(I,J) = 0.0D0
D(I,J) = A(I,J) + B(I,J)
AZTURN
END
                                                                   Z(I) = 0.000

Z(I) = CCNST*X(I)

REFURN
                                                    00 5 1 = 1,3
                                                                                     'n
                                                                                                                                                                                                                                                                               ္
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APPENDIX B

LISTING OF SIMPLIFIED MISSILE LAUNCHER

(MISSLNCH) SIMULATION PROGRAM.

On the following pages is a listing of the missile launcher (MISSLNCH) computer program. MISSLNCH is used to simulate the missile dynamics during the launch phase of the analysis in order to obtain initial conditions for the flight phase simulation (MISSIM) program. The computer code developed is compatible with the FORTRAN G, FORTRAN H, and WATFIV compilers used in conjunction with the IBM 370/158 digital computer available at Auburn University. All computations in the program use double precision arithmetic.

All input into the program is accomplished by punched cards. Each card contains ten data fields which are eight columns wide. A generalized (G) field descriptor is used in the format for all read statements. This format was chosen for simplicity, since it allows integer, logical, or real (external fixed point or floating point) variables to be read with the same format. The entire input necessary to use MISSLNCH is read in the main program and is explained below.

IS Spin-axis moment of inertia $(kg-m^2)$.

IT Transverse-axis moment of inertia (kg-m²).

THETAT Elevation (or pitch) angle of launch tube (rad).

OMEGAT Steady angular velocity of launch turret measured about vertical axis (rad/sec).

XA,YA X and Y components, respectively (measured in the turret reference system), of any point fixed within the launch tube relative to a point on the turret axis of rotation (m).

DIA Missile largest diameter (m).

MASSR Missile mass (kg).

GRAV Magnitude of gravity (m/\sec^2) .

FT Steady thrust magnitude which acts on missile (Nt).

TX Spin torque applied to missile during launch (Nt-m).

XETO The distance from any point fixed within the launch tube to the missile center of mass when tipoff has ended (m).

TODIST The distance that the missile travels during the tipoff interval (m).

XGT,ZGT The X and Z components, respectively (measured in the tube reference system), of point G, the center of the infrared angle sensor (m).

X The vector of initial conditions of the state variables.

PRMT(1) Time at the beginning of the simulation (sec).

PRMT(2) Time at the end of the simulation (sec).

PRMT(3) The maximum allowed integration step size (sec).

PRMT(4) An upper error round to test for convergence in the integration algorithm.

ERROR A vector containing error weights of the state variables.

Is used to test for convergence in the integration algorithm
(The sum of the components must equal 1).

Since this computer program is to be used only during the short time during the launch phase, the missile physical model is considerably more simple than that used in the flight phase. During the launch phase, the missile is modeled as a rigid, constant mass body with constant moments of inertia, which is acted upon by a constant thrust and initial spin torque. In addition, the MISSINCH program which follows is also a simple mathemathcal model of the missile/launcher system, and does not contain the level of

generality, nor the inclusion of large numbers of comment cards to explain the sections of the program that was evident in the MISSIM program of Appendix A. If a more complex missile/launcher model is desired, the reader is directed to Ref. 2 for a listing of the more complicated mathematical model used during that study.

Some subroutines used in MISSLNCH are also used in MISSIM. In order to avoid repetition, their listings are presented only in Appendix A. The subroutines are TILDE, TRANSP, MATINV, MATMPY, MATXV, CXMAT, CXVEC, VAC, VSUB, MAD and MSUB.

```
READ 100, (PRAT(I),I=1,4), (ERROR(I),I=1,13)
CALL DAKGS (PRAT,K,Eraus,13,IHLE, FUNC,OUTPUT,AUX)
IF(IHLE,LE, 10) STOP
PRINT 300,IHLF
FORNAT(1H,//,5X,'LHLF=',12)
STOP
                                                                                                                                                                                                                                                                                                                                                                              SUBROUTINE VECTOR (A, B, M)
REAL+8 A (13), B (3)
DO 100 I=1,3
O 3(I) = A (I+N)
END
END
                                                                                                                                                                                                                                                                                                                                                                                                                                            100
                                                                                           300
 IMPLICIT REALES (A-H,O-Z)

EXTEBNAL PURC,OUTPUT

BEALE IR, L, IS, IT, LE, ASST

COMFON(COM)/IR (3, 3), ASTT (3, 3), CMEGTT (3), E23 (3, 3), E7

1 (3, 3), ANT (3), D. T. S. (3), PTR (3), FLT (3), ANT (3, 3), C

2 (3, 3), ANT (3), ERROR (13), PTR (3), FLT (3), ANT (3, 3), C

2 (3, 3), ANT (3), ERROR (13), PRRT (5), ANX (8, 13)

READ 100, IS, IT, THETAT, OHEGAT, XA, YA, DIA, LE, MASSB, GBAV, PTR (1068-0)

100 FORMAT (1068-0)

XBTO-1, UD)+LE-TODIST

DO 200 I=1,3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        IR (2, 2) = IT

IR (2, 2) = IT

IR (3, 3) = IT

CTHETT = DCOS (INSTAT)

SIGETT = DSIN (THETAT)

ASTT (1, 1) = CTHETT

ASIT (2, 2) = 1,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ASTT(1, 3) =-STHETT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ASTT (3, 3) = CTHETE
ASTT (3, 1) = STHETT
OMEGIT (3) = CHEGAT
                                                                                                                                                                                                                                                                                                                               FIR(1) = 0.
ISR(1) = 0.
DT(1) = 0.
BGT(1) = 0.
DO 200 J= 1, 3
IR(1, J) = 0.
ASIC(1, J) = 0.
E23(1, J) = 0.
                                                                                                                                                                                                                                                                                        JAEGII (I) =0.
FRI (I) =0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         E1(I,J)=0.
ART (I,J)=0.
C(I,J)=0.
L(I,J)=0.
                                                                                                                                                                                                                                                                       RAT (I) =0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          200
```

```
XDOT(13)=PT/MASSH-GRAV*STHETT+XT*(OMEGAT*CTHZTT)**2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        EULER (1) = D4TAN2 (NAT1 (2, 3), MAT1 (3, 3)) *RAD
SULER (2) = DARSIN (-MAT1 (1, 3)) *RAD
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               EULER (3) = DATAM 2 (3AT1 (1,2), MAT1 (1,1)) * KAD
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   CALL MATMPY (AMT, ASTI, MATZ)
CALL MATMY (MATZ, UMEGIT, VECT)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                CALL MATHPY (ASTT, MAT1, MAT2)
CALL TANNSP (MAT2, MAT3, 3, 3)
CALL MATKY (MAT3, RG, VEC1)
                                                                                                                                                                                                                                                                       CALL MATXV (AST, VECT, VECZ)
CALL VECTOR(X, VECT, 0)
CALL VAD(VECT, VECZ, VECZ)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      CALL MAINPY (AHI, MAIZ, MAII)
                         IF (XI . 3E. X3FJ) GO TO 200
                                                                                                                                                                                                                                   IF (XT .LT. XETU) GO TO 800
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ANGRAT (1) = X (I+9) + VEC1(I)
CALL VECTOR (XDOT, VEC1,0)
CALL MATXV (ARI, VEC1, VEC3)
                                                                                                                                                                                                                                                       CALL VSUB (RAT, RGT, VECT)
                                                                                                                                                                                                                                                                                                                                                    R;(I)=VEC3(I)
RAD=57.29377951DU
PSIT=UMEGET(3)*TIME
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          A(1)=R(1)-.95*CP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              R(2) = R(2) - . 95*5P
                                                                                    JAEGAT = OMEGTE (3)
                                                                  XDOT (10) = TX/IS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  3 (3) =B (3) -4.5
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            3AT1(2,1)=-SP
                                                                                                                                                                                                                                                                                                                                                                                                                         CP = 0008 (PSIT)
                                             X301 (7) = X (10)
                                                                                                                                                                                                                                                                                                                                                                                                                                           (LISA) NISC=GS
                                                                                                                                                                                                                                                                                                                                      30 300 I=1,3
                                                                                                                                                                                                                                                                                                                                                                                                                                                               MA [1 (1, 1) = CP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     MAT 1 (2,2) = CP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        3A21 (1,2) = 5P
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                MAT1 (3,1)=0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    MAT1(1,3)=0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          AAT1(3,2) = 0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 30 430 I=1,3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             Do 500 I=1,3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        MAT1(2,3)=0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    R(I) = VEC1(I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              MATT (3,3) = 1.
                                                                                                                                                                       XDOT (11) = 0.

XDOT (12) = 0.
       37+(h) X=1)
                                                                                                                                XDOT (8) =0.
                                                                                                                                                   KDU F (9) =0.
                                                                                                                                                                                                               RETURN
                                                                                                                                                                                                                                     000
                                                                                                                                                                                                                                                                                                                                                            300
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    4.00
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  530
                   COMMON/COMM/IN (3, 3), ASTE (3, 3), OMEGIE (3), E23 (3, 3), ST 1 (3, 3), RATE (3), DE (3), FIRE (3), FRE (3), RATE (3), ARTE (3), C 2 (3, 3), LE (3, 3), LE, XBIO, XEIO, MASSK, GRAV, TX, FT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         PAT (1) =- AASSR#JRAV#STHETT+VEC2 (1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 FAT (3) =MASSR#JRAV#CIHETZ+VEC2 (3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ART (2, 1) =-X (5)
ART (2, 1) =-CPHI*X (9) +SPHI*X (8)
SISADULINE FUNC (TIME, X, XDOF)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            art (3, 1) = Sphi+x (9) +cpai+x (8)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   CALL TRANSP (ASTT, ATST, 3, 3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       CALL MATXV (MAT1, VEC1, VEC2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       CALL VECTOR(XDOT, VECT, 3)
CALL VAD(VECT, VEC2, VEC3)
CALL MAIXV(AIR, VEC3, VEC1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CALL MAIKY (ART, PTR, VEC2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               CALL TILDE (VEC1, MAT1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   CALL VECTOR(K, VEC1, 3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            CALL VECFOR(X, VEC1, 9)
                                                                                                                                                                                                                                                                                                                                                      C(1,2) = X(8) *SPHI
C(1,1) = X(3) *CPHI
C(2,2) = CPHI
C(2,3) = -SPHI
C(3,2) = -SPHI
                                                                                                                                                                                                                                                     STHERFASIT (3,1)
CRAETFASIT (1,1)
                                                                                                                                                                                                                                                                                             JPHI=DSIN (X(7))
                                                                                                                                                                                                                                                                                                                  CPHI = DCGS (X (7))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ART (3, 2) =- SPH1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 FR2 (2) = VEC 2 (2)
                                                                                                                          DIMENSION R (3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ARE (2, 2) =CPHE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ART (2, 3) =5PHI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  AAT (3, 3) = CPHI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              XDOF (4) =X (13)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ABT (1, 2) = X (9)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        30 100 I=1, 3
                                                                                                                                                                                                                                                                                                                                                                                                                                                               C(3,3) =CPHI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ART (1, 1) = 1.
                                                                                                                                                                                                          15=13(1,1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  (DOT (5) =0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        (DOT (4) =0.
                                                                                                                                                                                                                                   IT=IH (2,2)
                                                                                                                                                                                                                                                                                                                                      C(1,1)=1.
```

CALL PILDE (OMEGPE, MATT)

(1) = VEC 1 (1)

100

```
CALL MATXV (ART, OMEGTT, VEC1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             CALL CXVEC (VEC1, VEC2, CONST)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               CALL VECTOR(X, VEC2,3)
CALL TILDE(VEC2,MAT2)
CALL MATXV(MAT2,VEC1,VEC2)
                                                                                                                                                                                                                                                                                                                                           CALL MATXV (ATB, VEC1, VEC3)
CALL CXVEC (VEC3, VEC1, 2, D0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   CALL MATYY (MATZ, VEC2, VEC1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                CALL MATXV (MATZ, VECZ, VEC3)
CALL MATXV (ART, VEC3, VEC2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CALL MATXV (MATZ, VEC3, VEC2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              CALL MATMPY (ATR, MAT2, MAT1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      MATERY (E23, MAT1, MAT2)
                                                                                                                                                                                        CALL CXVEC (VECZ, VEC3, 2.DO)
CALL VAD (VEC1, VEC3, VEC2)
                                                                                                                                                                                                                                                                                                         CALL HATYV (MATZ, VEC3, VEC1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      MATXV (MAT2, VEC1, VEC2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       MATHPY (ARE, MATZ, MAT1)
CXVEC (VEC1, VEC2, 2-D0)
                                                                         VECTOR (XDOT, VEC2,3)
MATXV (MAT1, VEC2, VEC3)
                                                                                                                                                      MATXV (A"IT, VEC3, VEC2)
                                                                                                                                                                                                                                                                                                                                                                                   CALL CXVEC (VEC3, VEC1,2.DO CALL VAD (VEC1, VEC2, VEC3) CALL MATXV (E23, VEC3, VEC1) CALL MATXV (ARI, VEC1, VIC2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             CALL MATKY (ART, VEC2, VEC1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            VSUB (VEC1, VEC2, VEC3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             CALL VAD (VEC3, VEC2, VEC1)
CALL VECTOR (X, VEC2,9)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          MATKV (IH, VEC2, VEC3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          MATXV (IR, VEC2, VEC1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               VAD (VEC1, VEC3, VEC2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             MAIMPY (MATZ, MAT 1, L)
                                                                                                                                                                                                                                                                     CALL VECTOR (XDOT, VEC3,3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          CALL MATKV (ATR, FTR, VEC2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        CALL MATXV (E23, FRT, VEC2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          CALL CXMAT (L, MAT1, CONST)
                                    VAD (VEC 2, VEC 3, VEC 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             CALL VAD (VEC1, VEC2, VEC3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        CALL VAD (VEC2, TSR, VEC1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            TILDE (VEC2, MAT2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          CALL VECTOR (X, VEC1, 3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               TILDE (VEC1, MAT2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  CALL FILDE (VEC1, MAT2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    VECTOR (X, VEC1, 3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         CALL TILDE (VEC1, MAT2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      CALL MAD (IR, MAT1, L)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     CALL TILDE (DT, MAT2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            CONST =-MASSR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               CONST =- MASSR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          CALL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      CALL
                                                                                                                                                                                    600 V.L.(i)=VEC1(I)
PAINT 700 TIME, RG(1), R(1), EULER(1), ANGRAI(1), VEL(1), R
PAINT 700 TIME, RG(1), ANGRAI(2), VEL(2), RG(3), R(3), EULER(
23), ANGRAI(3), VEL(3)
706 PORMAI(1H, //, 1X, '11ME=', G12.5, ', 1H, '3X, 'XG=', G12.5, 7, 1H, '3X, 'YG=', G12.5, 3X, 'P=', G12.5, 3X, 'THEIA=', G12.5, '1H, '3X, 'XG=', G12.5, 3X, 'Y=', G12.5, 3X, 'THEIA=', G12.5, 3X, 'Q=', G12.5, 3X, 'Y=', G12.5, 3X, 'Y=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       CALL TILDE (OMEGIT, MAT1)
CALL MATXV (MAT1, VEC1, VEC2)
CALL WATXV (MAT1, VEC2, VEC1)
CALL WECTOR (KDOT, VEC2, VEC1)
CALL MATXV (MAT1, VEC2, VEC3)
CALL MATXV (MAT1, VEC3, VEC2)
CALL VAD (VEC1, VEC3, CALL VAD (VEC1, VEC3, CALL VAD (VEC1, VEC3, CALL VAD (VEC1, VEC3, VEC2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         CALL CXVEC (FRT, VEC3, CONST)
CALL YSUB (VEC3, VEC2, VEC1)
CALL HAIXV (E1, VEC1, VEC2)
XDOT(13) = VEC2(1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             HATXV (MAIT, VEC1, VEC2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   CALL WECTOR (X,VEC1,0)
CALL MARXV (ATST,VEC1,VEC2)
CALL VAD (VEC2,RAT,VEC1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        CALL MATXV (MAT1, VEC1, VEC2)
CALL MATXV (MAT1, VEC2, VEC1)
CALL MATXV (ASTT, VEC1, VEC3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            CALL MATXV (MATZ, VEC1, VEC2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          MATXV (ASTT, VEC2, VEC1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          KDOF(E+6) = VEC2(E)
CALL VECTOR(K, VEC1, 0)
CALL MATKY (AIST, VEC1, VEC2)
CALL WAD (RAI, VEC2, VEC1)
                                 CALL MATYW (MAT1, BAT, VECZ)
CALL MATXW (ASTT, VECZ, VECT)
CALL MATXW (ART, VEC1, VECZ)
CALL WAD (VECZ, VEC3, VEC1)
                    MATYV (MATI, BAT, VEC2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               CALL WECTOR (X, WEC1, 9)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          CALL VECTOR (X, VEC1, 3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     CALL VECTOR (X, VEC2,9)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          CALLILDE (VECZ, MAF2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      DO 900 I=1,3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 5.4=.,612.5)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     CONTENUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                Srop
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        900
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               005
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104
            SGBROUTINE DHKG, (PRMI, Y, DERY, NDIM, IHLE, PCI, OUIP, AUX)
DIMENSION Y (NDIM), DERY (NDIM), AUX (3, MDIM), A (4), B (4)
1, C (4), PAHT (5)
DOUGLE PRECISION PRAI, Y, DERY, AUX, A, B, C, X, XEND, H, AJ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               PREPARATIONS OF PIRST RUNGE-KUTTA STRP
                                                                                                                     100 AUK(U,I) = 0666666666666000 7DU * DERY(I)
                                                                                                                                                                                                                                                                                                 PREPARATIONS FOR MUNGE-KUTTA METHOD
                                                                                                                                                                                                                                                               IF (H* (KEND-X)) 3800, 3706, 203
                                                                                                                                                                                                                                                                                                                              A(2) = 29289321881345248D0

A(3) = 1.7071067611665475D0

A(4) = 166666666666667D0

B(1) = 2.00

B(2) = 1.00

B(3) = 1.00

B(4) = 2.00

C(1) = 500
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             START OF A RUNGE-KUTTA STEP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         IP ( (X+A-XEND) *H) 700,600,500
                                                                                                                                                                                                                                                                                                                                                                                                                                                                            C(2) = 29289321341345248DU
C(3) = 1,7371367811865475D0
                                                                                   1, 3J, CJ, 41, R2, DELT, EBSS
50 100 L=1, NDIM
                                                                                                                                                                                                            CALL FCT(X,Y,DERY)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  A'IX (2, I) = DERY (I)
AUX (3, I) = 0.D0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              MIGN. 1=1 008 00
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             AUX (1, 1) =Y (I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    AUX (6, I) =0.D0
                                                                                                                                                                                           PAA1 (5) =0.00
                                                                                                                                                           XEND=PRMT (2)
                                                                                                                                                                                                                                               EARUR IEST
                                                                                                                                       X=PR (1)
                                                                                                                                                                                                                                                                                                                  A(1) = .500
                                                                                                                                                                            H=P4MT (3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             C(4) = . 500
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                H=XEND-X
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        IHLP=-1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ISTEP=0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     IREU=0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         I END=0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               500 H=XEND-
600 IEND=1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       H+H=H
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    300
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               007
                                                                                                                                                                                                                                                                                                                  200
                                                                                                                                                                                                                               o o
                                                                                                                                                                                                                                                                               OO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              00
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            000
                                                                                                                                                                                                                                                                                        SUBMOJIINE JUTPLI (TIME, X, XDJI, IHLF, NEU, PRMI)
                                                                                                                                                                                                                                                                                                  IMPLICIT AFAL*3 (A-H,H,J-Z)
DIMENSION X(13),XDOT(13),PRRT(5)
IF((IME-PRET(1)),LI, 1,D-5)GO TO 100
IF(NSIRP-NSIRP*1), DI 100
USTER-NSIRP*1
CALL MAFINV(L.LINV, DEFEP)
CALL MAFXY(LINV, VACZ, VEC3)
DD 1000 1=1,3
0 XDOT(I+9)=VEC3(I)
HATURN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Paint 200, (X(I), I=1, 13)
Paint 200, (XDOF(I), I=1,13)
PJRMAI(IH, 2X,0 (G12,5,3X))
                                                                                                                                                                                                                                                                                                                                                                                                                                            RAD=57.2957795100
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  PRINT 200, TIME
                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ANG1=X (7) *AAD
ANG2=X (8) *RAD
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ANG 3=X (9) *RAJ
                                                                                                                                                                                                                                                                                                                                                                                                                CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                  NJ48=10
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      NS I EP= 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            RETURN
                                                                                                                                                                                                                                                                                                                                                                                                 ARTORN
```

30.

1000

200

RECORDING OF LALTIAL VALUES OF THIS SIEP

700 CALL UNTP (X, Y, DERY, IREC, NDIM, PRAT)

```
2400 DELE=DELT+AUK (8, I) *DABS (AUX (4, I) -Y (I))
IP (DELT-PAMT (4)) 2800, 2800, 2500
                                                                                                                                                                                                                                                                                           Y(I)=AUX(5,I)
DERY(I)=AUX(7,I)
CALL OUTP(X-H,Y,DERY,IHLF,NDIM,PEHT)
IP(PRHT(5))4000,3000,4000
DO 3100 I=1,NDIM
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      IP (ISTEP-INOD-INOD) 400,3460,400
IP (DELT-,02D0*PRHI(4)) 3500,3500,400
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         CALL GUTP (X, Y, DERY, IRLF, NOIM, PRMI)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             REPURNS TO CALLING PROGRAM
                                                                             IP(IHLP~10)2600,3600,3600
DO 2700 1=1,NDIM
AUX(4,1)=AUX(5,1)
ISTEP=ISTEP+ISTEP-4
                                                                                                                                                                                                  RESULT VALUES ARE GOOD CALL PCT(X,Y,DERY)
DO 29GO [=1,NDIM
AUX (1,I) =Y (I)
                                                                                                                                                                                                                                                                                                                                                                                                                IF (IEND) 3200, 3200, 3900
                                                                                                                                                                                                                                                                                                                                                                                                                                                 INCREMENT GETS DOUBLED
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         IF (IALF) 400, 3300, 3300
                                                                 EARUM IS TOO GREAT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          CALL FCT (X,Y,DERY)
                                                                                                                                                                                                                                                               AUX (2, I) = DERY (I)
AUX (3, I) = AUX (6, I)
      50 2400 I=1, NDIM
                                                                                                                                                                                                                                                                                                                                                                                      DERY(I) =AUX(2,I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ISTEP-ISTEP/2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    LSTEP-ISTEP/2
                                                                                                                                                                                                                                                                                                                                                                      X (I) = AUX (1, I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         THOD=ISTEP/2
                                                                                                                                                                                                                                                                                                                                                                                                                                                              IALP=IHLP-1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   IHLF=IHLF-1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             0068 n100
                                                                                                                                                                      GJTO 1600
                                                                                                                                                                                                                                                                                                                                                                                                    REC=IHLF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               3010 3400
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 3050 400
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           IHLP=11
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             3700 IHLP=12
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            3800 I.ILF = 13
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       RETIN N
                                                                                                                                                         IEND=0
                                                                                                                                           H-X=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            H+H=K
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    X+11-11
                                                                              7500
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           3600
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          3400
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         3330
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      3400
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   3500
                                                                                              0097
                                                                                                                                                                                                                                                                                                            2900
                                                                                                                                                                                                                                                                                                                                                       3000
                                                                                                                                                                                                                                                                                                                                                                                      3100
                                                                                                                                                                                                                                                                                                                                                                                                                                                              3200
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       0007
                                                                                                            2700
                                                                                                                                                                                                                   2800
                                                                                                                                                                                                                                                                                                                                                                                                                        IN CASE ITEST=0 THERE IS NO POSSIBILITY FOR TESTING OF ACCURACY.

DO 1700 I=1, NDIM
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    IN CASE IFEST=1 TESTING OF ACCURACY IS POSSIBLE
                                                                            START OF INNERMOST RUNGE-KUTTA LOUP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      IF (ISTEP-INOD-IMOD) 2100,2300,2100
                                                                                                                                                                                                                                                                                                                                     END OF INNERMOST BUNGE-KUTTA LOOP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       COMPUTATION OF TEST WALUE DELT
                                                                                                                                                                                                                                 110 AUX (6, I) = AUX (6, I) + R2-CJ*R1
IF (J-4) 1200, 1500, 1500
                                                                                                                                                                                                                                                                                                                                                                                      TEST OF ACCURACY
1500 IF(fIEST) 1600,1600,2000
IP (PRAT (5)) 4660, 800, 400J
                                                                                                                                                                                  R2=AJ* (R1-BJ*AUX (6, I))
Y(I) = Y(I) + R2
                                                                                                                                                                                                                                                                                 IF (3-3) 1300, 1400, 1300
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ISTEP=ISTEP+ISTEP-2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           2100 CALL PCT (X, Y, DERY)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       DO 1900 I=1,NDIM
Y(I)=AUX(1,I)
DERY(I)=AUX(2,I)
                                                                                                                                                                                                                                                                                                             CALL FCT(X,Y,DERY)
GUTO 1000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 AUX (6, I) = AUX (3, I)
GOTO 900
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          DO 2200 I=1, NDIM
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        30X (7, I) = DERY (I)
                                                                                                                                                             DO 1100 I=1, NDIM
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          AUX (5, I) =Y (I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              2000 INOD=ISTEP/2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 AUX (4, I) =Y (I)
                                sou itesf=0
900 [STEP=ISTEP+1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              IHLP=IHLP+1
                                                                                                                                                                           RI=H*DERY (I)
                                                                                                                                                                                                                        R2=B2+B2+B2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           2300 DELT=0.D0
                                                                                                                                                                                                                                                                                                   1300 X=X+.5D0*H
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          H= 2005 -H
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    I PES 7= 1
                                                                                                                      A3=A (3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                H-X=X
                                                                                                                                    6J=B(J)
                                                                                                                                                    (C) = C()
                                                                                                                                                                                                                                                                      1200 J=J+1
                                                                                                          1=1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            2200
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          1900
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       1600
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       1700
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   1900
                                                                                                                                                                                                                                                                                                                   1400
                                                                                                                        1000
```

APPENDIX C

AERODYNAMIC COEFFICIENTS

In this appendix, aerodynamic data for a typical SHORADS rocket, the motion of which was simulated in this study, is presented and the way in which this data is used in the flight simulation code is described. This data was provided by Mr. John Howerton, U.S. Army Research and Development Command, Redstone Arsenal. Alabama.

C_{N} and C_{y}

The coefficients C_N and C_y are obtained from C_N for which values are given in Table C-la for twenty-seven Mach number values and two incidence angle $(i_T = \sqrt{\alpha^2 + \beta^2})$ ranges, $i_T \leq 4^\circ$ and $i_T \geq 4^\circ$. During the simulation, when values of C_N and C_y are needed, the incidence angle is computed and the proper one-dimensional array of stored C_N values is chosen. Corresponding Mach numbers which bracket the flight Mach number are determined next and the value of C_N used in computing C_N and C_y is determined by linear interpolation. For the rocket considered herein, C_N and C_y for $i_T > 4^\circ$ are computed using $C_N = C_N$ and $C_N = C_N$ and $C_N = C_N$ is a function of Mach number as shown by Table C-la.

 $\frac{c}{A_o}$

Values of the axial force coefficient, $^{\text{C}}_{A_0}$, as a function of Mach number are given in Table C-la also. A linear interpolation subroutine contained in the simulation code is used to determine the proper value of $^{\text{C}}_{A_0}$.

TABLE C-1. AERODYNAMIC CHARACTERISTICS.

	C _N _{\alpha}	C _N _α	C _N o	C _{Ao}
M	i _t <4°	i _t >4°	i _t >4°	
0.0	15.0	26.0	-0.8	0.44
0.1	15.0	26.0	-0.8	0.44
0.2	15.0	26.0	-0.8	0.433
0.3	15.6	26.1	-0.79	0.430
0.4	15.0	26.1	-0.78	0.42
0.5	15.5	26.4	-0.74	0.416
0.6	16.0	26.5	-0.70	0.41
0.7	16.25	26.7	-0.71	0.41
0.8	16.2	26.5	-0.72	0.41
0.85	16.25	26.7	-0.725	0.415
0.90	16.7	27.0	-0.74	0.435
0.925	17.1	27.5	-0.74	0.46
0.95	17.5	27.6	-0.74	0.50
0.975	17.7	27.8	-0.725	0.55
1.0	18.0	28.0	-0.715	0.605
1.025	18.2	28.3	-0.71	0.645
1.05	18.5	28.5	-0.705	0.665
1.075	18.6	28.6	-0.70	0.685
1.1	19.0	28.7	-0.70	0.69
1.15	19.1	28.9	-0.70	0.68
1.2	18.9	28.5	-0.70	0.66
1.25	18.8	28.0	-0.70	0.605
1.3	18.6	27.5	-0.695	0.57
1.4	18.5	27.0	-0.695	0.55
1.5	18.0	26.2	-0.625	0.54
1.6	18.0	25.5	-0.550	0.53
1.7	18.0	25.0	-0.480	0.53
i				

TABLE C-1 (CONT)

T (DECREES	C tp) Ms1	C _{fp}
0.0	-10.81	-9.406
1.0	-11.80	-10.56
2.0	-12.51	-11.59
3.0	-12.99	-12.52
4.0	-13.30	-13.32
5.0	-13.50	-14.02
8.0	-13.96	-15.42
10.0	-14.77	-15.78
12.0	-16.54	-15.68

CANARDS DEPLOYED	MO CAMARD DEPLOYMENT
-320.0	-250.0
-350.0	-300.0
-370.0	-330.0
	CANARDS DEPLOYED -320.0 -350.0

(c)

(b)

Er PERCENT ACTUATOR PISTON TRAVEL	Br PERCENT CANARD DEPLOYMENT		
0.0	57.0		
5.0	57.0		
7.5	58.0		
10.0	59.0		
15.0	64.25		
20.0	69.5		
25.0	74.25		
30.0	79.0		
35.0	82.5		
40.0	86,0		
45,0	88,25		
50.0	90.5		
55.0	92.0		
60.0	93.5		
65.0	95.0		
70.0	96.5		
75.0	97.25		
80.0	98.0		
85.0	98.5		
90.0	99.0		
95.0	99.5		
100.0	100.0		

B _r M	0.9	1.0	.1.05	1.15	1.3	1.5
57	1000.0	968.0	955.0	945.0	942.0	947.0
60	1003.0	974.0	963.0	953.0	951.0	955.0
65	1013.5	998.5	978.5	967.5	964.5	967.0
70	1024.0	1003.0	994.0	982.0	978.0	979.0
75	1039.5	1020.0	1011.0	999.0	994.0	995.0
80	1055.0	1037.0	1028.0	1016.0	1010.0	1012.0
85	1079.0	1057.0	1047.0	1034.0	1027.0	1028.5
90	1104.0	1079.0	1067.0	1054.0	1048.0	1049.0
95	1132.0	1104.0	1090.0	1076.0	1080.0	1070.0
100	1162.0	1125.0	1110.0	1100.0	1096.0	1100.0

f₂(B_r,M)
(e)

f ₂	r i
(MILLIMETERS)	(DEGREES)
0.0	0.0
-2.0	1.0
~8.0	2.0
-16.0	3.0
-24.0	4.0
-30.0	5.0
-36.0	7.0
-38.0	9.0
-38.0	12.0

(f)

 $\frac{c_{\ell}}{p}$

The roll damping coefficient, C_{ℓ} , is given in Table C-1b as a function of incidence angle, i_T , for Mach numbers less than and greater than unity. In the simulation code linear interpolation is used to find the proper C_{ℓ} value.

C and C n

The pitch and yaw rate damping coefficients, C_{m_q} and C_{n_r} , respectively, are equal, since the rocket is geometrically symmetric with respect to the x-axis. For canard (destabilizing fins) undeployed and deployed, values of the coefficient C_{m_q} are given in Table C-1c along with corresponding values of ℓ -x_{cg}, the distance of the center of mass of the rocket from its nose. The distance ℓ_{cg} is computed in the simulation code during each evaluation of the derivatives of the state variables and the linear interpolation subroutine is used (as in other calculation discussed above) to find the proper value of $C_{m_e} = C_{n_e}$.

 $^{\text{C}}_{\text{ni}_{\alpha}}$ and $^{\text{C}}_{\text{n}_{\beta}}$

For the rocket simulated herein, $C_{n_{\beta}} = -C_{m_{\alpha}}$ and $C_{m_{\alpha}}$ is a function of the center of pressure location x_{cp}^{t} (measured from the aft end of the rocket) which in turn is a function of Mach number, aerodynamic incidence angle and B_{r} , the percent of the total area of the canards (destabilizing fins) which is exposed to the flow field surrounding the rocket. In the simulation code, $C_{m_{\alpha}} = C_{N_{\alpha}} (x_{cp}^{t} - x_{cg})$ and $x_{cp}^{t} = f_{1}(B_{r}, M) + f_{2}(i_{T})$. Here, B_{r} is dependent upon ℓ_{r} , the distance the deployment piston has traveled. The distance ℓ_{r} is a linear function of time which is zero at 0.8 seconds

after booster motor ignition and has its maximum value at 1.7 seconds after booster motor ignition.

To find $C_{m_{\alpha}}$, the value of ℓ_r is first determined. Then B_r is determined by linearly interpolating using the values in Table C-ld. Next, $f_1(B_r, M)$ is found by using a double linear interpolation scheme and the data of Table C-le. The value of i_T and the corresponding value for f_2 are then found from the data listed in Table C-lf. These values of f_1 and f_2 are used to find x_{cp}^{\dagger} and the current value of x_{cg}^{\dagger} is used along with the x_{cp}^{\dagger} value and the appropriate value of $C_{N_{\alpha}}$ to compute $C_{M_{\alpha}}$.